

Outer Scale Definition

Model dependant

Infinite $\phi(\kappa) \propto (\kappa^2)^{-11/6}$

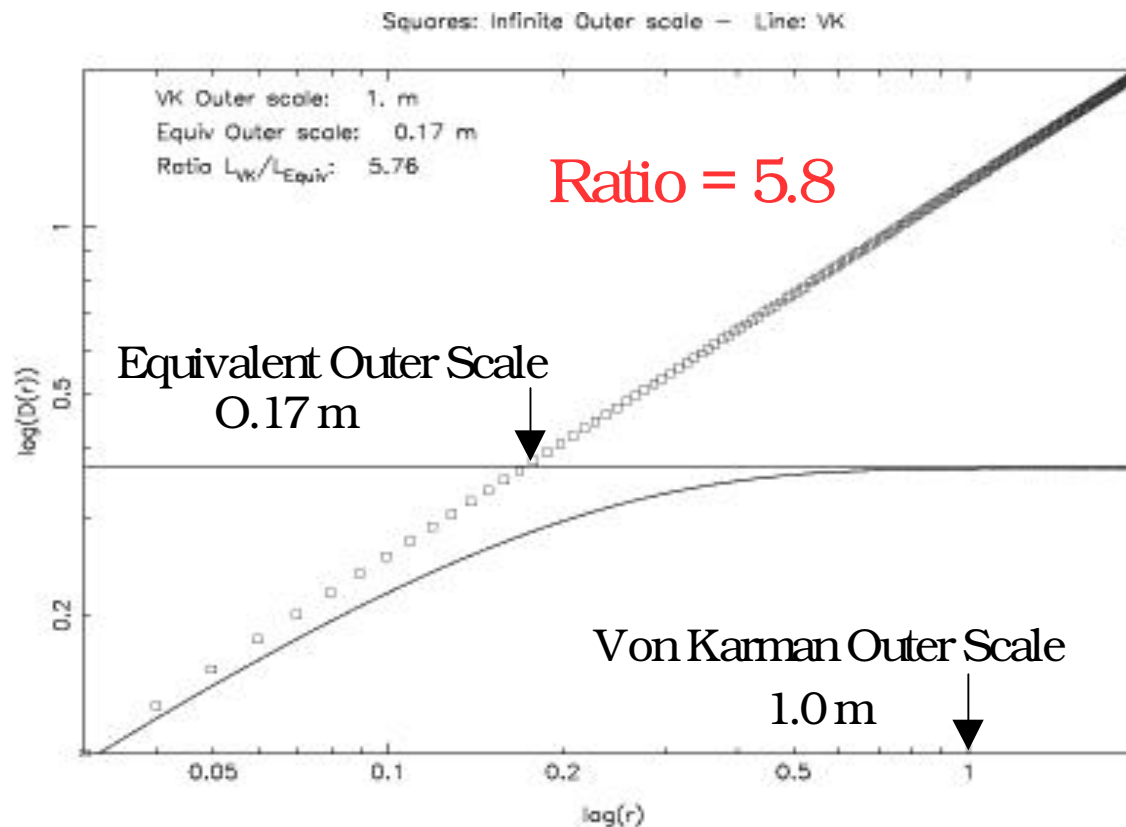
Von Karman $\phi(\kappa) \propto (\kappa^2 + (2\pi/L_0)^2)^{-11/6}$

Equivalent (Tatarski)

$$D_\theta(L_T) = C_\theta^2 L_\theta^{2/3} = \Delta\theta^2$$

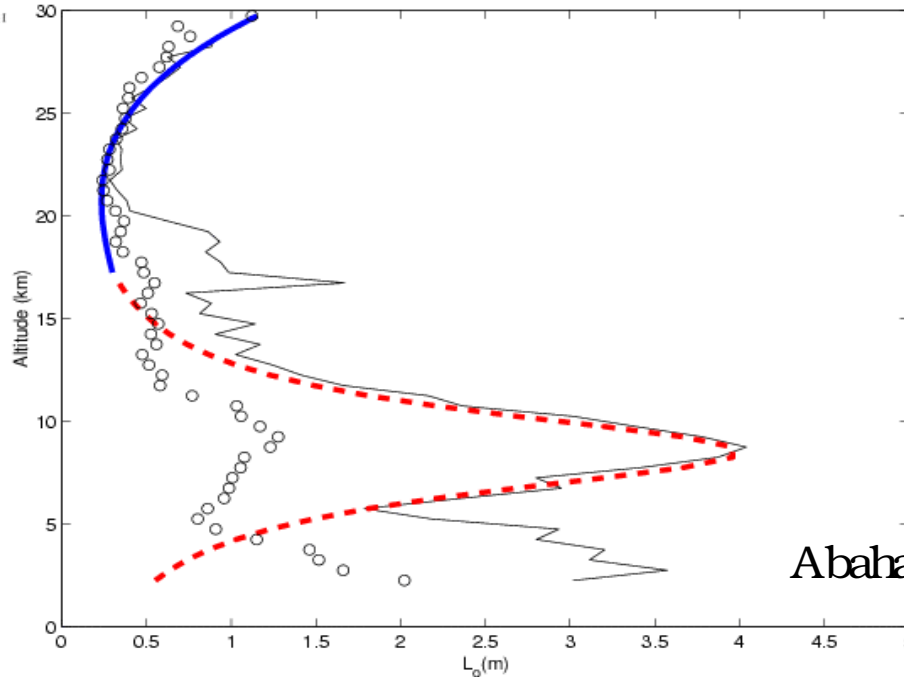
$$C_\theta^2 = a^2 L_\theta^{4/3} (\text{grad } \theta)^2$$

$$D_\theta(r) = \int_0^\infty \left(1 - \frac{\sin(Kr)}{Kr}\right) K^2 \Phi_\theta(K) dK$$



Saturation $\Delta\theta^2$

Outer Scale Scatter



Abahamid, Jabiri, Vernin et al. (2003), A&A, in press

Measurement	Instrument/Telescope	L_0 (m)	Reference
in situ soundings			
Refractive index structure function	Balloons (Paranal, Chile)	2.5	Fuchs ^a 95
Interferometry			
Phase structure function (Ph.S.F.)	I2T (Calern, France)	~ 8	Mariotti <i>et al.</i> ¹⁰ 84
	SUSI (Australia)	5 ~ 10	Davis <i>et al.</i> ¹¹ 95
Ph.S.F. + Phase temporal power spectrum (Ph.T.P.S.)	mounted on WHT (Canary IIs.)	~ $2 \times 2\pi$	Nightingale <i>et al.</i> ¹² 91
	WHT + COAST (Cambridge, UK)	∞	Hannif <i>et al.</i> ¹³ 94
Ph.T.P.S., single baseline	Mark III (Mt. Wilson, USA)	> 2000	Colavita <i>et al.</i> ¹⁴ 87
Ph.T.P.S. with different baselines	Mark III (Mt. Wilson, USA)	~ 30	Buscher <i>et al.</i> ¹⁵ 95
	Mark III (Mt. Wilson, USA)	~ 30	Buscher <i>et al.</i> ¹⁶ 91
	ISI (Mt. Wilson, USA)	5 - 20	Bester <i>et al.</i> ¹⁷ 92
Spectral decorrelation	GIZT (Calern, France)	~ 22	Berio <i>et al.</i> ¹⁸ 96
Shack-Hartmann-kind technique with a single telescope			
AA structure function	CFH (Hawaii)	5 - 8	Tallon ¹⁸ 89
Zernike variances	3.6m ESO (La Silla, Chile)	~ 50	Rigault <i>et al.</i> ²⁰ 91
AA variances	OHP (Provence, France)	5 - 100	Ziad <i>et al.</i> ²¹ 94
Tilt covariances	KECK (USA)	16 - 80	Takato <i>et al.</i> ²² 95
Shack-Hartmann-kind technique with multiple telescopes			
AA covariance	G.S.M. (Calern, France)	10 - 300	Agabi <i>et al.</i> ²³ 95

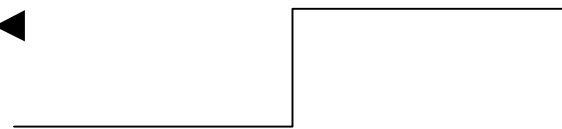
Avila, Ziad et al. (1997)
JOSA, **14**, 3070

Atmospheric Parameters Relevant to AO

To characterize r_0 , θ_{FCAO} , θ_{PCAO} , τ_{AO} , d_0 one needs to know
vertical profiles of optical turbulence $C_N^2(h)$ and wind $V(h)$
with $0 < h < 20\text{-}30$ km

Operational Profilers

Generalized Scidar
Instrumented balloons



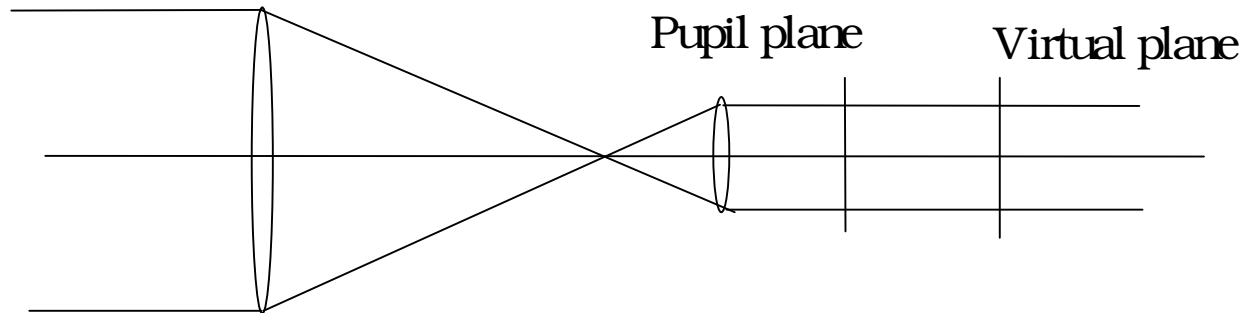
Prototype Profilers

Single Star Scidar's
Slodar

Other combinations

MASS + DIMM + $V(h)$ from meteo model

Single Star Scidar basic equation



$$C(\vec{r}, \tau) = \sum_{i=1}^N C_i(\vec{r}, h_i) * G(\vec{r}, \sigma_{v_i} \tau) * S(\vec{r}) * \delta(\vec{r} - \vec{v}_i \tau)$$

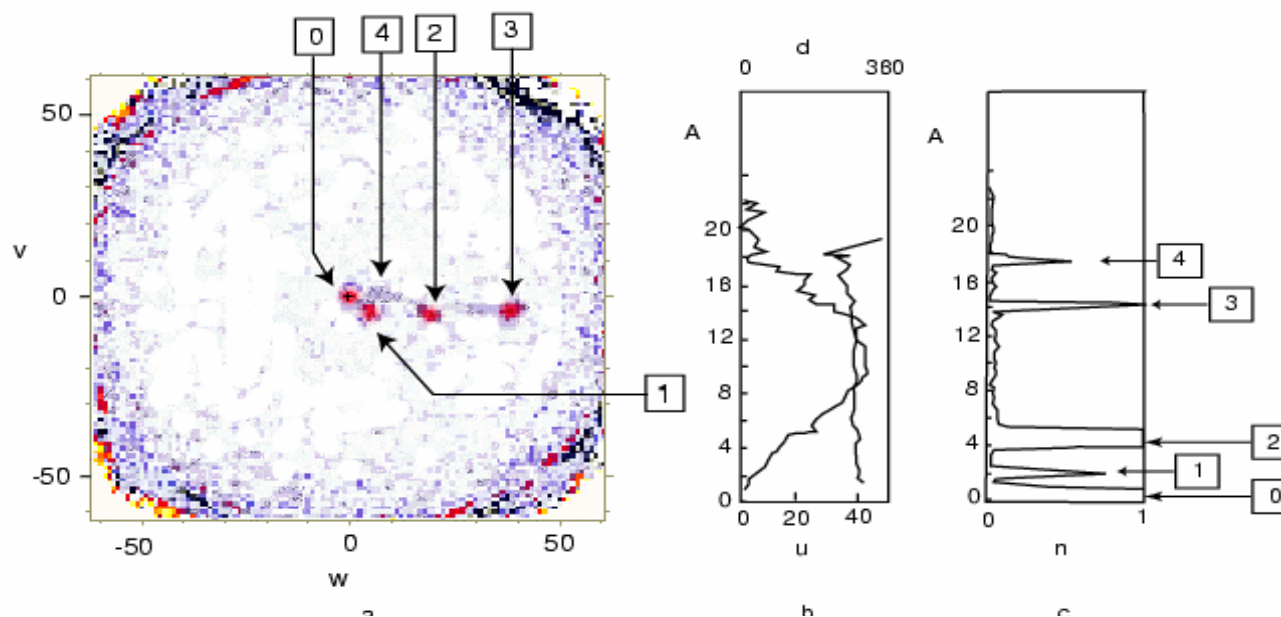
$C_i(\vec{r}, h_i)$ Autocorrelation for a layer at altitude i

$G(\vec{r}, \sigma_{v_i} \tau)$ Gaussian convolution due to wind variations

$S(\vec{r})$ Impulse response of the receiver

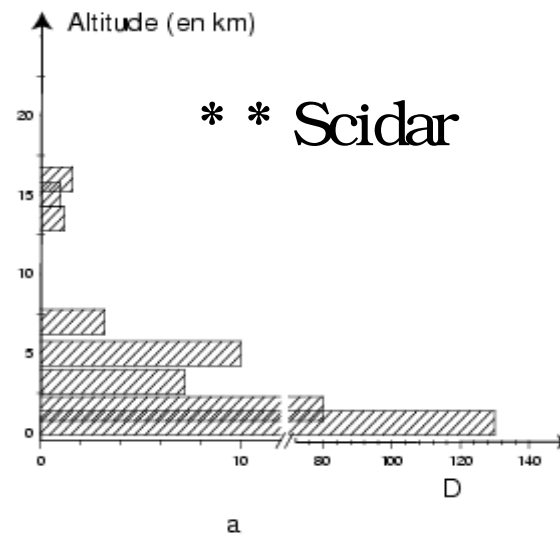
$\delta(\vec{r} - \vec{v}_i \tau)$ Displacement due to wind speed

Single Star Scidar results

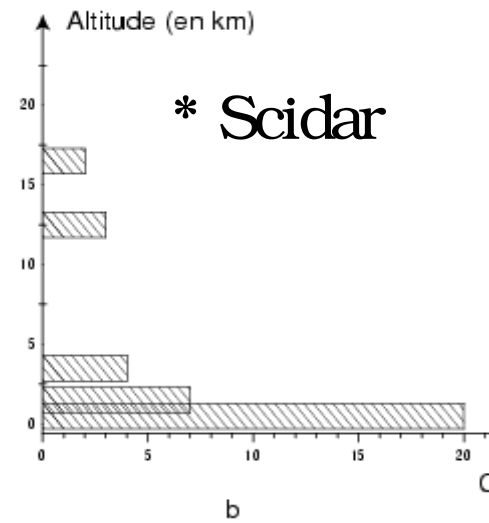


couche	SCIDAR étoile simple					Ballons		
	h_i (km)	σ_{v_i} (m/s)	$C_n^2(h_i)\Delta h_i$ ($\times 10^{-14} \text{ m}^{1/3}$)	$ \vec{v}_i $ (m/s)	Direction ($^\circ$)	h_i (km)	$ \vec{v}_i $ (m/s)	Direction ($^\circ$)
0	0.2 ± 0.1	0.2	25 ± 1.0	0.2	-	0.1	0.1	-
1	2.0 ± 0.2	0.8	07 ± 0.1	06	230	2.3	7	280
2	5.0 ± 0.5	0.6	04 ± 0.1	18	255	4.5	20	270
3	12.5 ± 1.5	0.4	03 ± 0.1	37	264	14	30	260
4	16.2 ± 1.0	0.5	02 ± 0.1	05	260	17.5	6	265

Single Star Scidar vs Generalized Scidar



Seeing** (21h09)=0.55''
Seeing** (22h54)=0.97''

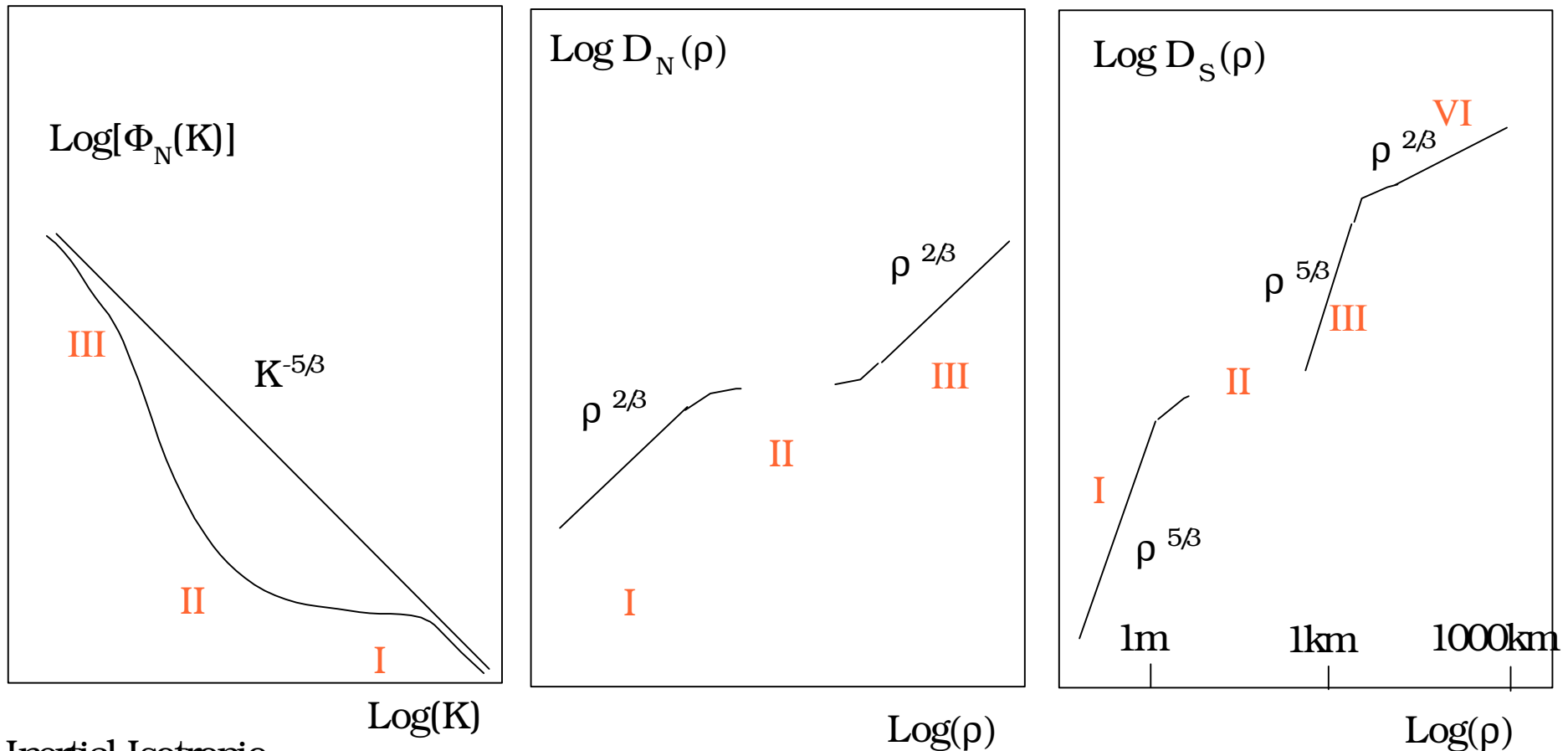


Seeing* (21h20)=0.85''

Habib, Vernin, Benkhaldoun, Submitted to CRAS Paris

Phase Structure Function at various baselines

Coulman, Vernin, 1991, Appl. Opt., **30**, 118



I Inertial Isotropic

II Spectral Gap

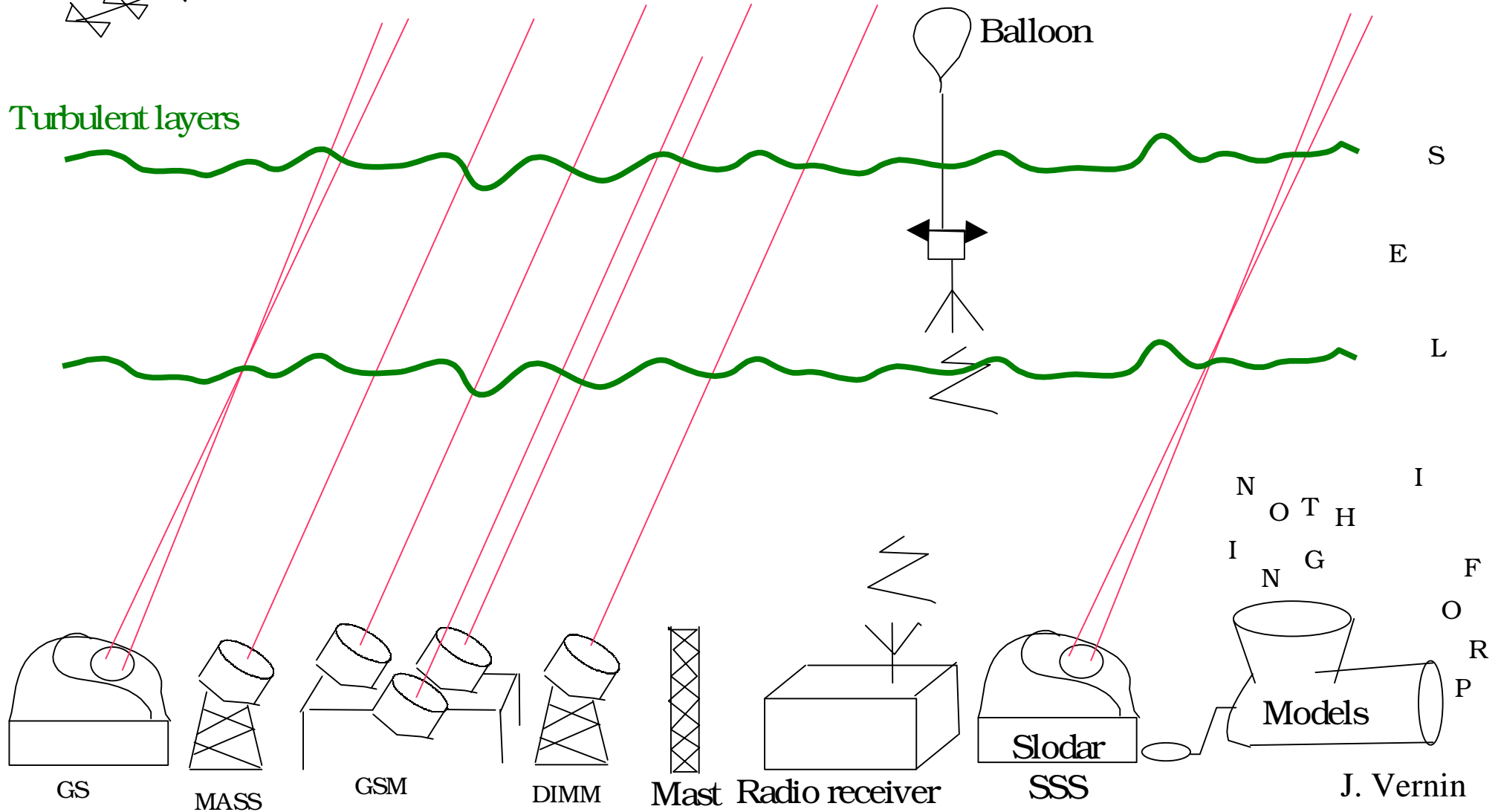
III Anisotropic 2D turb.

Thin atmosphere
 $B < H$

VI Thick atmosphere
 $B > H$

Kite

Instruments



Which model for atmospheric turbulence?

- Verification of the atmospheric turbulence model
- Measurement of atmospheric parameters with the GI2T Interferometer

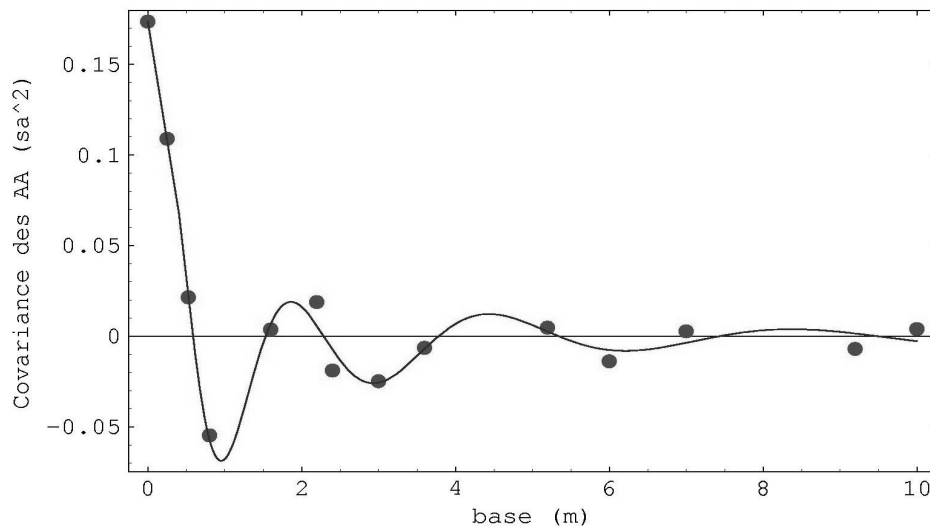


GSM Instrument

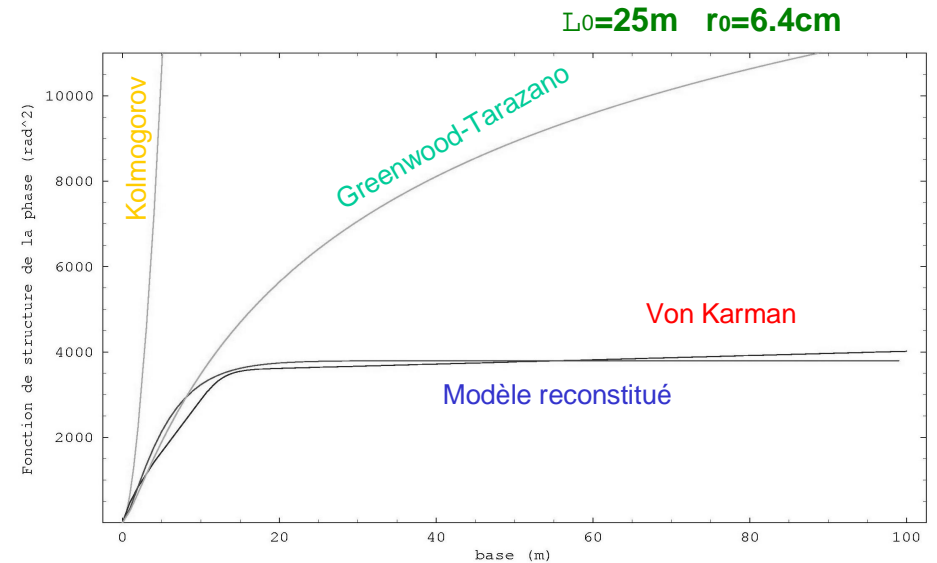
Verification of the atmospheric turbulence model

$$C_\alpha(x, 0) = \frac{\lambda^2}{8\pi^2} \frac{\partial^2 D_\phi(x, 0)}{(\partial x)^2} \quad (\text{F. Roddier, progress in Optics 1981})$$

➔ $D_\phi(x) = \frac{8\pi^2}{\lambda^2} \int \left[\int C_\alpha(x, 0) dx \right] dx + Ax + B$



AA longitudinal covariances measured with the GSM for different baselines



Phase structure function reconstructed from GSM data with $\sigma_{OPD}=10\lambda$

Optical Path Difference in an interferometer

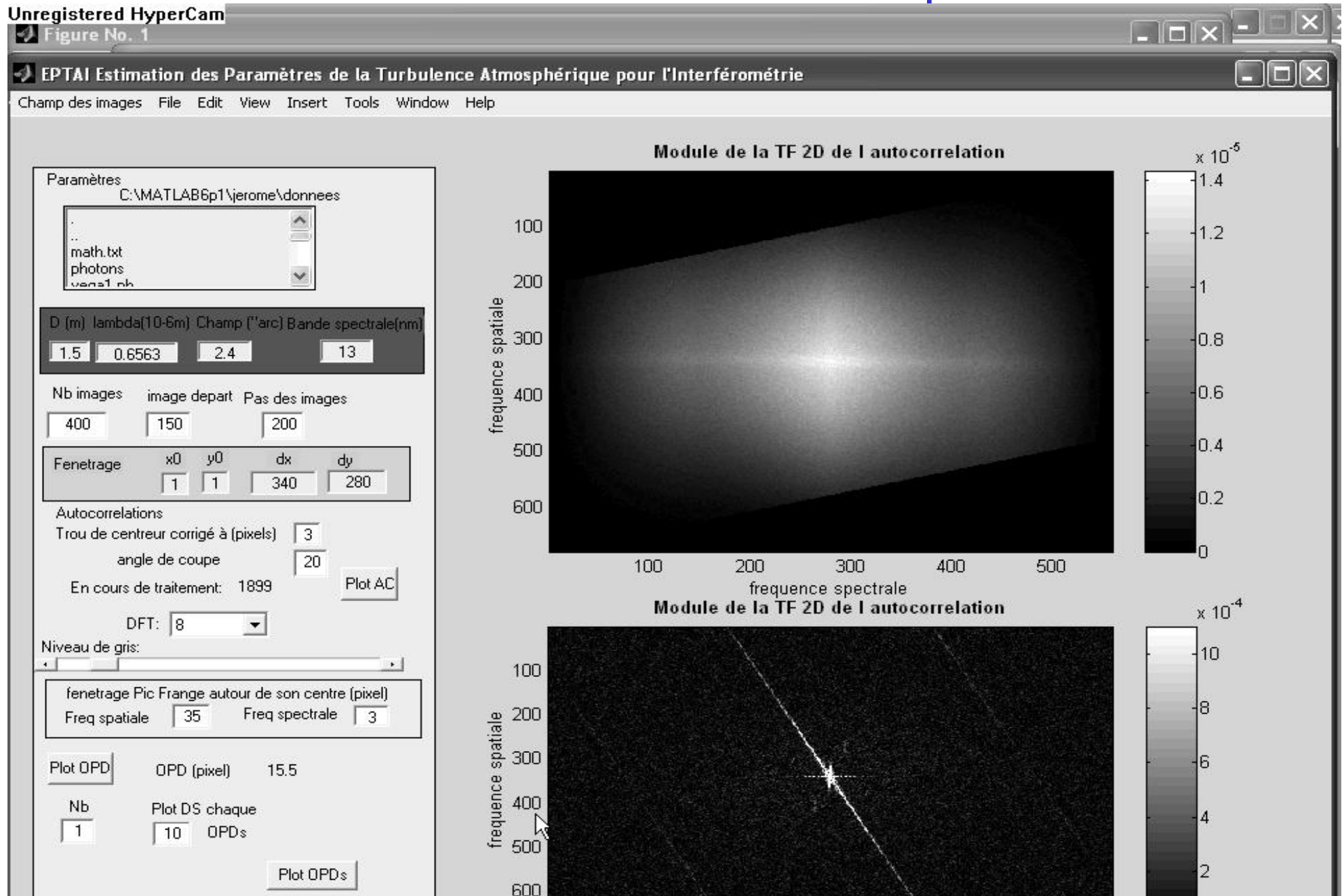
$$\sigma_{\text{OPD}}(b) = \frac{\lambda}{2\pi} \sqrt{\langle |\varphi(\vec{r}) - \varphi(\vec{r} + b)|^2 \rangle} = \frac{\lambda}{2\pi} \sqrt{D_\varphi(b)}$$

$$D_\varphi(b) = 4\pi \int f W_\varphi(f) [1 - J_0(2\pi f b)] \left[\frac{2J_1(\pi D f)}{\pi D f} \right]^2 df$$

- for the Von Karman model:

$$W_\varphi(f) = 0.0229 r_0^{-5/3} \left(f^2 + \frac{1}{L_0^2} \right)^{-11/6}$$

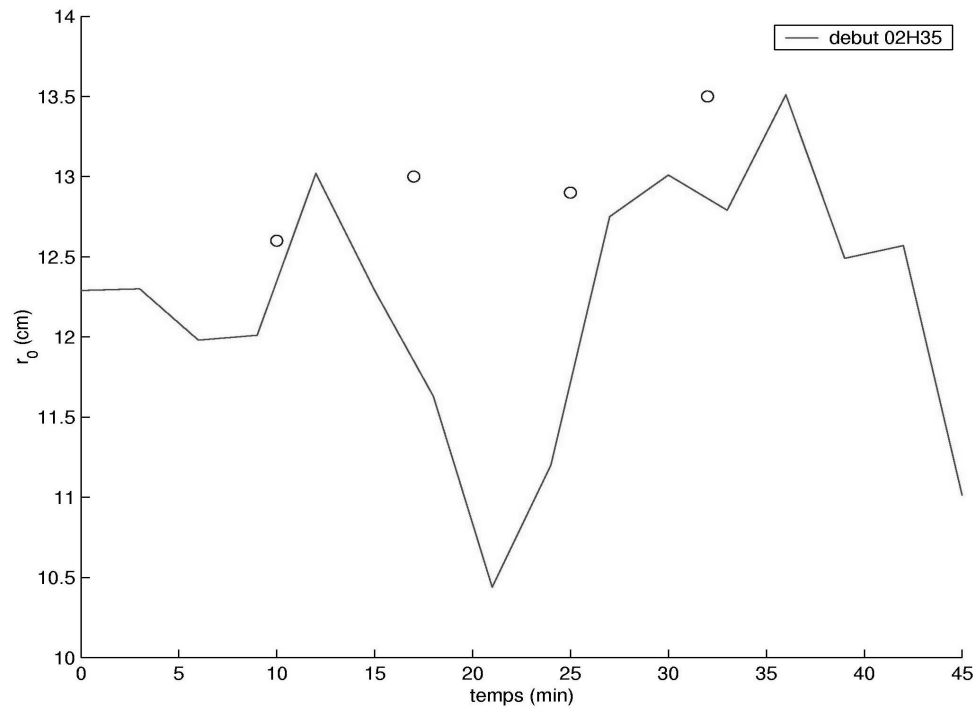
Estimation of the OPD & turbulence parameters with



Estimation of the turbulence parameters

GSM-GI2T observations and first results (06 June 2003)

Comparison r_0 GSM et GI2T



Comparaison L_0 GSM et GI2T

