

# Precision Cosmology from Future Galaxy Cluster Surveys

How do we control various systematics from observations and theory?

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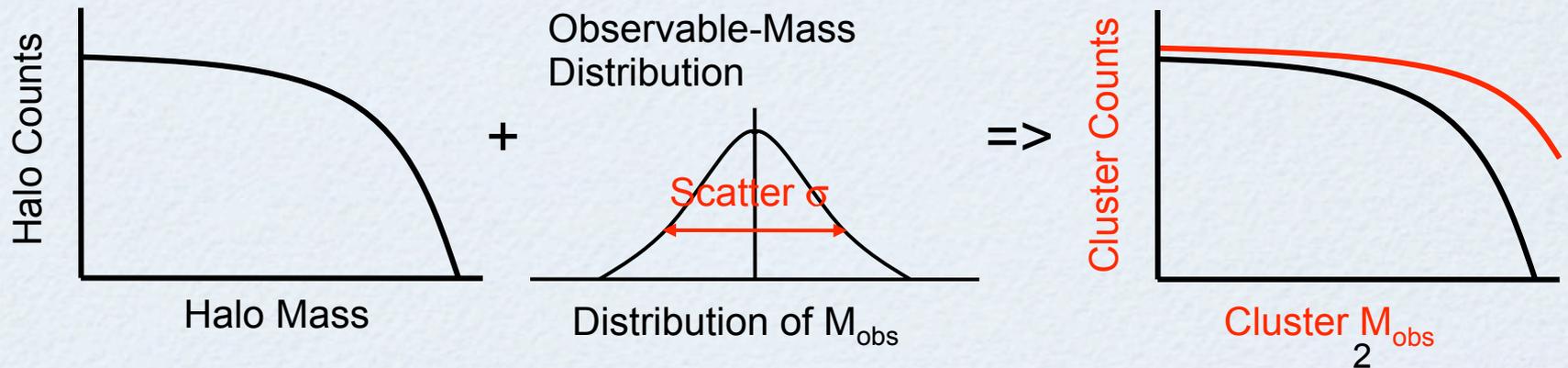
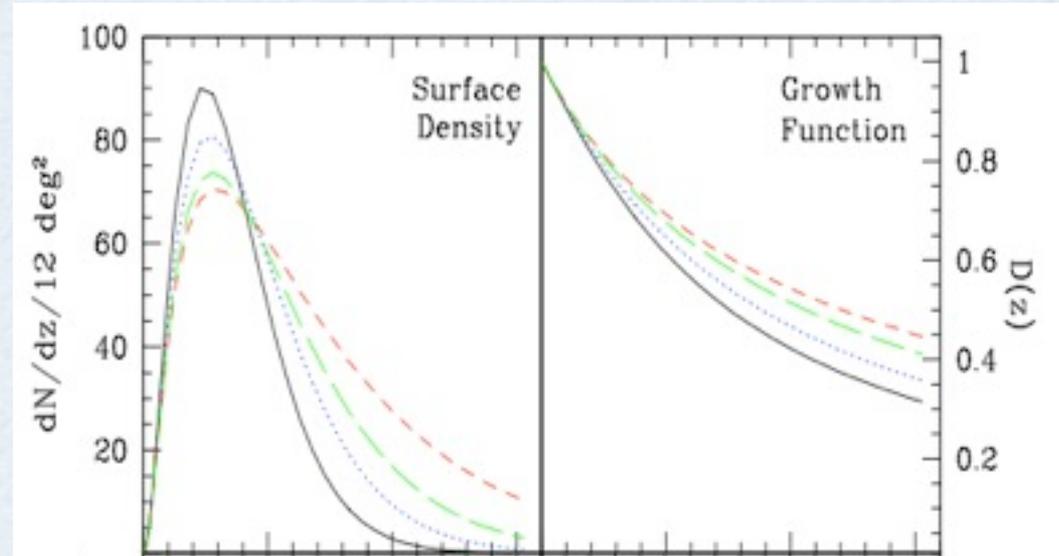
(in collaboration with Risa Wechsler,  
Eduardo Rozo, and Andrew Zentner)

ESO GCEU November 12, 2009

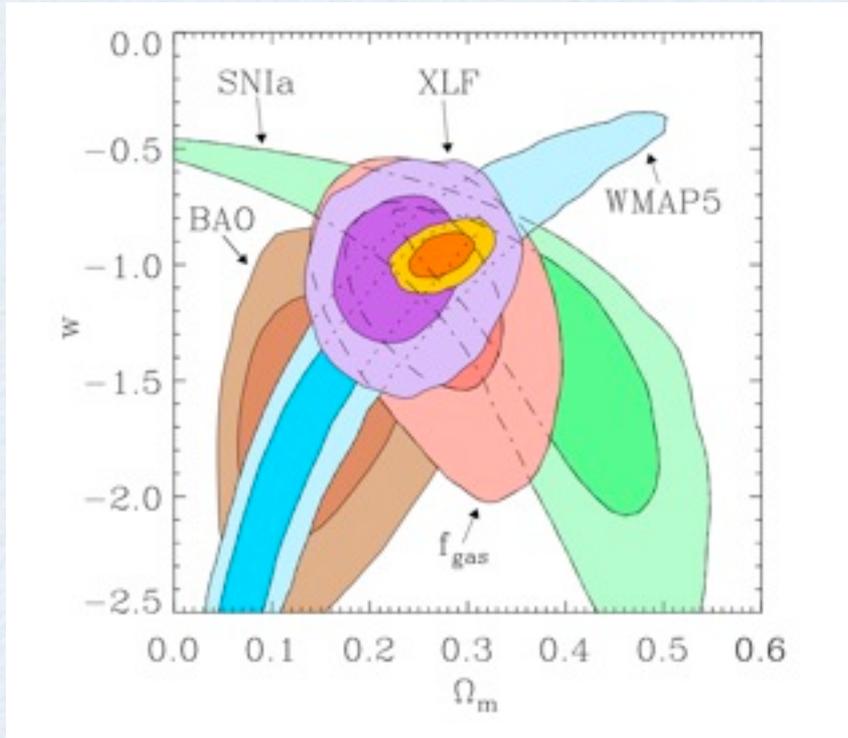
# Cosmology from Galaxy Cluster Counts

- Galaxy clusters probe:
  - Structure growth
  - Expansion rate

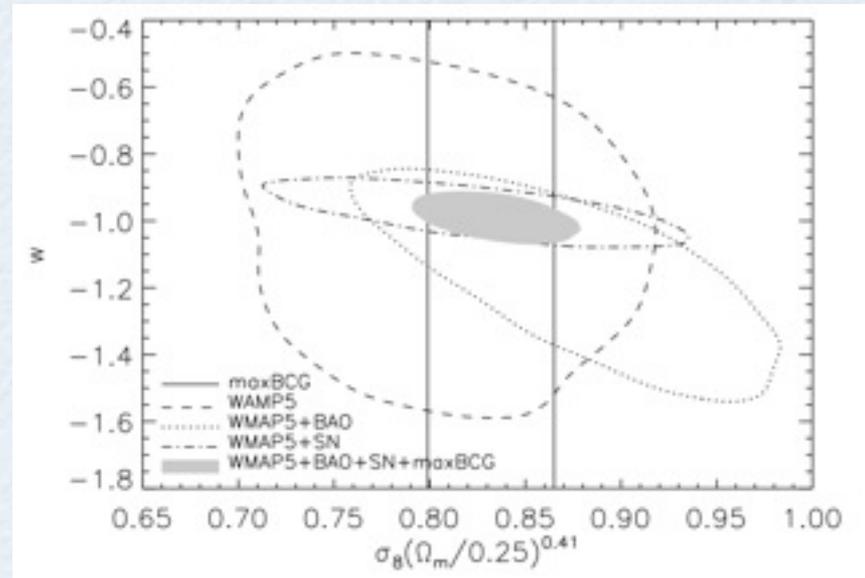
Figure: Haiman '01 ( $w = -1$ ;  $-0.6$ ;  $-0.2$ ; no DE)



# Current Cosmological Constraints from Clusters



Mantz et al. '09 for ROSAT and Chandra Clusters; also see Vikhlinin '09



Rozo et al. '09 for SDSS Clusters; also see Gladders '07 for RCS Clusters

# Outline

- Introduction
- Part I: Follow-ups and observable-mass distribution
  - External constraints from follow-up observations
  - Properties of follow-up mass tracers
  - Optimization of the follow-up target selections
- Part II: Theoretical uncertainties in mass function and halo bias
  - Requirements for future surveys
  - Comparison of different mass and redshift regimes

# The Dark Energy Survey

- Galaxy clusters selected from optical imaging ( $\sim 10^5$ ), 40% scatter
- Survey area = 5000 deg<sup>2</sup>; overlap with the South Pole Telescope (SZ survey)
- Survey depth:  $M_{\text{th}} = 10^{13.7} h^{-1} M_{\text{sun}}$  and  $z_{\text{max}} = 1$

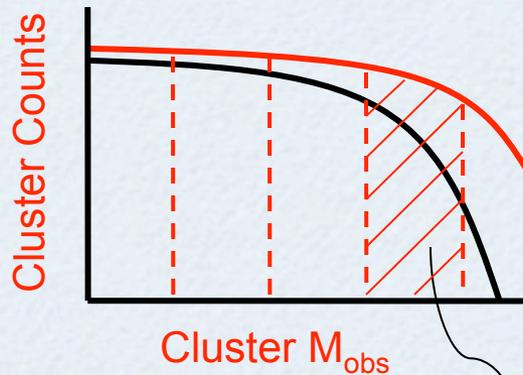
## Self-calibration Analysis

- Using sample variance (clustering of galaxy clusters) to self-calibrate the observable-mass distribution (Lima & Hu '04, '05).

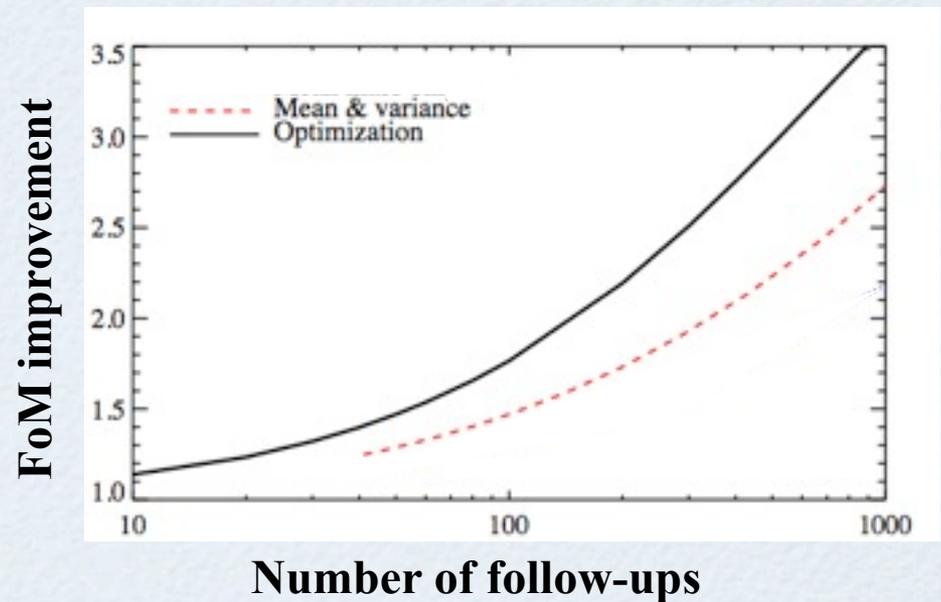
## The Dark Energy Figure of Merit (FoM)

- FoM :=  $1/[\sigma(w_a)\sigma(w_p)] \propto 1/(\text{area of the error ellipse of } w_0, w_a)$
- Current Data (WMAP5+SNe+BAO+X-ray clusters): 15.5 (Mantz '09)
- DETF Report (Albrecht '06): Stage III CL+Planck prior:
  - Optimistic: 35.21
  - Pessimistic: 6.11

# Part I: Follow-ups for DES-like Optical Surveys



Follow up part of the sample in a bin (measure the mass more precisely)

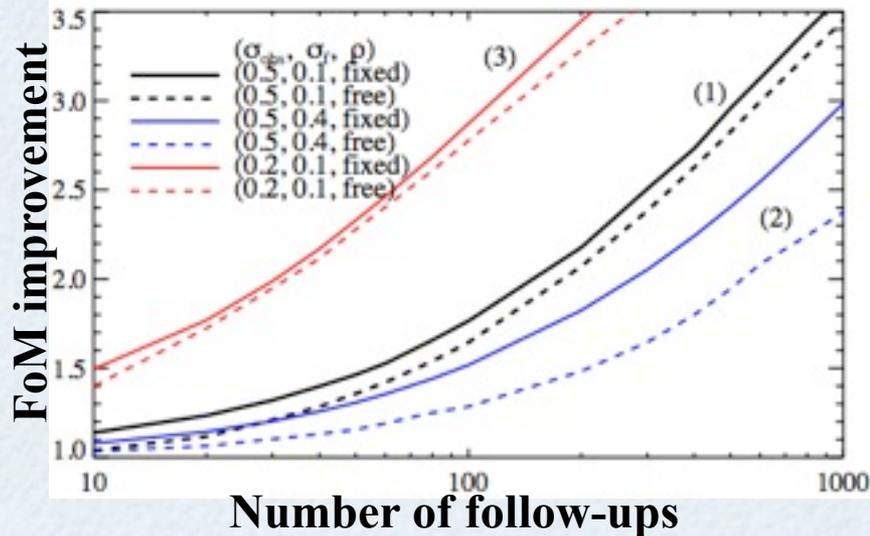


- The mean and variance of the follow-up mass measurements can further constrain the O-M distribution. The variance is particularly crucial for constraining the scatter.
- Optimized follow-up strategy can further improve the FoM.
- With 100 follow-up clusters, FoM can be improved by 77%

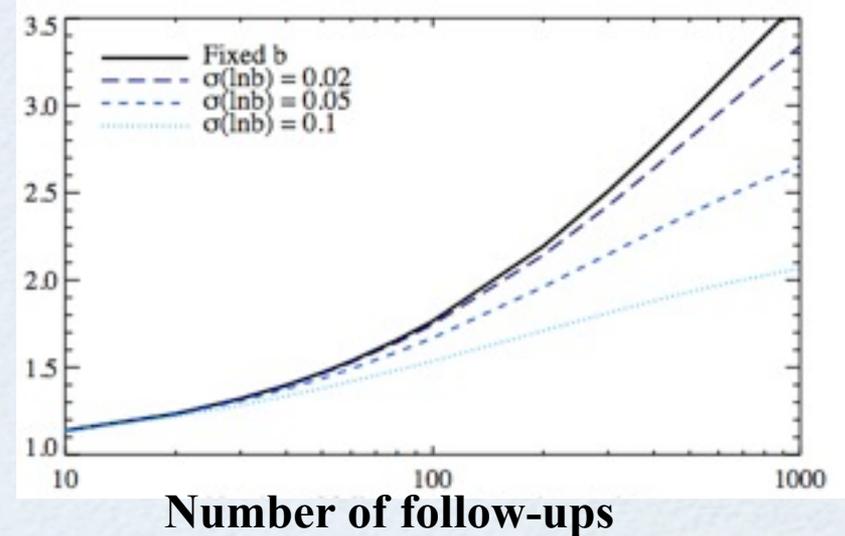
Wu, Rozo, and Wechsler, arXiv:0907.2690; Also see Majumdar and Mohr '03, '04

# Complications: Scatter and Bias of Follow-up Mass Tracers

Scatter: mild degradation



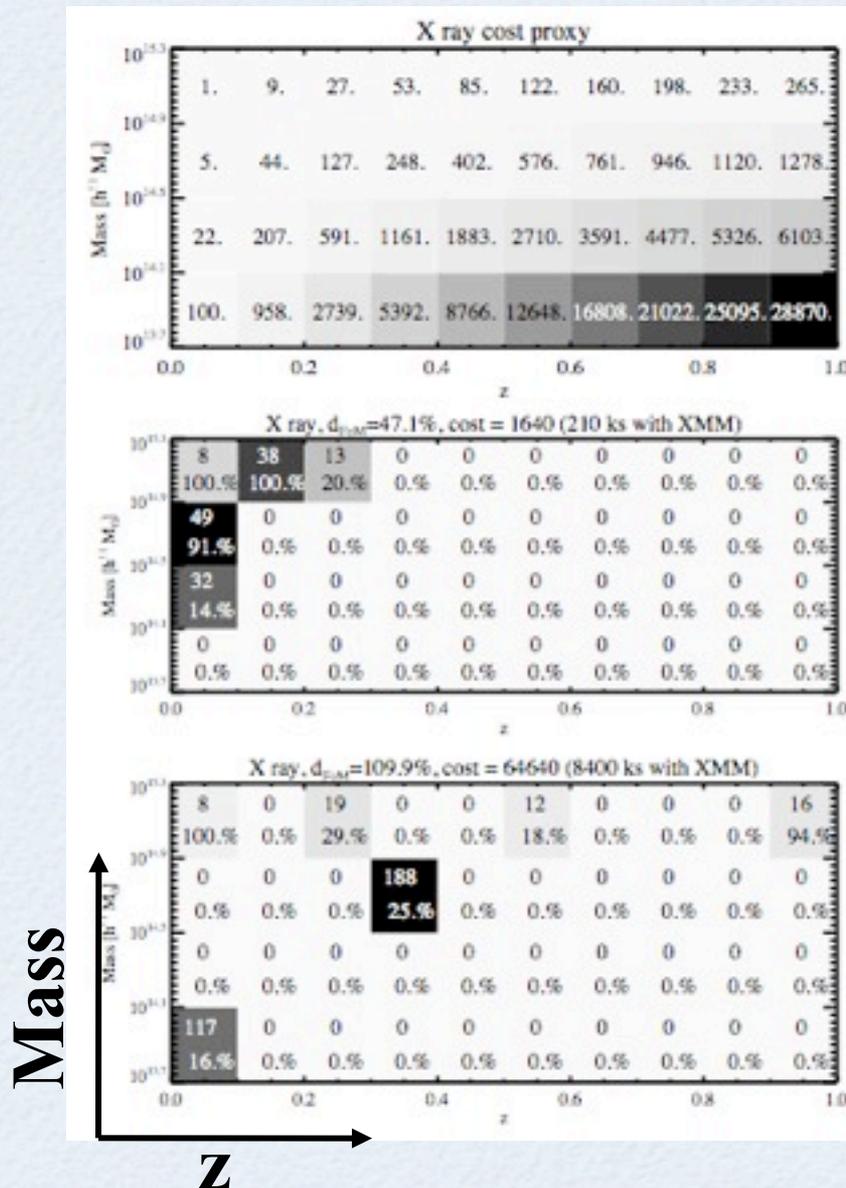
Bias: strong degradation



- Lowering the scatter in survey sample can further improve the power of follow-ups.
- The bias in follow-up mass measurements needs to be controlled at 5% level.

Also see Cunha '08 for cross-calibration; Nagai '07, Rudd '09 for possible bias

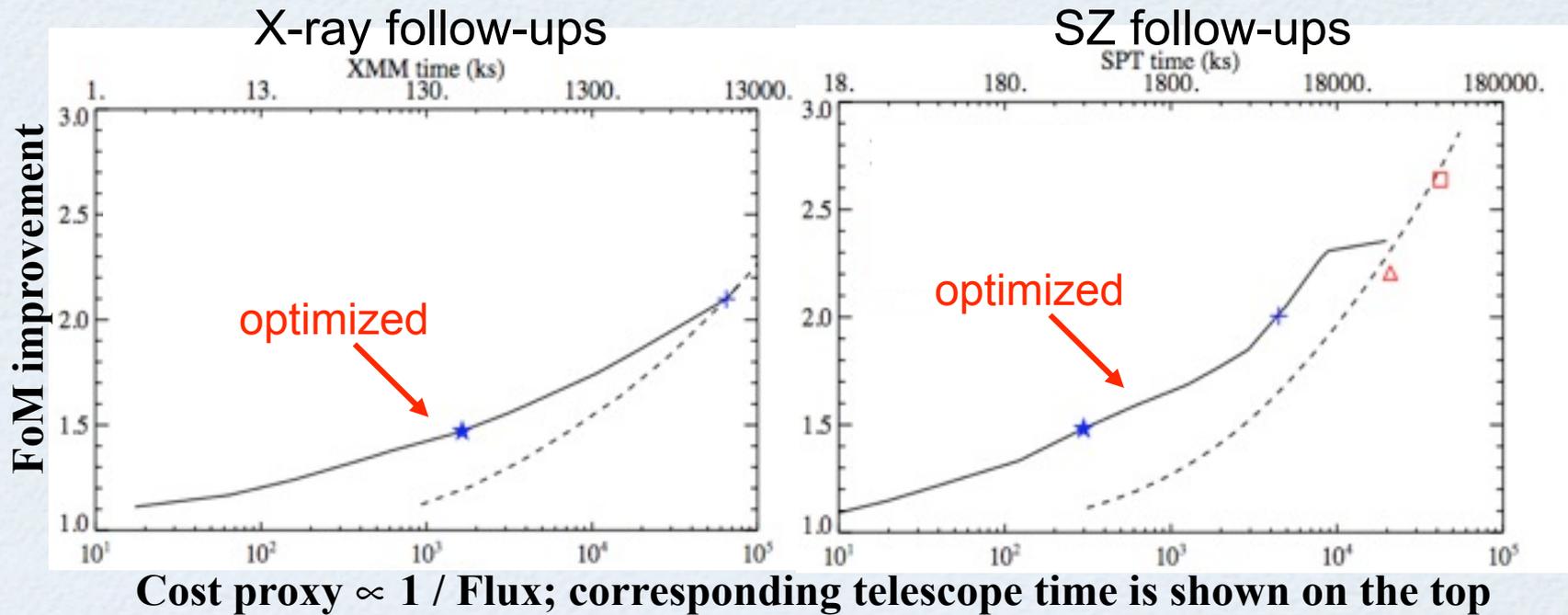
# Optimization: Different Strategies for X-ray and SZ



- Clusters are weighted by their observational cost  $\propto 1 / \text{Flux}$
- X-ray follow-ups
  - Cost is sensitive to redshift
  - Small program: low-z clusters
  - Large program: clusters span a redshift range
- SZ follow-ups
  - Cost is sensitive to mass
  - Small program: massive clusters span over a redshift range
  - Large program: some less-massive clusters



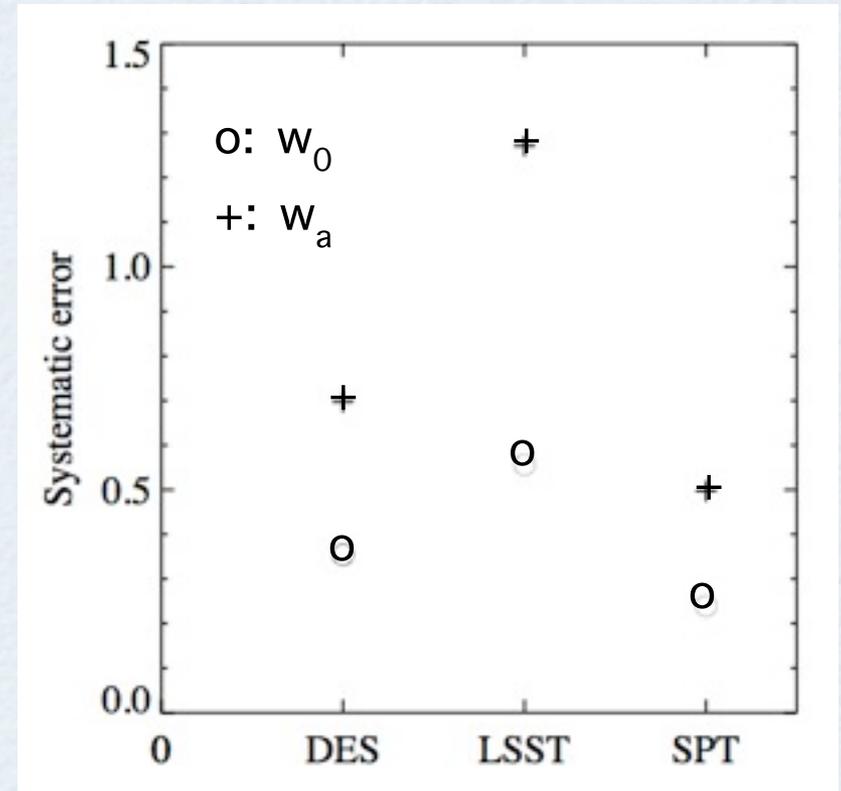
# Optimization: FoM as a function of Telescope Time



- Optimizing the FoM at a given cost can significantly improve the FoM. To achieve a given FoM, the optimization can reduce the cost by an order of magnitude over random selection.

# Part II: Theoretical Uncertainties in Halo Mass Function and Halo Bias

- How does the uncertainty in mass function and halo bias impact the cosmological constraints from clusters? What are the required accuracies of them in future cluster surveys?
- Current theoretical uncertainties in the shape of mass function ( $\sim 20\%$ ) can lead to significant systematic errors in future surveys. We compare Sheth-Tormen '99 and Tinker '08 fitting formulae as an example.

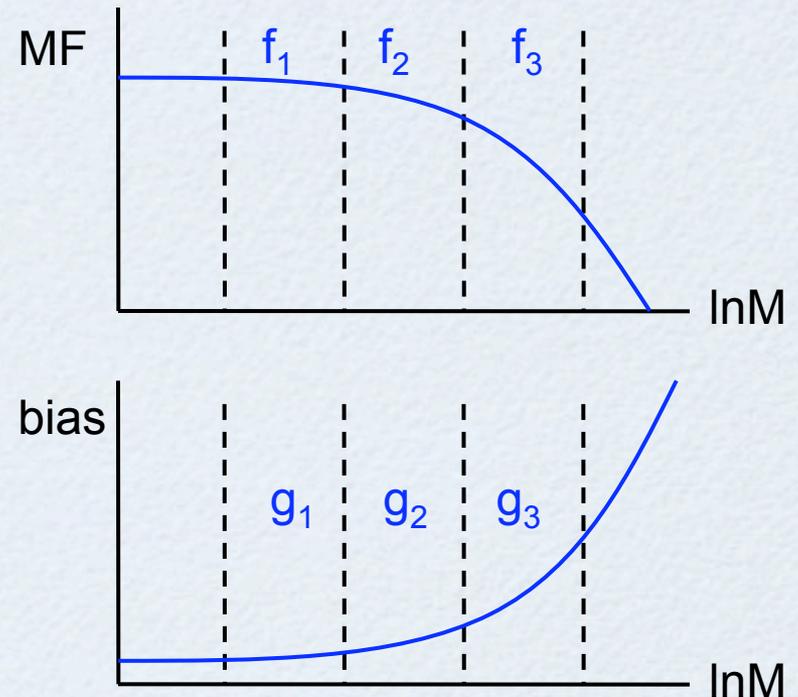


Wu, Zentner, and Wechsler, arXiv: 0910.3668

Also see Wu et al. '08 for the effects of assembly bias

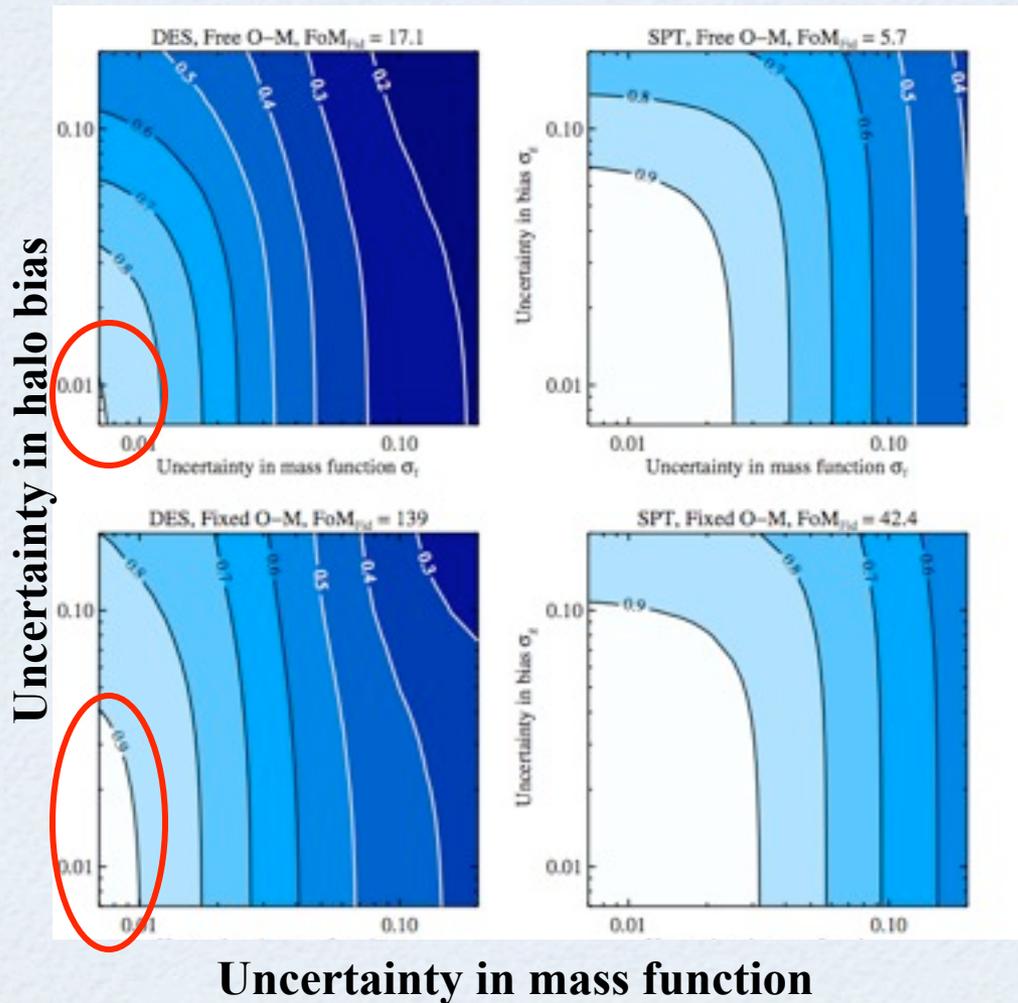
# Modeling the Uncertainties in Mass Function and Halo Bias

- We discretize the mass function and halo bias to describe the uncertainty in a parameterization-independent way.
- The Tinker function is used as the fiducial model.
- We include  $f_i$ 's and  $g_i$ 's as additional nuisance parameters and study their impacts.



Also see Cunha & Evrard '09 for the study of parameters in the Tinker function

# Degradation in the Dark Energy Figure of Merit



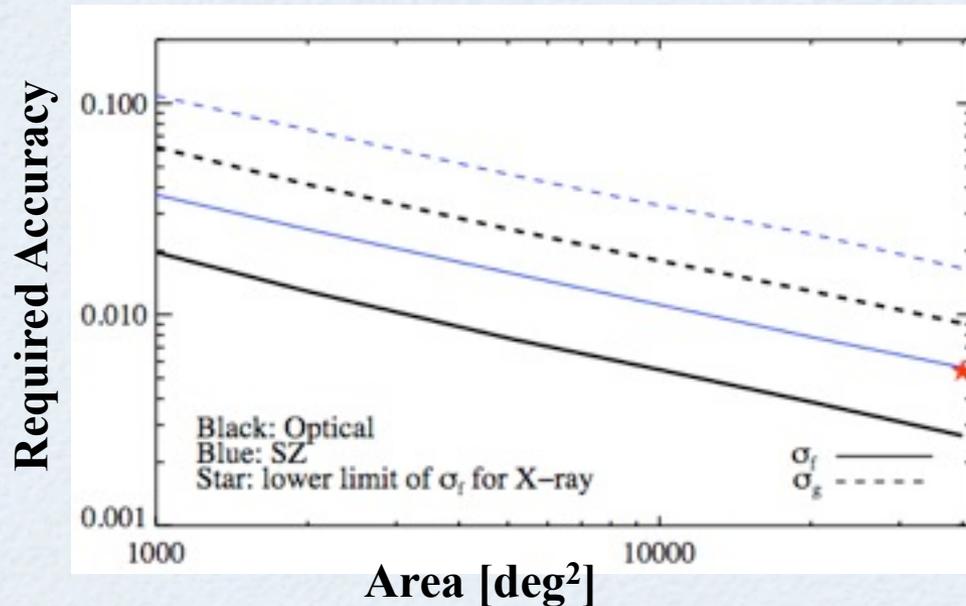
**Top: unknown O-M**  
**Bottom: known O-M**  
**Left: DES assumption**  
**Right: SPT assumption**

- For DES, percent-level accuracy on MF is required.
- The requirement on halo bias is less stringent.

DES assumptions:  $M_{\text{th}} = 10^{13.7} M_{\text{sun}}/h$ ; Scatter = 0.4; Area = 5000 deg<sup>2</sup>

SPT assumptions:  $M_{\text{th}} = 10^{14.1} M_{\text{sun}}/h$ ; Scatter = 0.2; Area = 2000 deg<sup>2</sup><sup>13</sup>

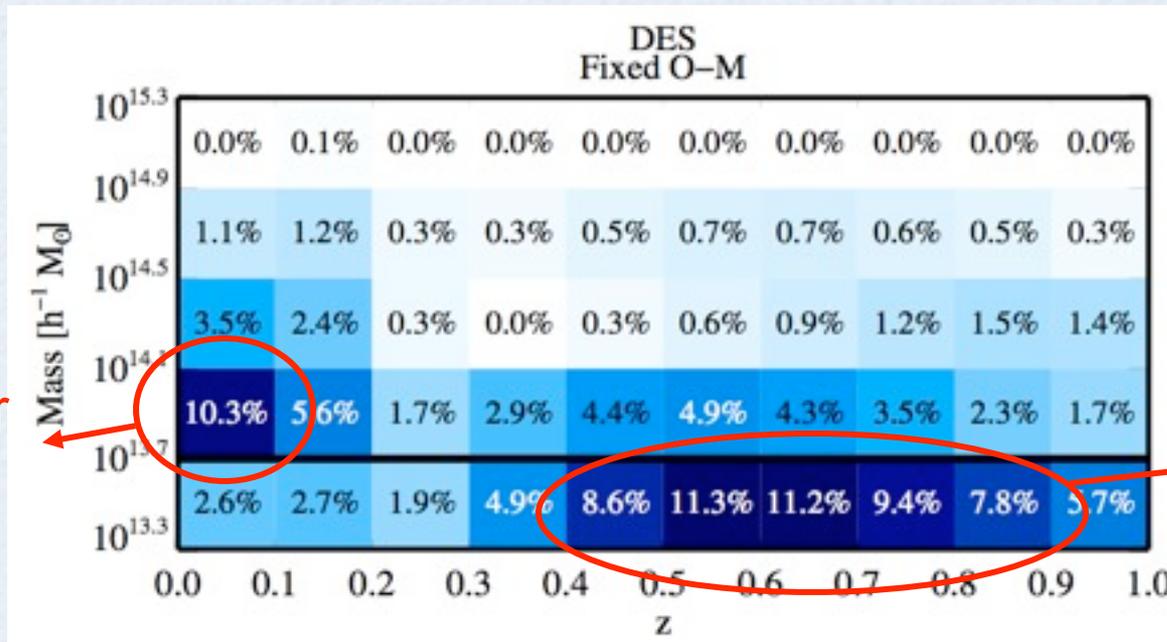
# Effects of Survey Area



Most stringent requirement will come from a full-sky optical survey.

- Future full-sky optical surveys will required sub-percent level accuracy in mass function.
- The required constraints are almost independent of  $z_{\max}$  and assumptions of observable--mass distribution.
- Optical surveys have more stringent requirements than X-ray and SZ surveys.

# Comparing Bins



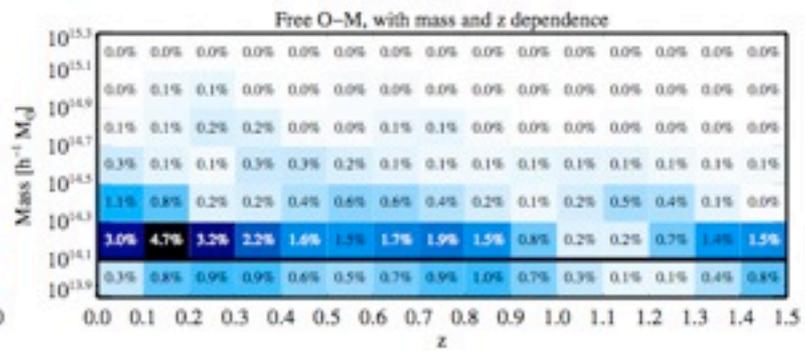
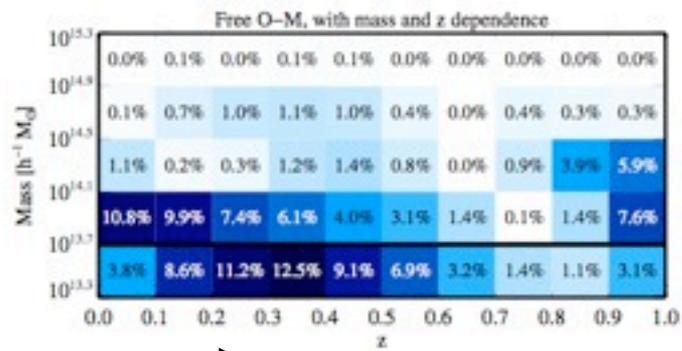
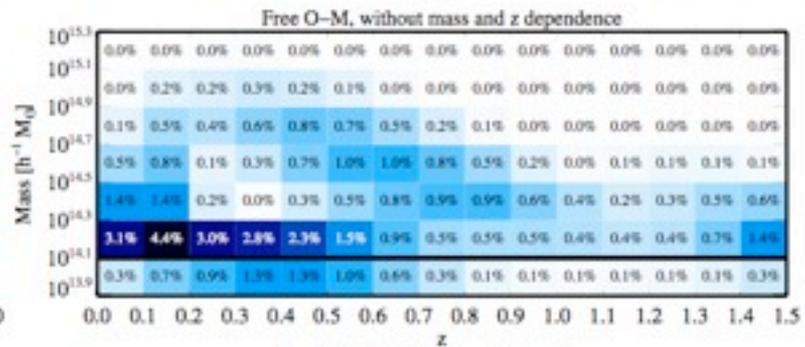
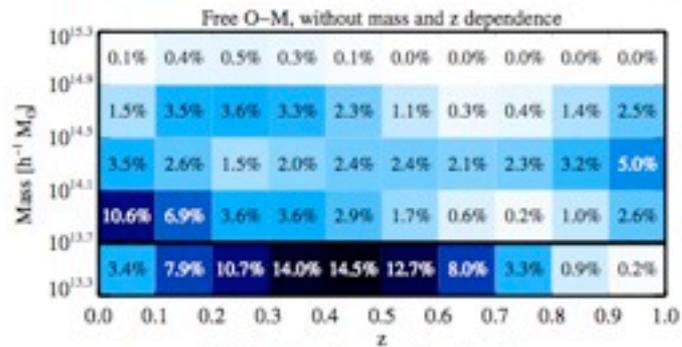
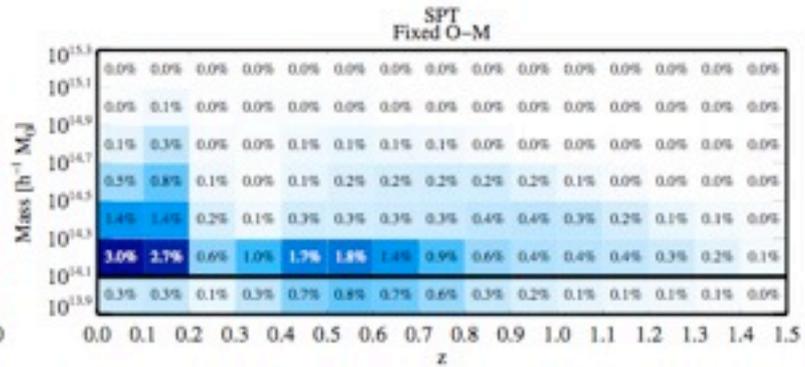
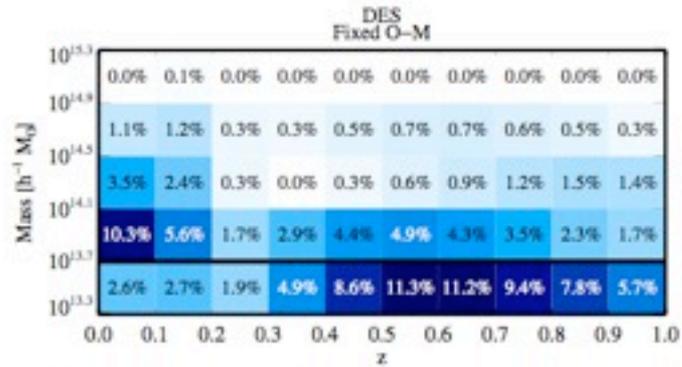
Lowest z:  
longest lever  
arm for dark  
energy  
constraints

Lowest mass:  
greatest  
cluster counts

- We tighten the MF in one bin at a time and calculate the FoM improvement.
- This pattern reflects the CMB prior, cluster counts, and degeneracy between scatter and MF.
- Improving the mass function accuracy in low redshift and low mass will be the most beneficial.

# Comparing Bins

Mass



Z

More general O-M assumption

# Summary

- We studied how follow-ups for future optical galaxy cluster surveys can improve the dark energy constraints.
  - The systematic errors of the follow-up mass tracers need to be controlled at  $\sim 5\%$  to avoid significant degradation in FoM.
  - Optimization can reduce the observational cost by up to an order of magnitude. Less than 200 X-ray or SZ clusters can improve the FoM by 50% in DES-like surveys.
  - ✓ **Note for observers:** Follow-ups over a wide range of mass and redshift are the most effective!
- We studied the impact of theoretical uncertainties in mass function on future surveys.
  - Future optical surveys will require percent-level accuracy in mass function to avoid severe degradation in the FoM.
  - ✓ **Note for simulators:** The low mass and low redshift regimes are the most important to accurately calibrate mass function.