

# Axisymmetric Core-Collapse Supernovae Simulations with CHIMERA



**Bronson Messer**

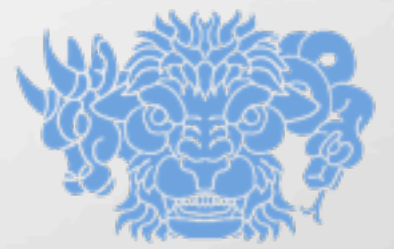
**Oak Ridge Leadership Computing Facility**

**Theoretical Astrophysics Group  
Oak Ridge National Laboratory**

**Department of Physics & Astronomy  
University of Tennessee**

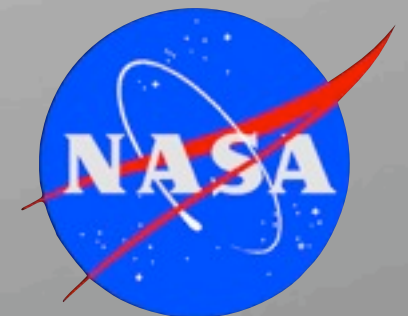


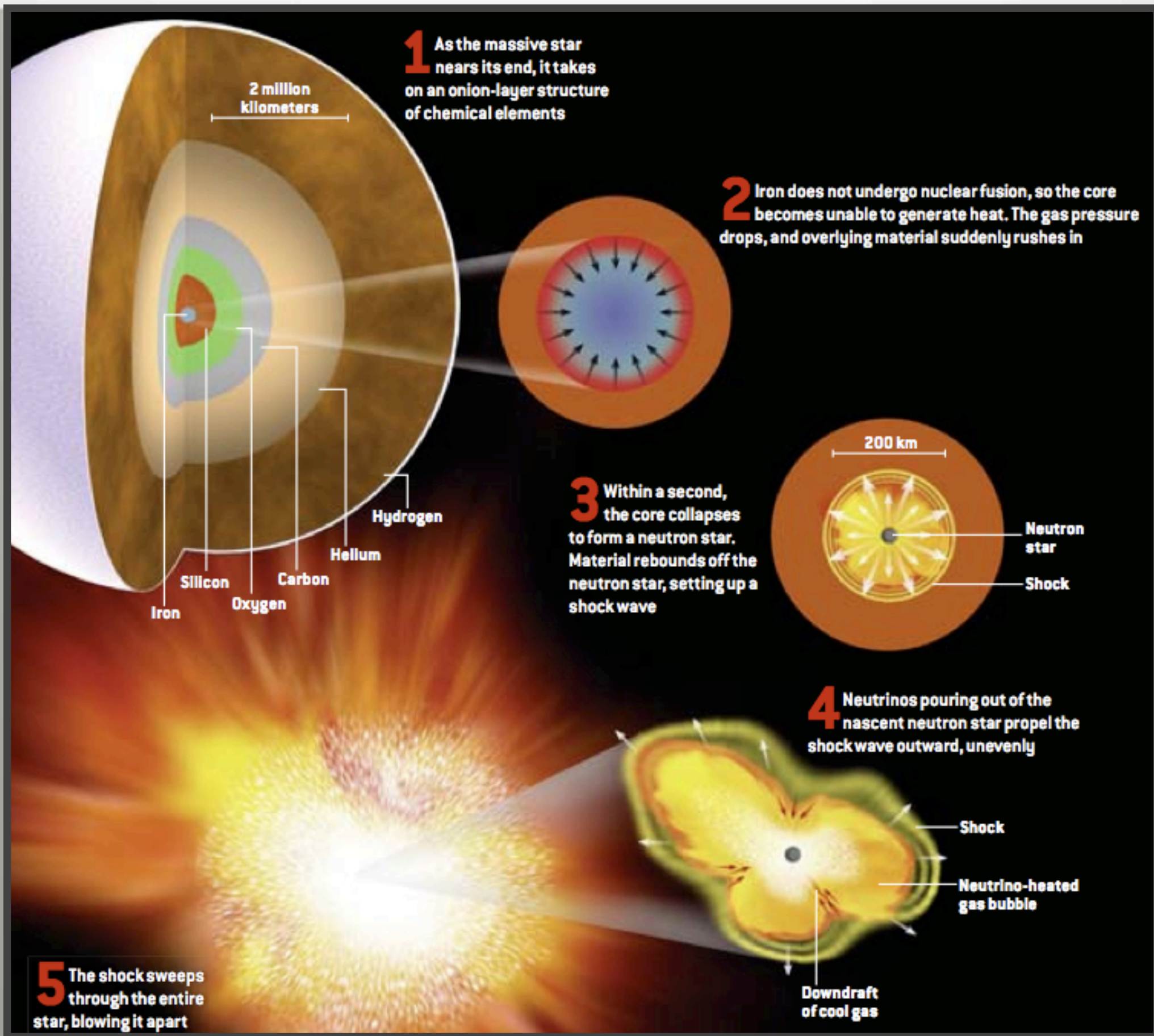
# CHIMERA Collaboration



- Steve Bruenn, Pedro Marronetti (Florida Atlantic University)
- John Blondin, Chris Mauney (NC State University)
- Eirik Endeve, Raph Hix, Austin Harris, Eric Lentz, Bronson Messer, Anthony Mezzacappa, Konstantin Yakunin (ORNL/UTK)
- Former Team Members
  - Reuben Budjiara, Austin Chertkow, Ted Lee

The research and activities described in this presentation were performed using the resources of the Oak Ridge Leadership Computing Facility at Oak Ridge National Laboratory, which is supported by the Office of Science of the U.S. Department of Energy under Contract No. DE-AC0500OR22725.





Hillebrandt, Janka, & Müller 2006 (Sci Am)

# Neutrino trapping

$$\lambda_\nu = \frac{1}{\sigma_A n_A}$$

$$n_A = \frac{\rho}{Am_u}$$

During stellar core collapse, the neutrino opacity is dominated by coherent scattering on nuclei.

$$\sigma_A = \frac{1}{16} \sigma_0 \left( \frac{E_\nu}{m_e c^2} \right)^2 A^2 \left[ 1 - \frac{Z}{A} + (4 \sin^2 \theta_w - 1) \frac{Z}{A} \right]^2$$

Freedman, *PRD* **9**, 1389 (1974)

$$\lambda_\nu \approx 100 \text{ km} \left( \frac{\rho}{3 \times 10^{10} \text{ g cm}^{-3}} \right)^{-5/3} \left( \frac{A}{56} \right)^{-1} \left( \frac{Y_e}{26/56} \right)^{2/3} \propto \rho^{-5/3}$$

Arnett, *ApJ* **218**, 815 (1977)

$$R_{\text{core}} \approx \left( \frac{3M_{\text{core}}}{4\pi\rho} \right)^{1/3} \approx 270 \text{ km} \left( \frac{\rho}{3 \times 10^{10} \text{ g cm}^{-3}} \right)^{-1/3} \left( \frac{Y_e}{26/56} \right)^{2/3} \propto \rho^{-1/3}$$

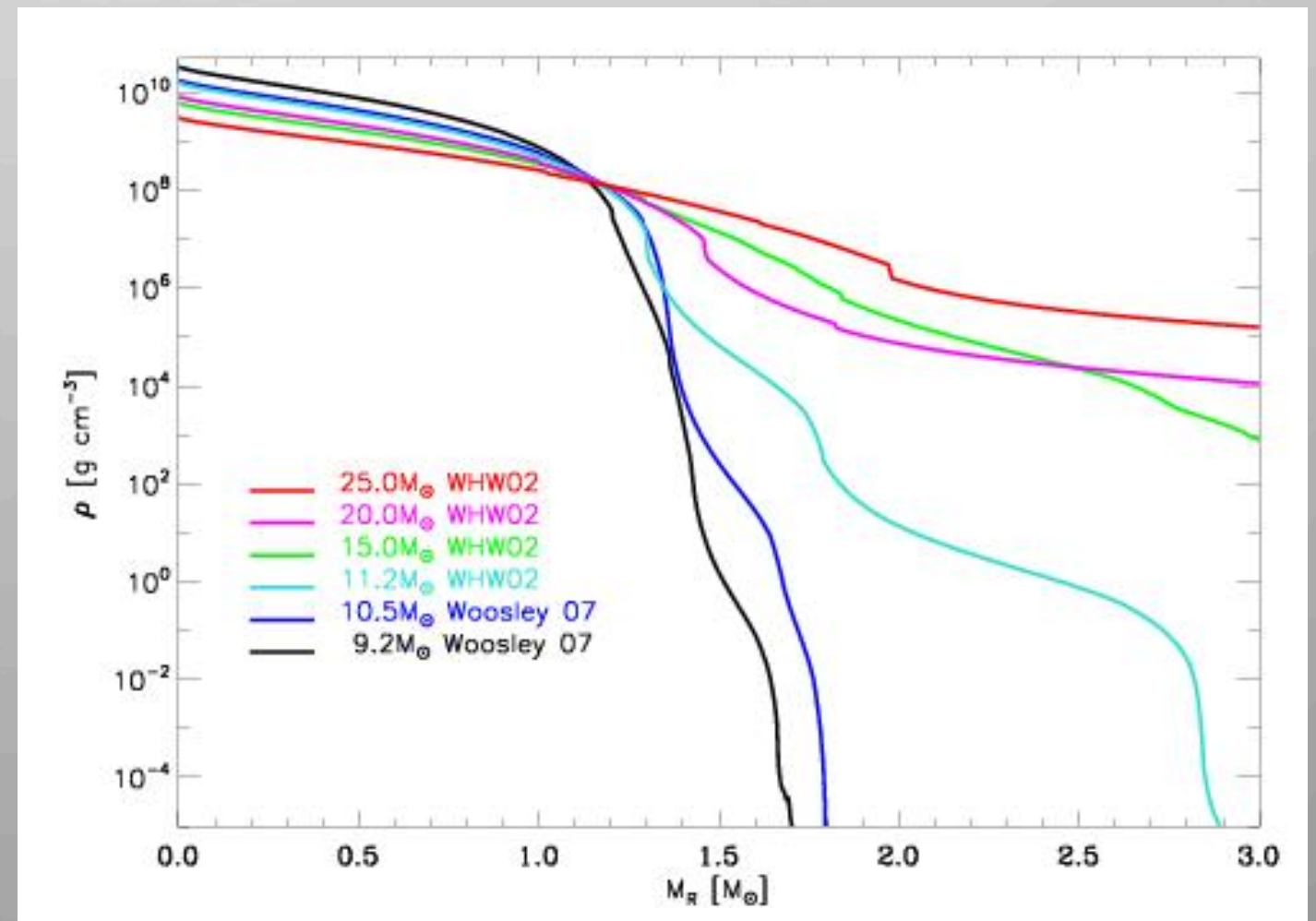
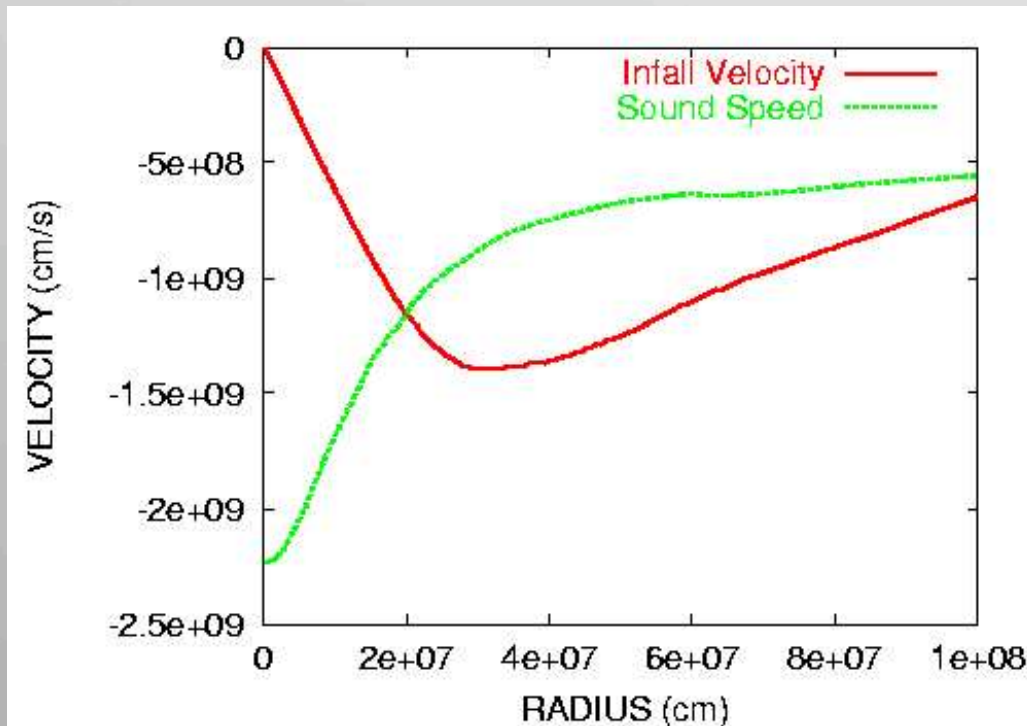
Electron-neutrino mean free path decreases much more rapidly with density than core size, and the neutrinos become trapped in the core.

Degenerate electron-neutrino Fermi sea develops...

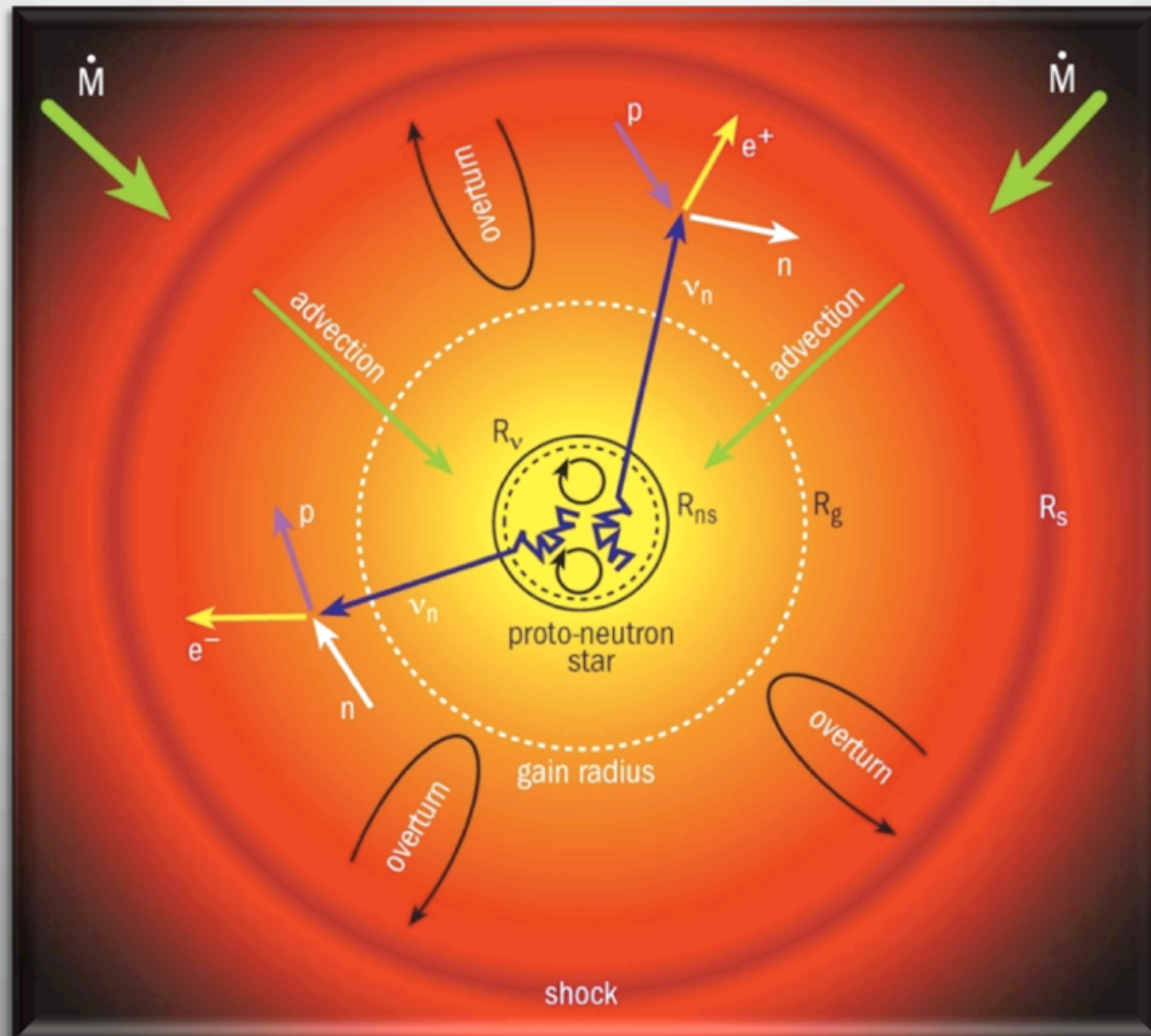


# Homologous collapse

- homologous collapse --> differences in core structure for different progenitors only appear after bounce



# Post-bounce profile



Hillebrandt, Janka, & Müller 2006 (Sci Am)

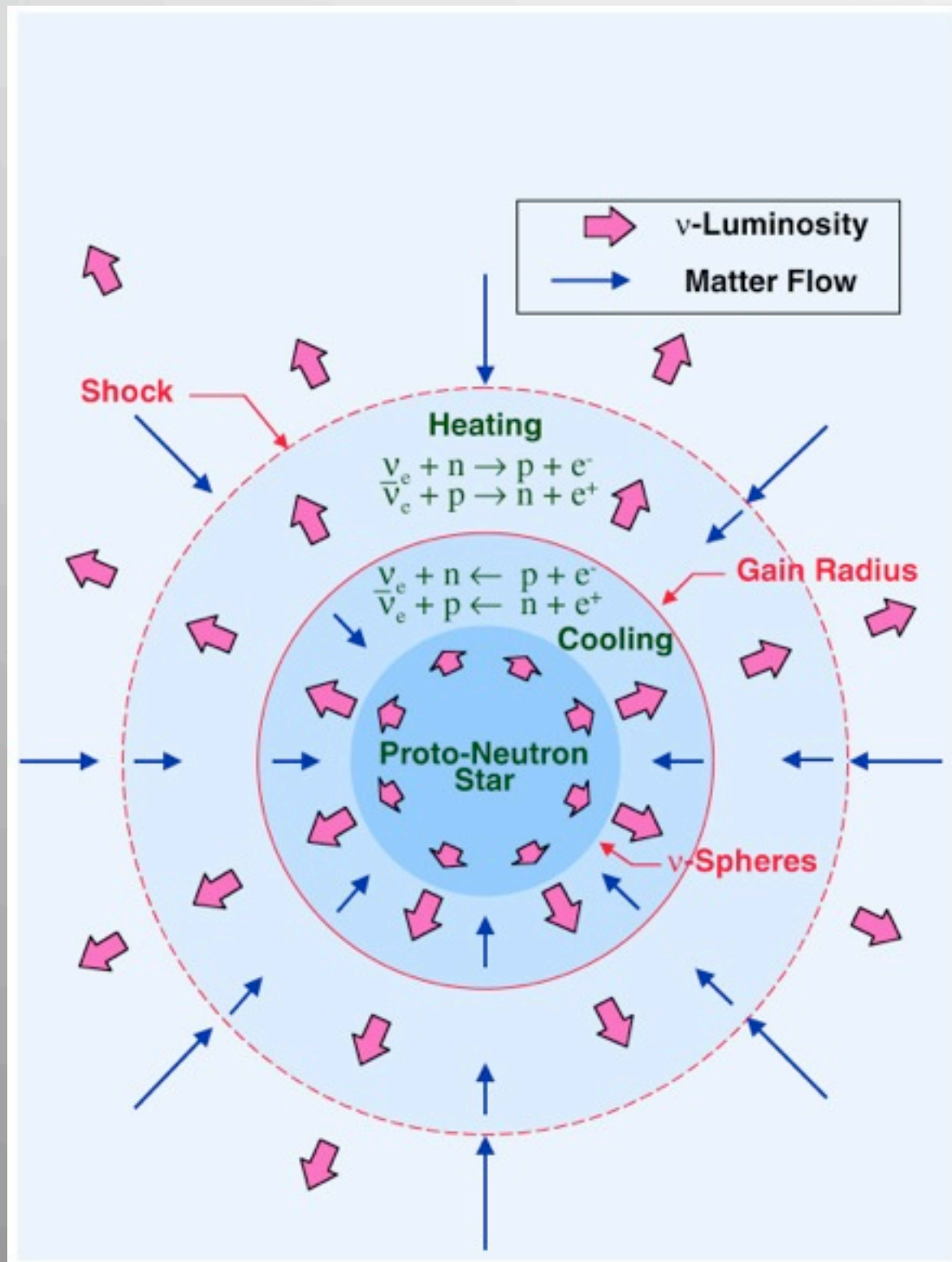


# How is the supernova shock revived?

## Known, Potentially Important Ingredients

- Gravity
- Neutrino Heating
- Convection
- **Shock Instability (SASI)**
- Nuclear Burning
- Rotation
- Magnetic Fields

*Need 3D models with all of the above, treated with sufficient realism.*

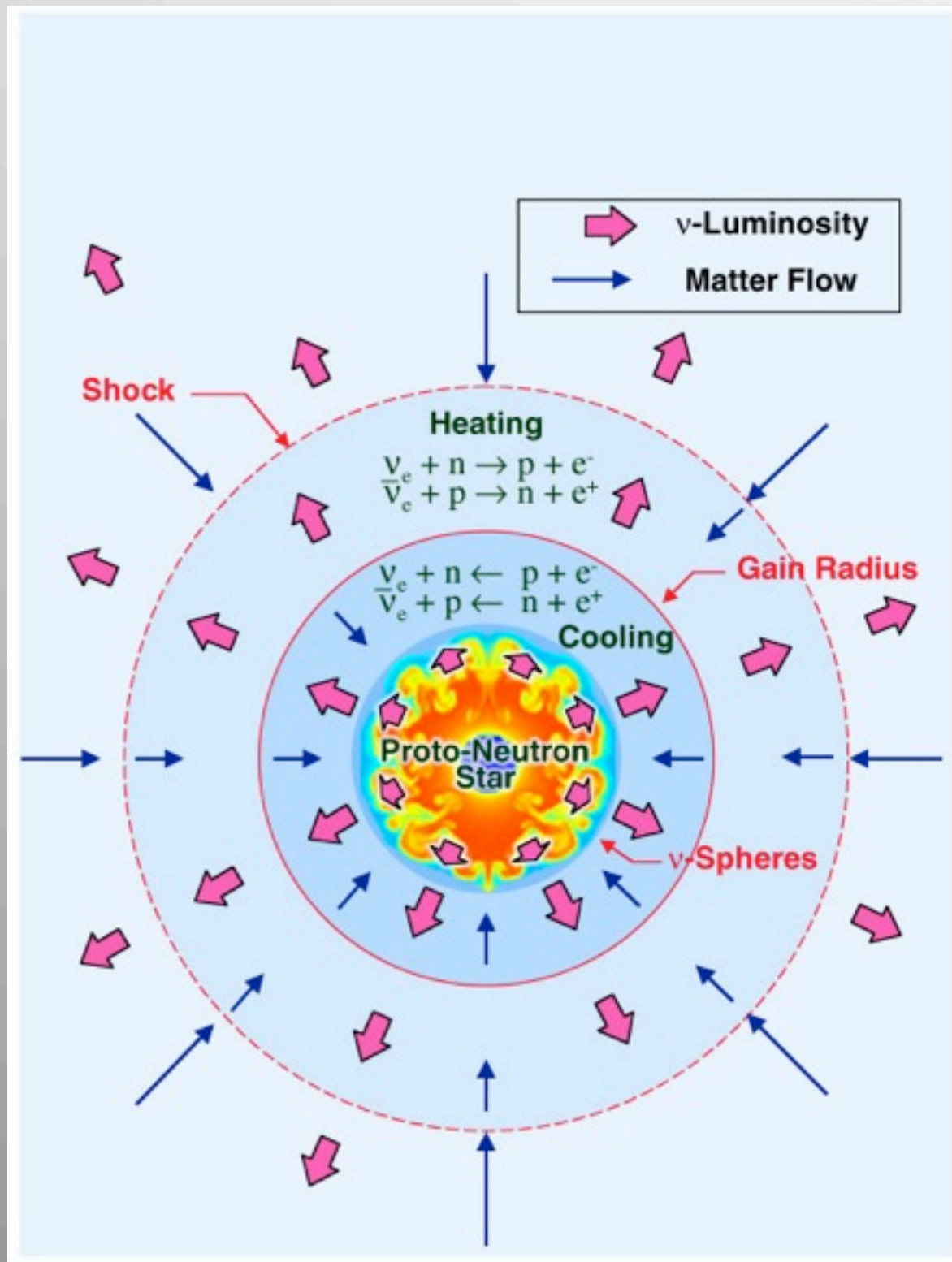


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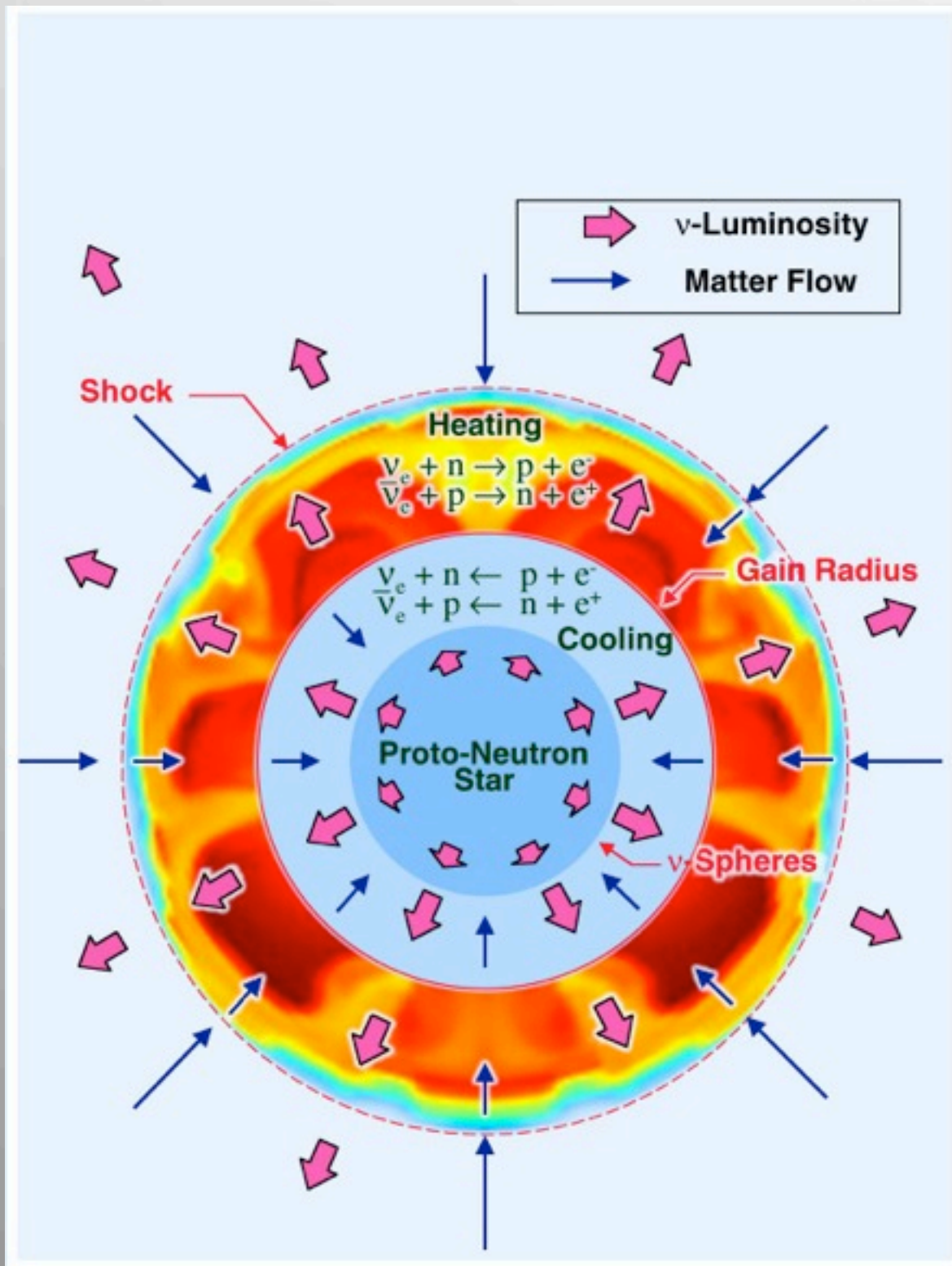


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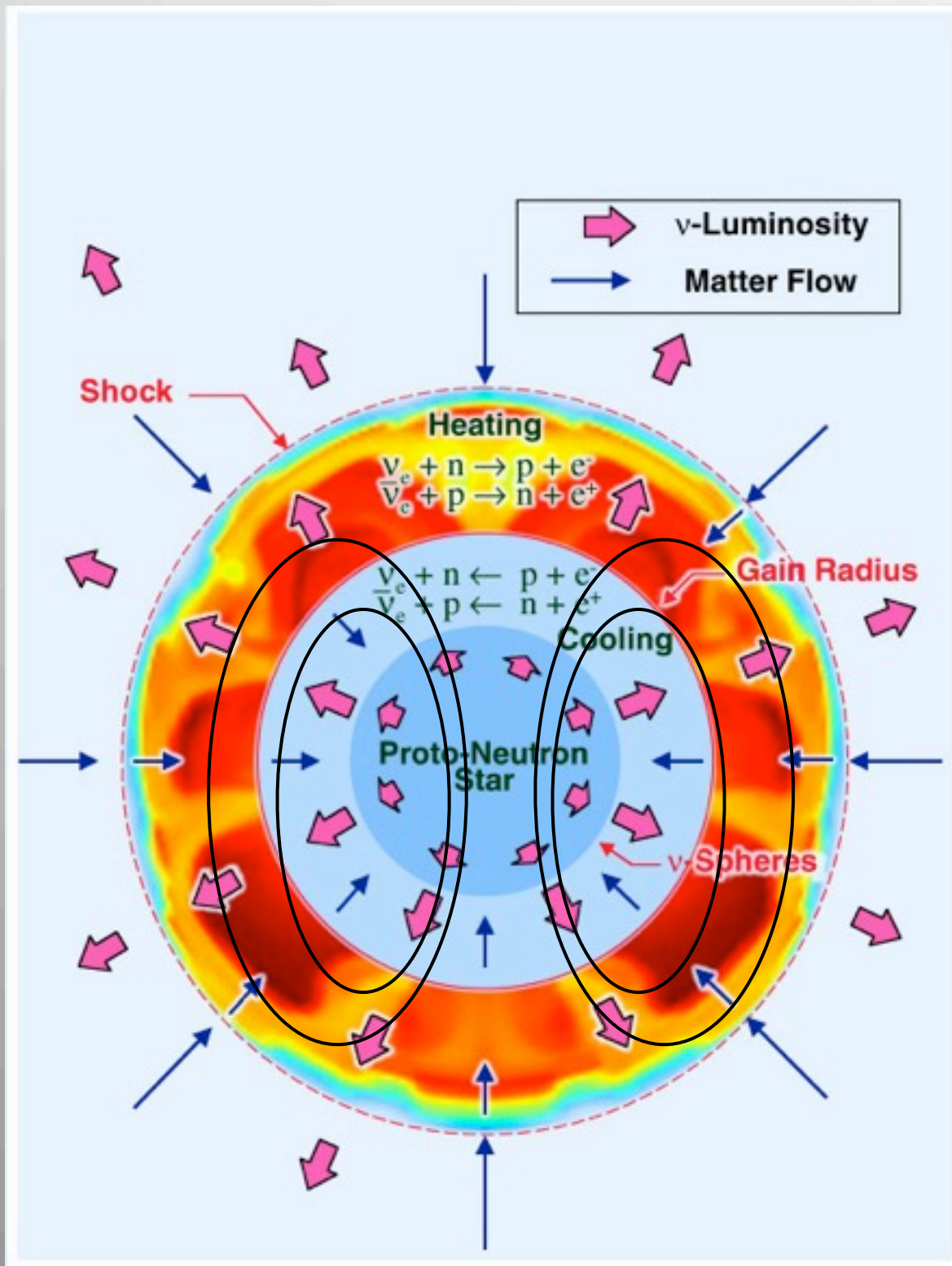


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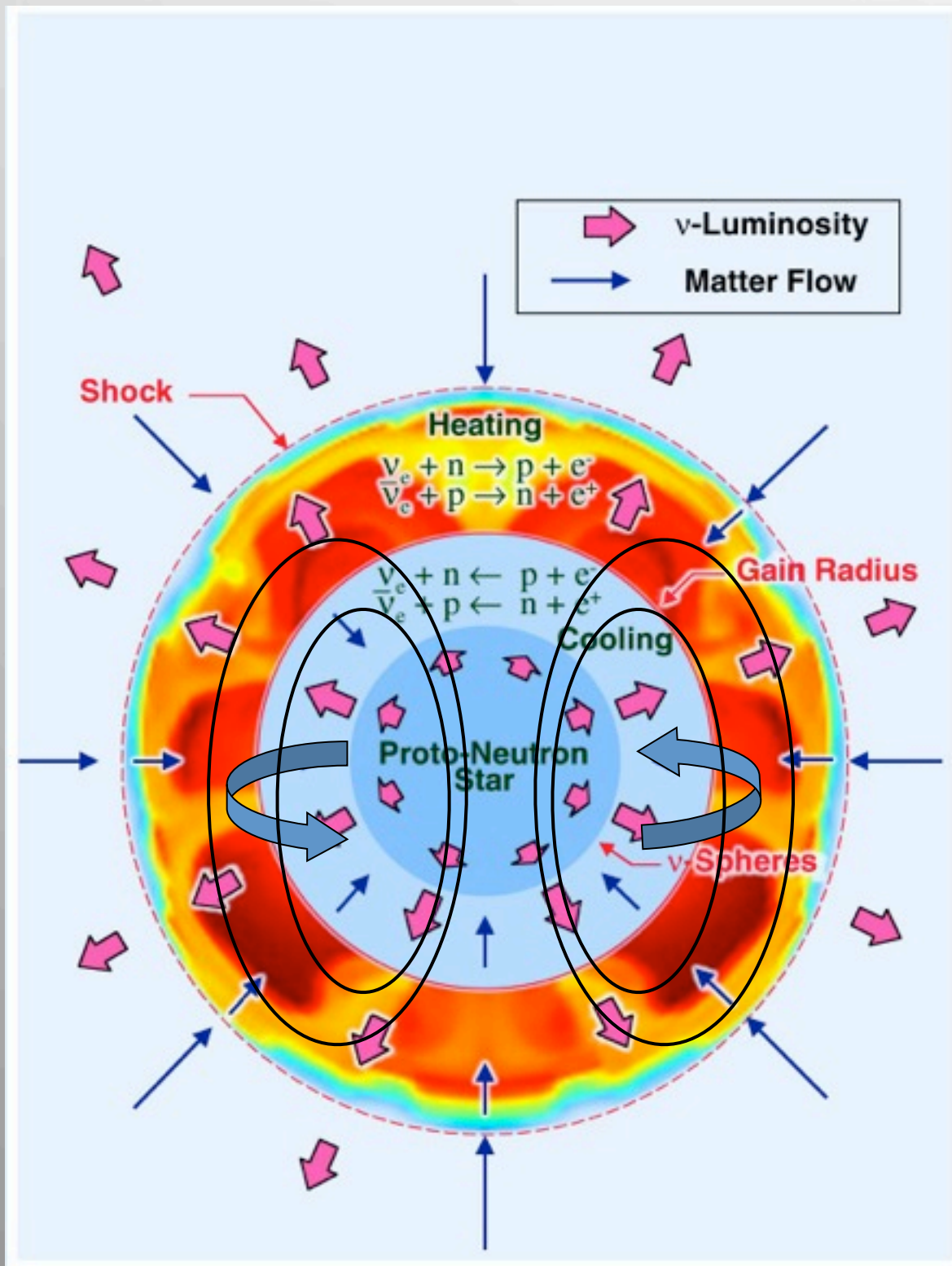


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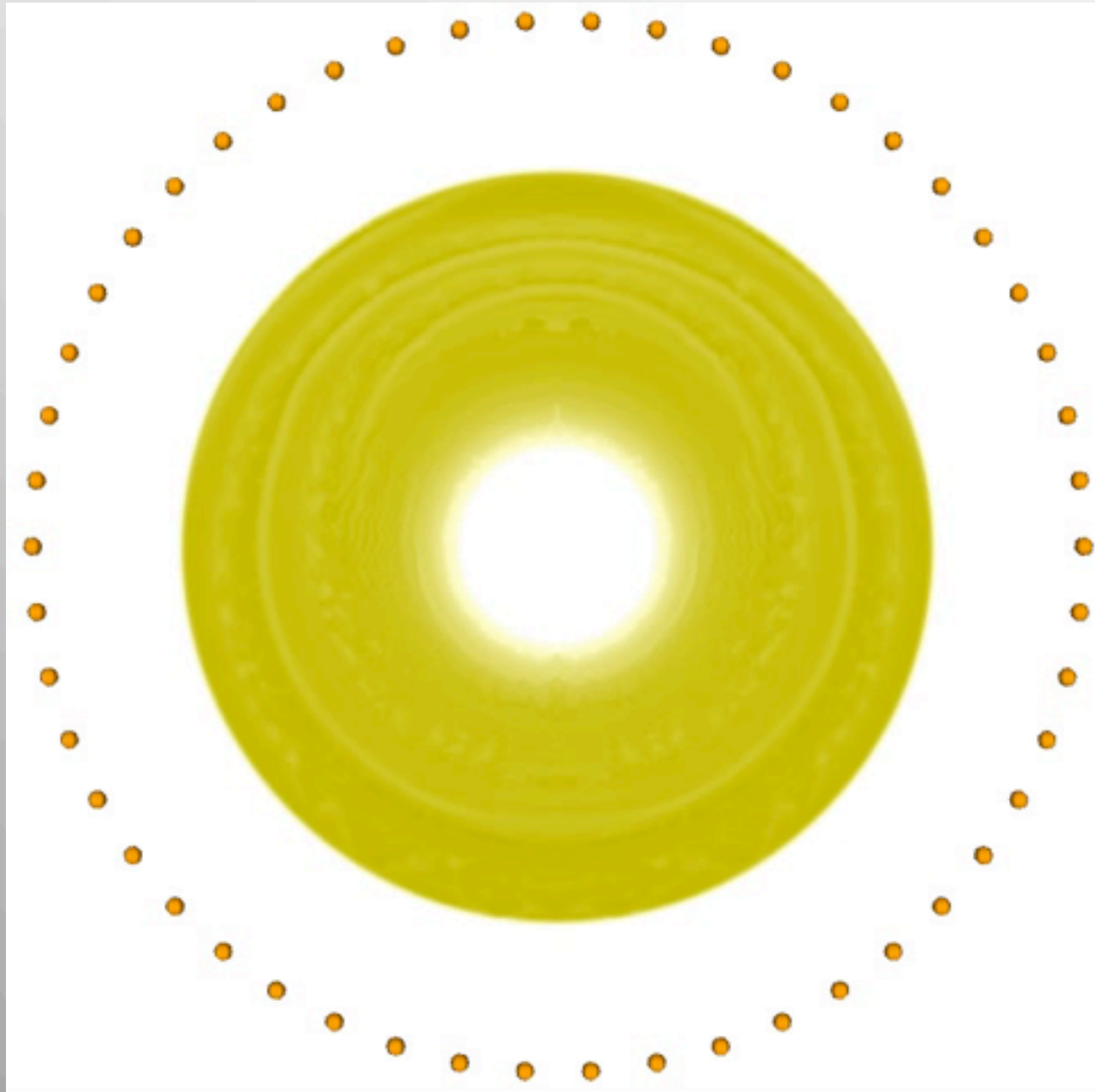
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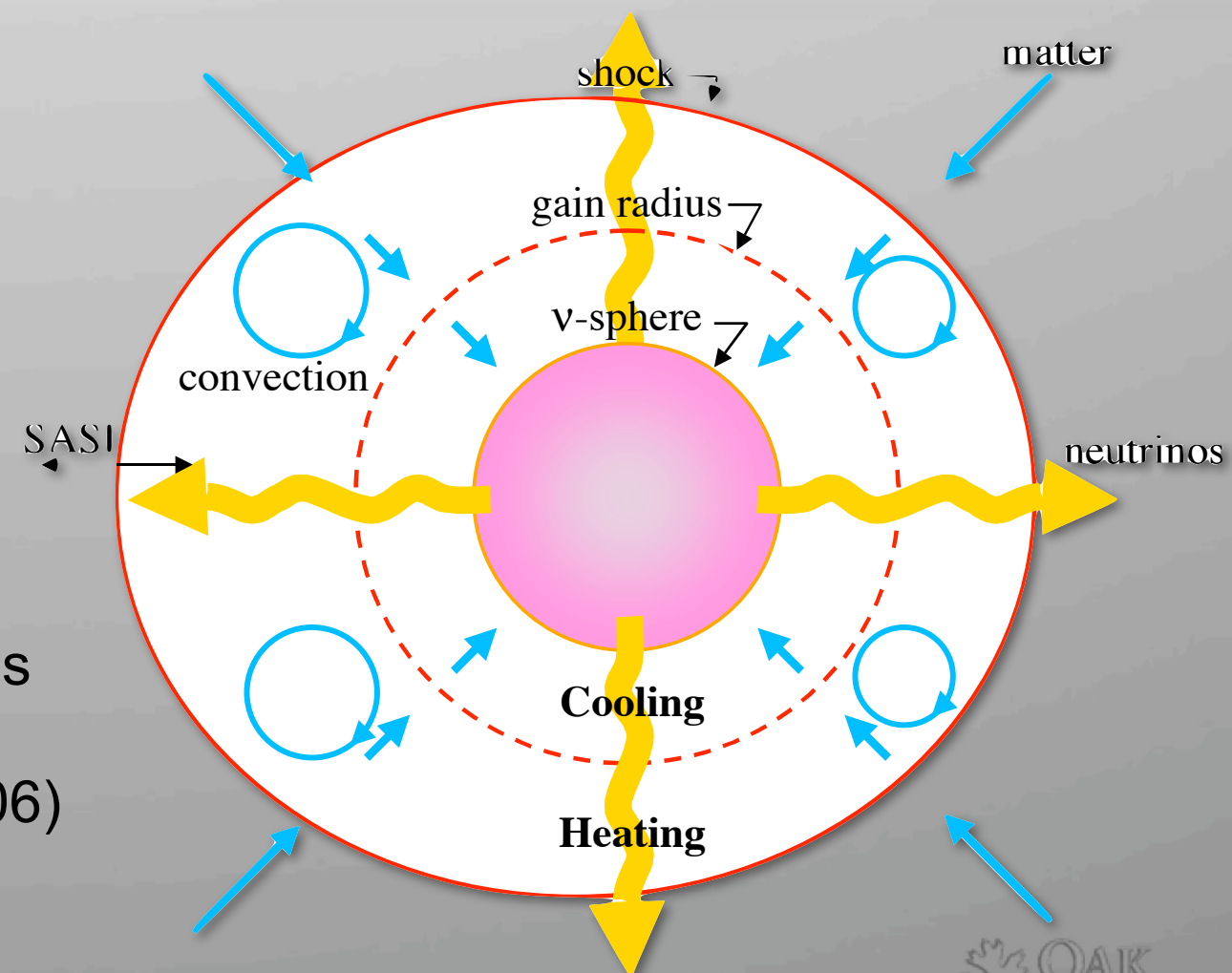
# Stationary Accretion Shock Instability (SASI)



*Shock wave unstable to non-radial perturbations.*

Blondin, Mezzacappa, & DeMarino, *Ap.J.* **584**, 971 (2003)

- Decreases advection velocity in gain region.
- Increases time in the gain region.
- Generates convection.



SASI has *axisymmetric and nonaxisymmetric* modes that are both linearly unstable!

- Blondin and Mezzacappa, *Ap.J.* **642**, 401 (2006)
- Blondin and Shaw, *Ap.J.* **656**, 366 (2007)



# CHIMERA

- “Ray-by-ray-Plus” MGFLD Neutrino Transport
  - $O(v/c)$ , GR time dilation and redshift, GR aberration
- 2D PPM Hydrodynamics
  - GR time dilation, effective gravitational potential
  - adaptive radial grid
- Lattimer-Swesty EOS + low-density BCK EOS
  - $K=220$  MeV
  - low-density EOS “bridges” LS to network
- Nuclear (Alpha) Network
  - 14 alpha nuclei between helium and zinc
- 2D Effective Gravitational Potential
  - Marek et al. A&A, 445, 273 (2006)
- Neutrino Emissivities/Opacities
  - “Standard” + Elastic Scattering on Nucleons + Nucleon–Nucleon Bremsstrahlung



# Important neutrino emissivities/opacities

## “Standard” Emissivities/Opacities

Bruenn, *Ap.J. Suppl.* (1985)

- Nucleons in nucleus independent.
- No energy exchange in nucleonic scattering.

$$e^- + p, A \leftrightarrow \nu_e + n, A'$$

Langanke et al. *PRL*, **90**, 241102 (2003)

- Include correlations between nucleons in nuclei.

$$e^+ + e^- \leftrightarrow \nu_{e,\mu,\tau} + \bar{\nu}_{e,\mu,\tau}$$

$$\star \nu + n, p, A \rightarrow \nu + n, p, A$$

Reddy, Prakash, and Lattimer, *PRD*, **58**, 013009 (1998)  
Burrows and Sawyer, *PRC*, **59**, 510 (1999)

- (Small) **Energy is exchanged due to nucleon recoil.**
- Many such scatterings.

$$\nu + e^-, e^+ \rightarrow \nu + e^-, e^+$$

$$\star N + N \leftrightarrow N + N + \nu_{e,\mu,\tau} + \bar{\nu}_{e,\mu,\tau}$$

Hannestad and Raffelt, *Ap.J.* **507**, 339 (1998)  
Hanhart, Phillips, and Reddy, *Phys. Lett. B*, **499**, 9 (2001)

- **Additional source of neutrino-antineutrino pairs.**

$$\nu_e + \bar{\nu}_e \leftrightarrow \nu_{\mu,\tau} + \bar{\nu}_{\mu,\tau}$$

Janka et al. *PRL*, **76**, 2621 (1996)

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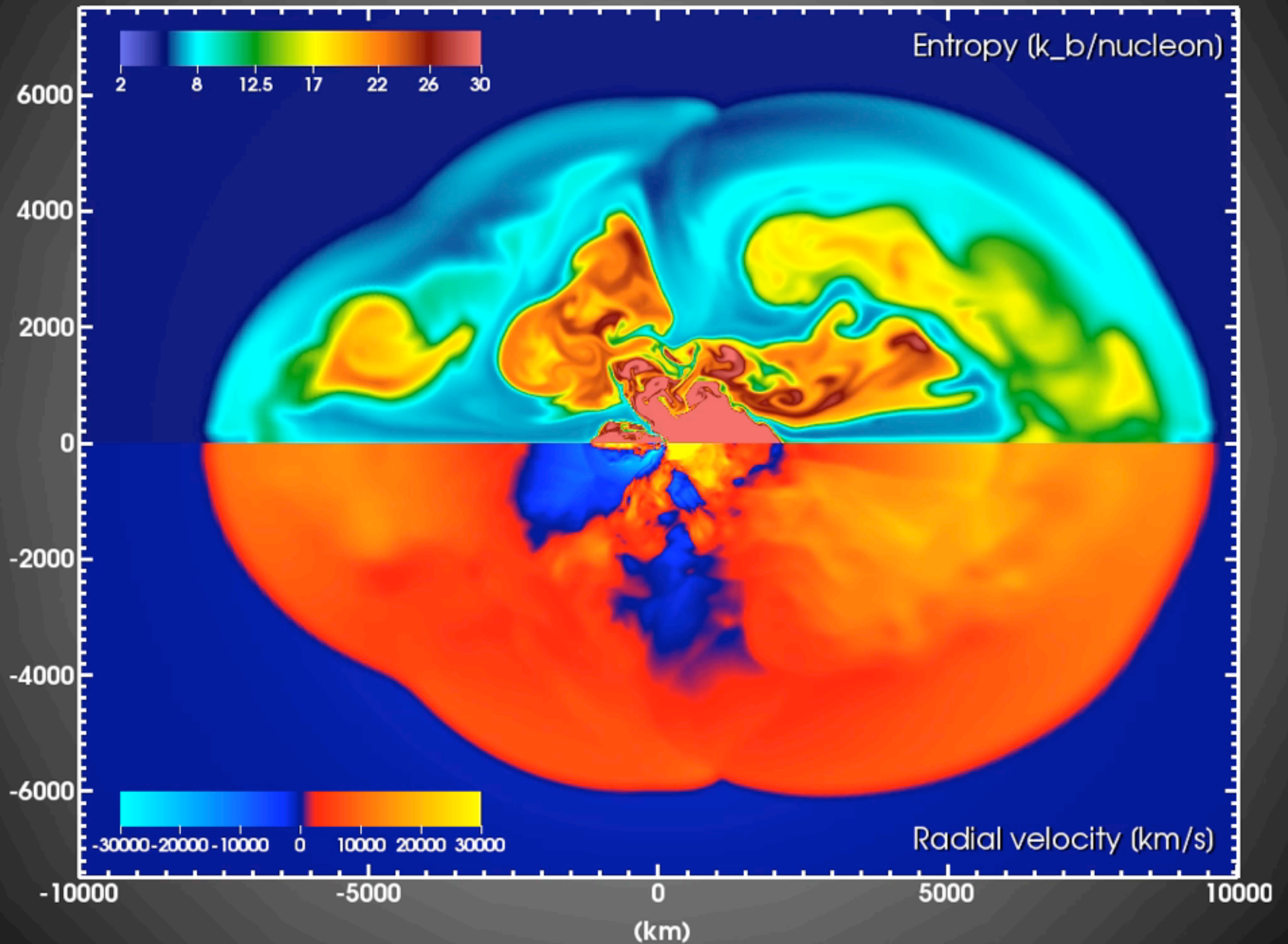
Buras et al. *Ap.J.*, **587**, 320 (2003)

Bruenn et al., *J. Phys. Conf. Ser.*, **46**, 393 (2006)  
Mezzacappa et al., *AIP Conf. Proc.*, **924**, 234 (2007)  
Messer et al., *J. Phys. Conf. Ser.*, **78**, 012049 (2007)

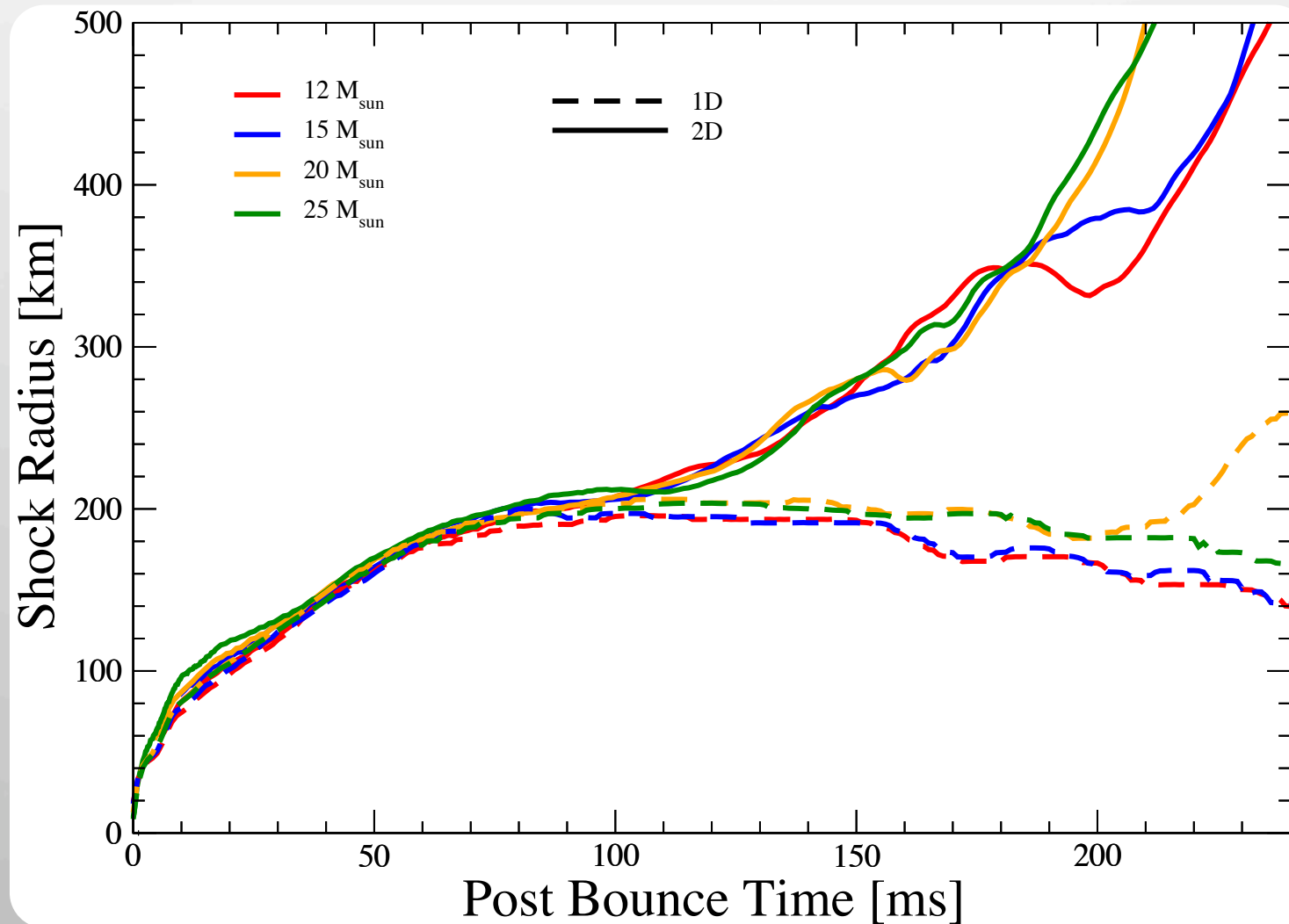


Chimera model: B12-WH07

Time = 800 ms



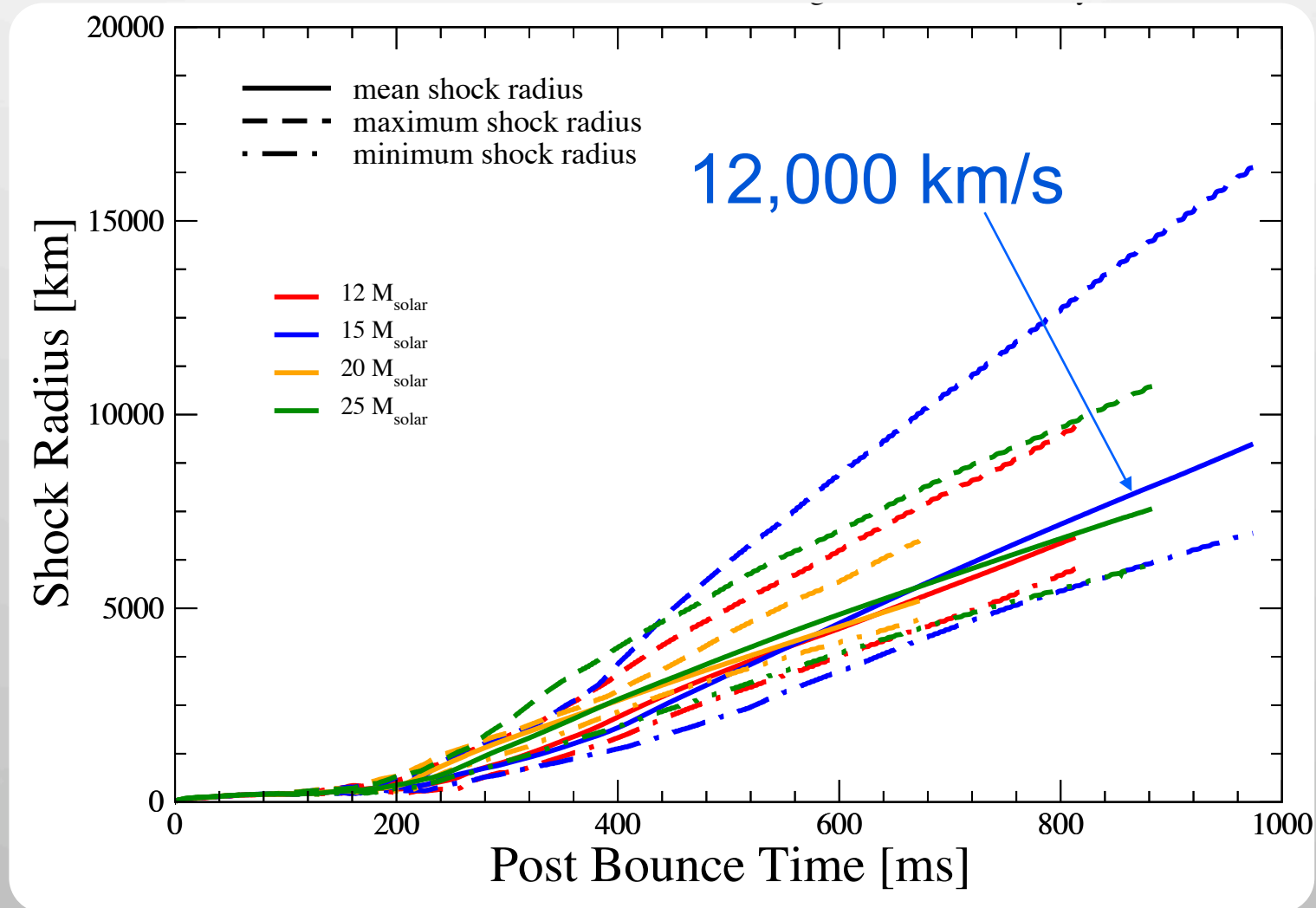
# The early phase



- For the first ~100 ms after bounce, the supernova shock is essentially spherical, with 1D models identical to 2D models.
- Once the Standing Accretion Shock Instability (SASI) and neutrino-driven convection begin, the shock deforms and gradually progresses outward in radius.
- Neutrino-driven convection precedes the development of the SASI at low mass (12  $M_{\odot}$ ) and trails the development of the SASI at high mass (25  $M_{\odot}$ ).
- One notable feature is the considerable delay in launching an explosion.  
(cf. (Herant et al. 1994): <100ms)



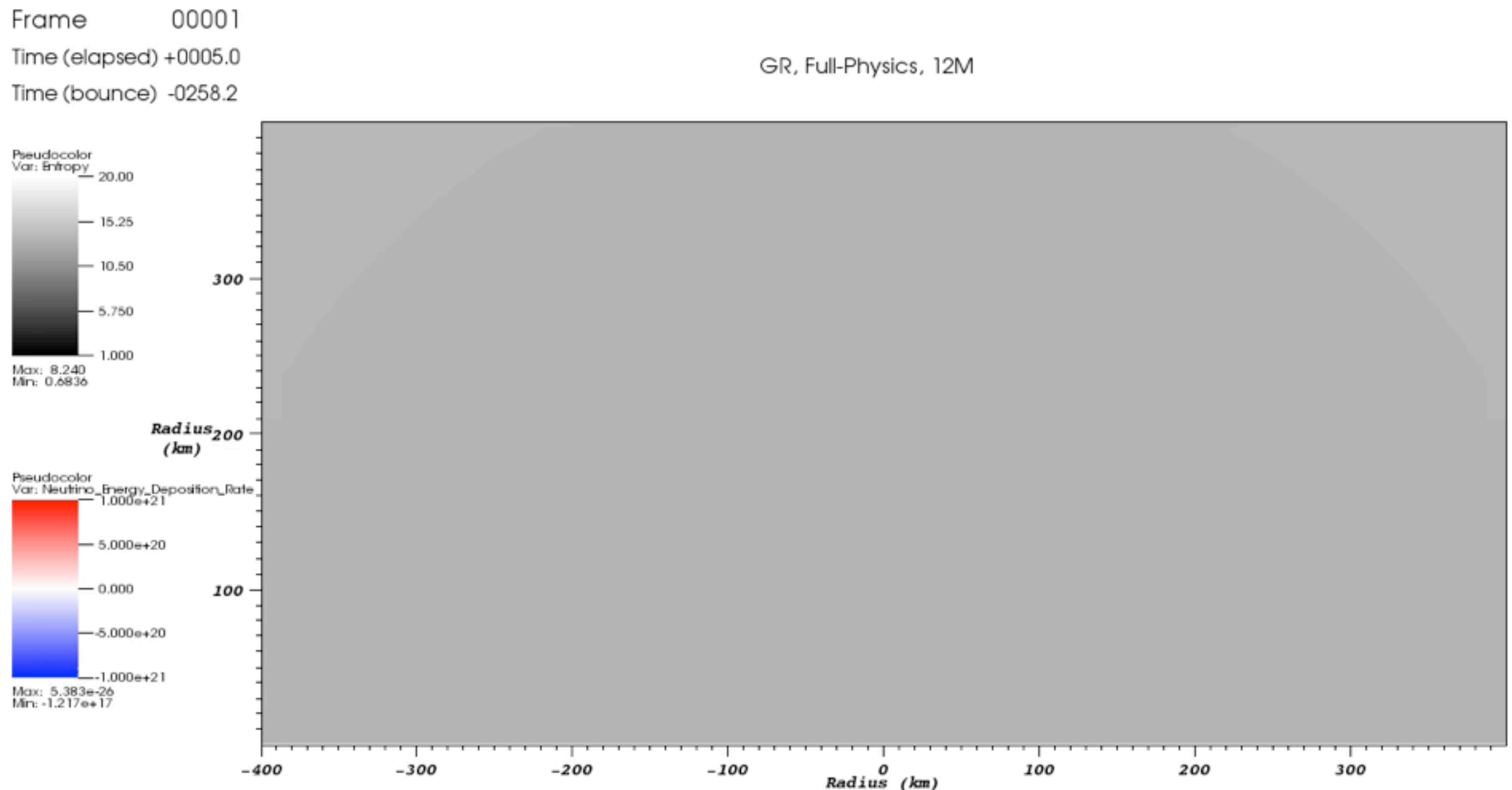
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# Working neutrinos

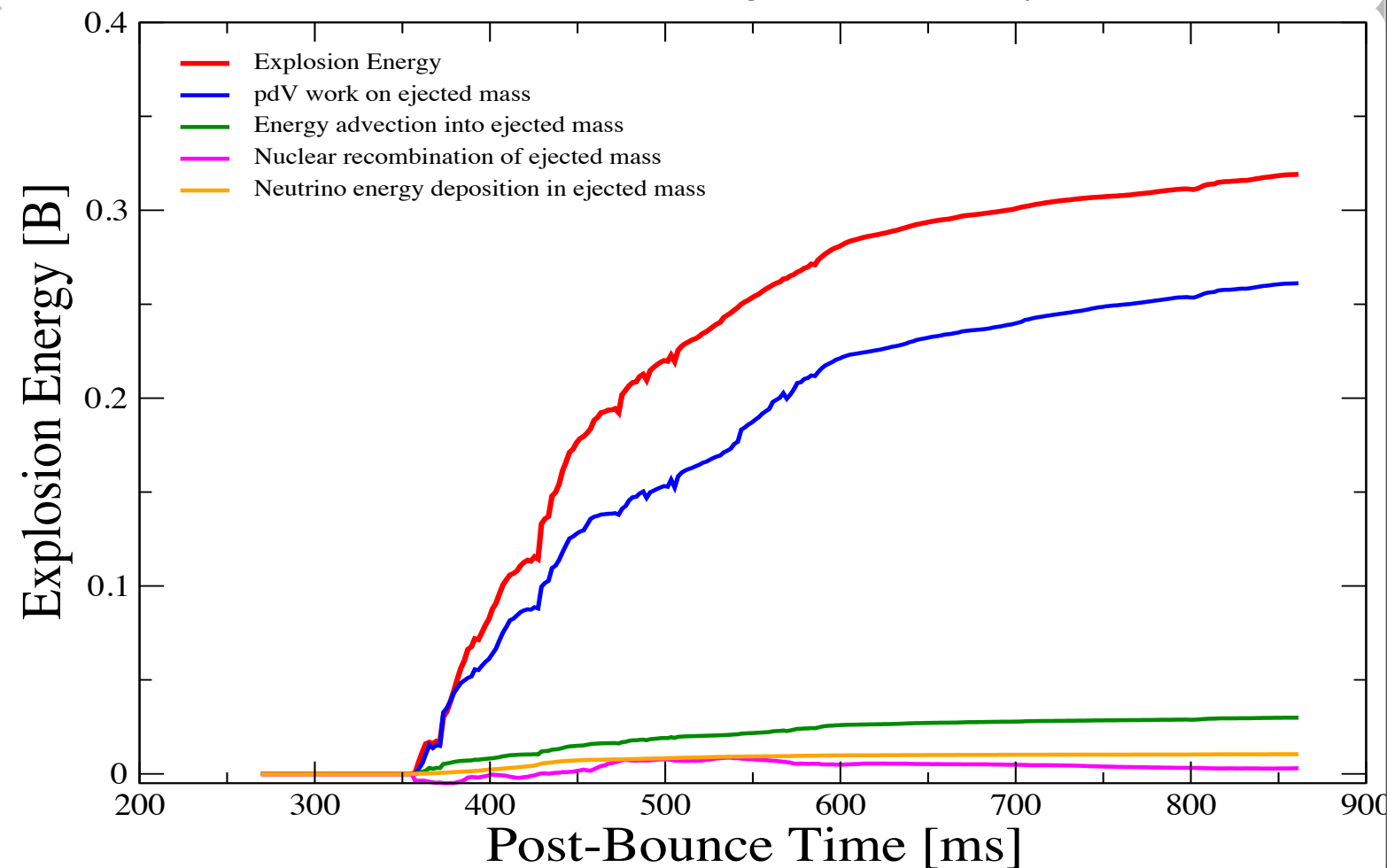
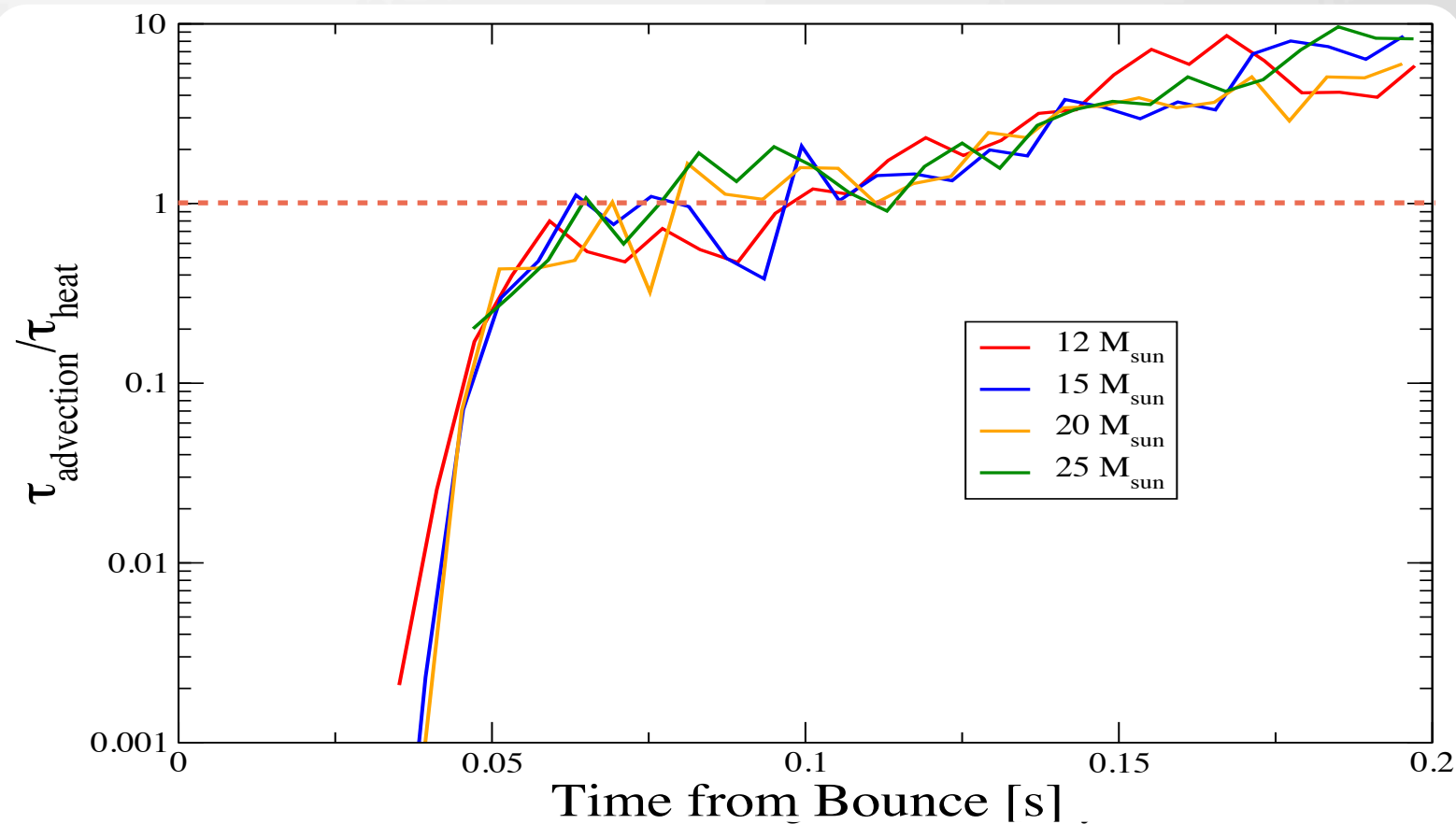
- The initially spherical gain surface between the cooling and heating regions begins to distort ~70 ms after bounce.
- Beginning at ~120 ms, the heating region is characterized by low-entropy downflows and high-entropy upflows, with the strongest heating at the bases of the impinging downflows.





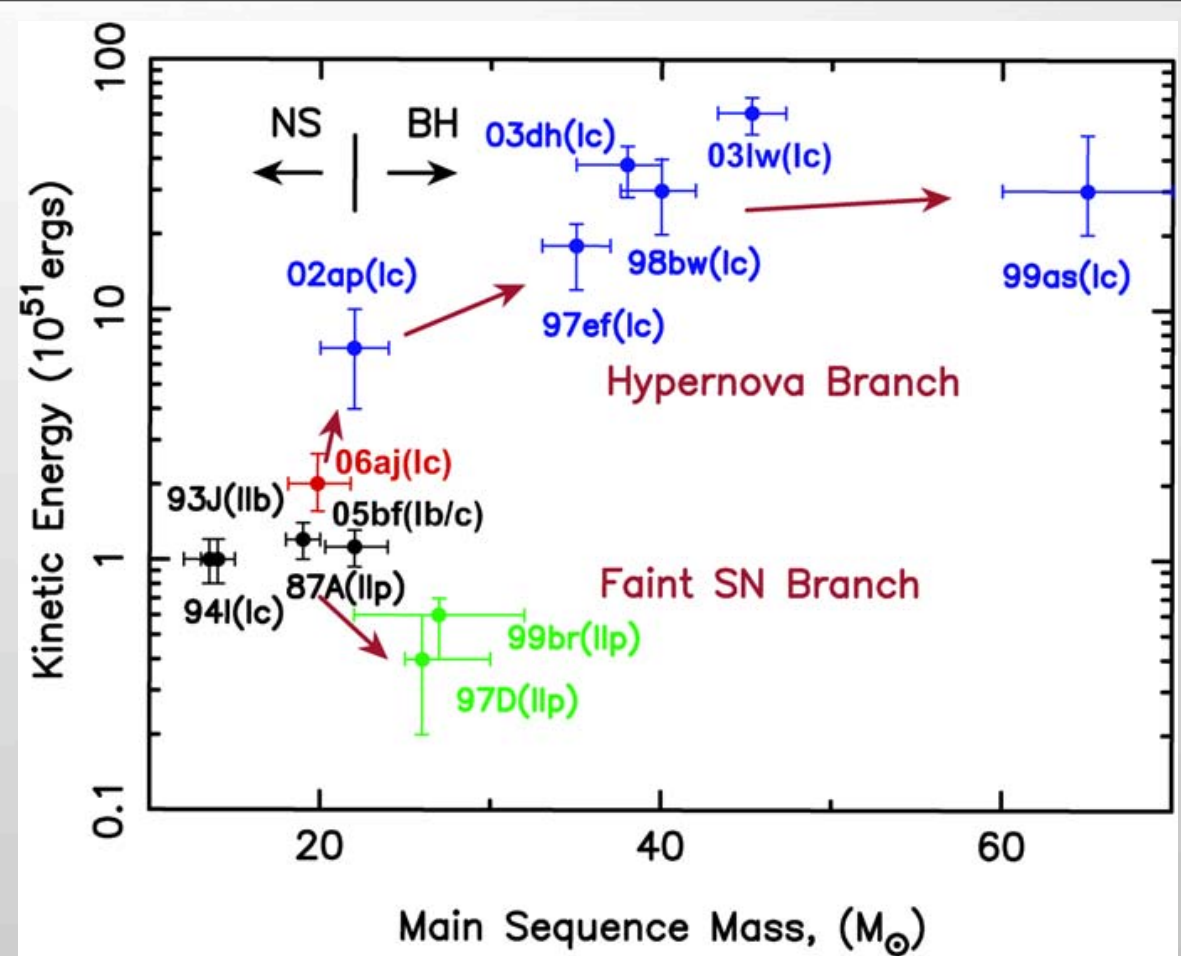
# How to make an explosion

- SASI gradually pushes the shock outward, increasing the size of the heating region until heating timescale ( $\tau_{\text{heating}}$ ) is smaller than advection timescale ( $\tau_{\text{advection}}$ ).
- Much of the explosion energy comes from the neutrino heating region, below the ejecta, in the form of PdV work and advected internal energy.

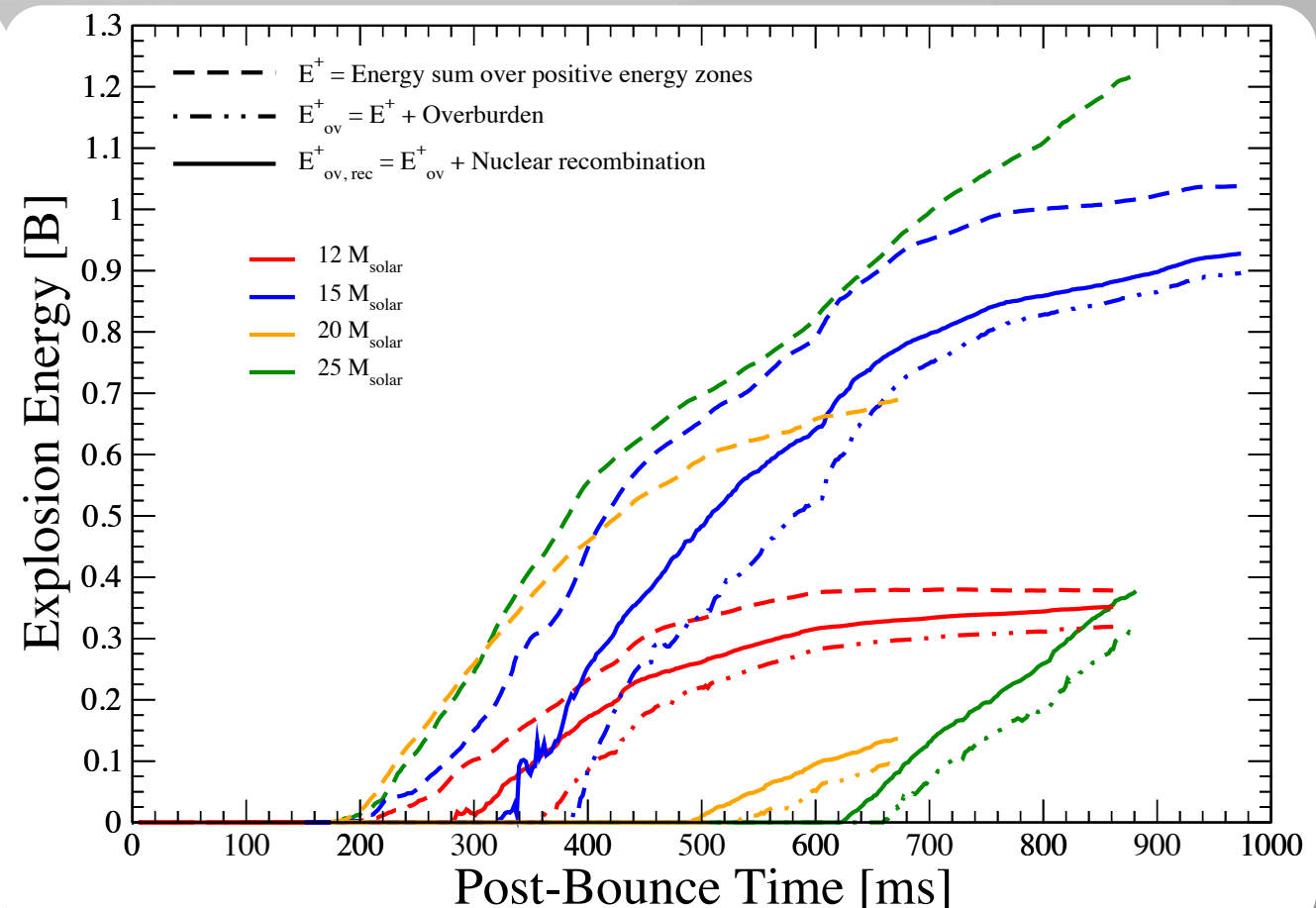
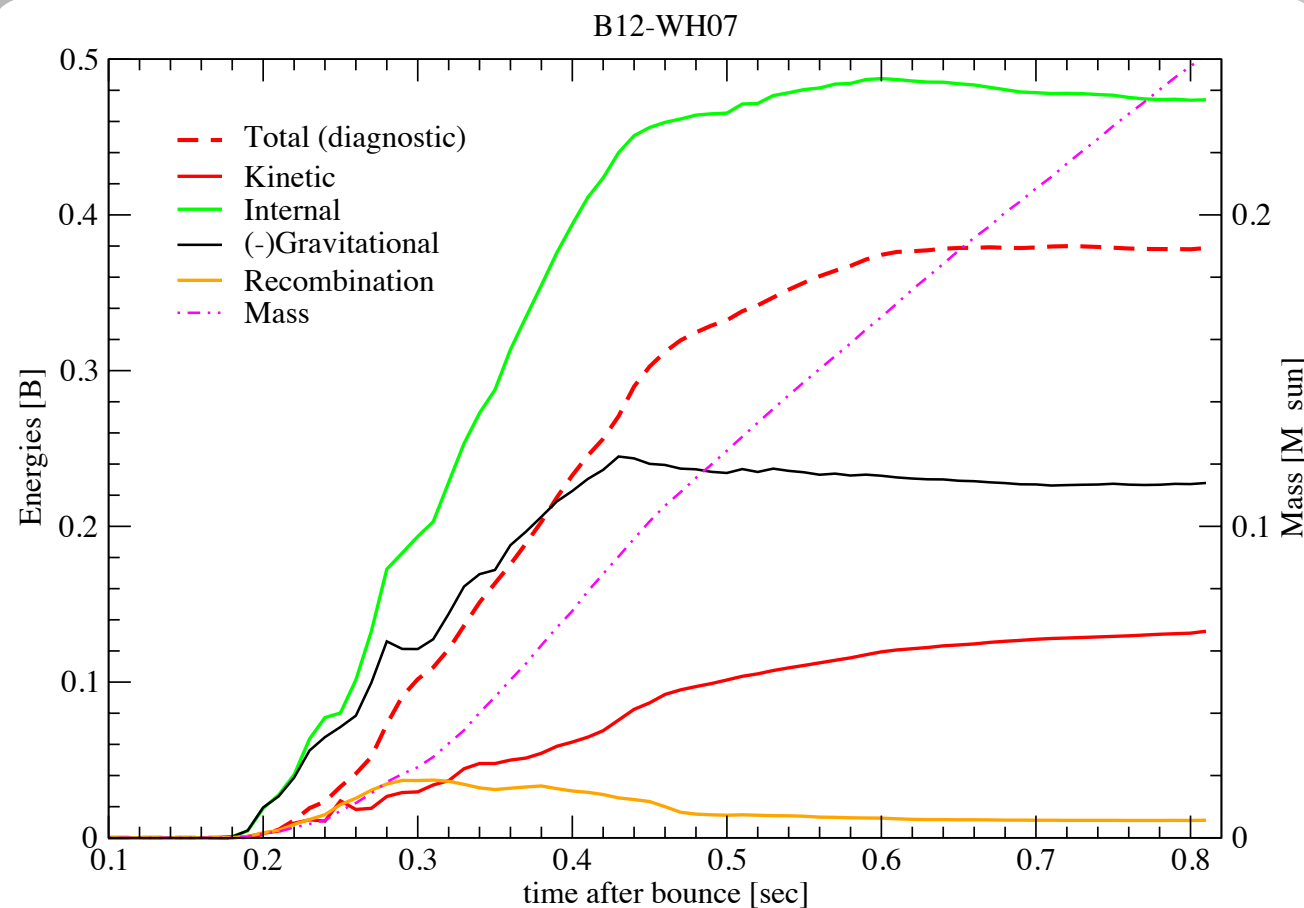


# Explosion energies

- Because models are still in the stage where internal energy dominates, we must estimate the explosion energy by assuming efficient conversion of  $E_i \Rightarrow E_k$ .
- One can construct a “diagnostic” energy,  $E_+ = E_i + E_g + E_k$ , summed over zones where  $E_+ > 0$ .
- To this we add contributions from nuclear recombination and removing the envelope.

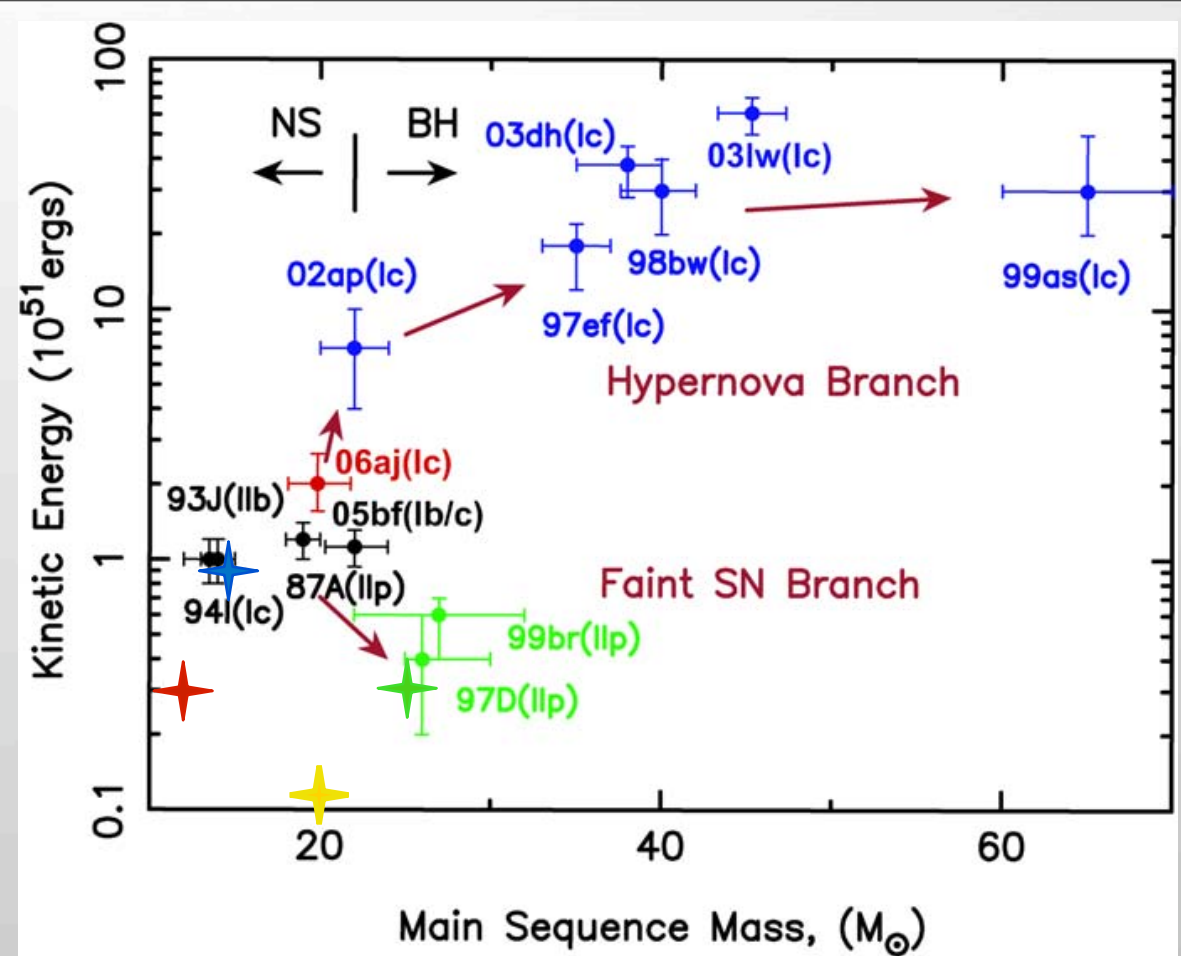


Nomoto, Tominaga, et al. (2006)

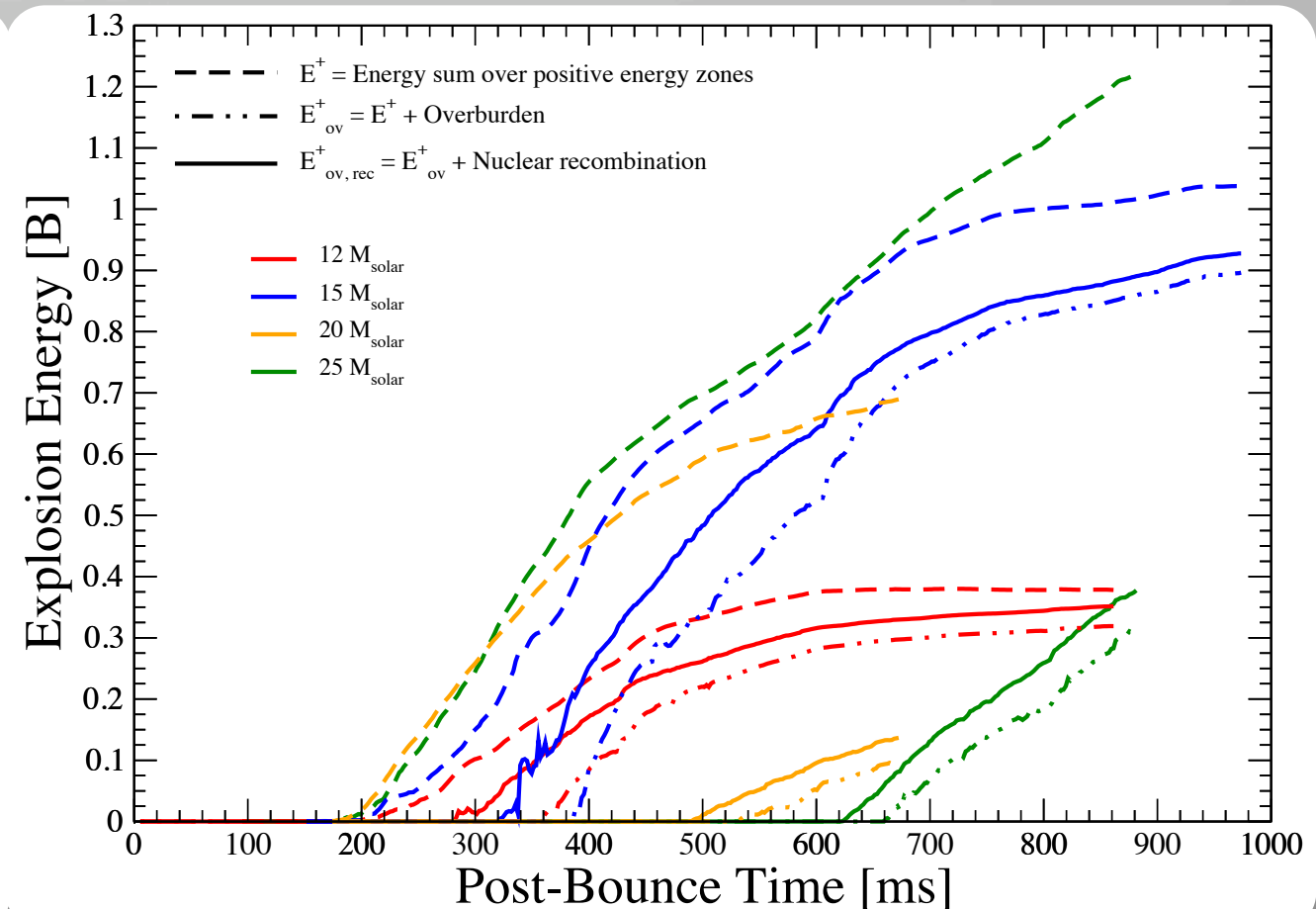
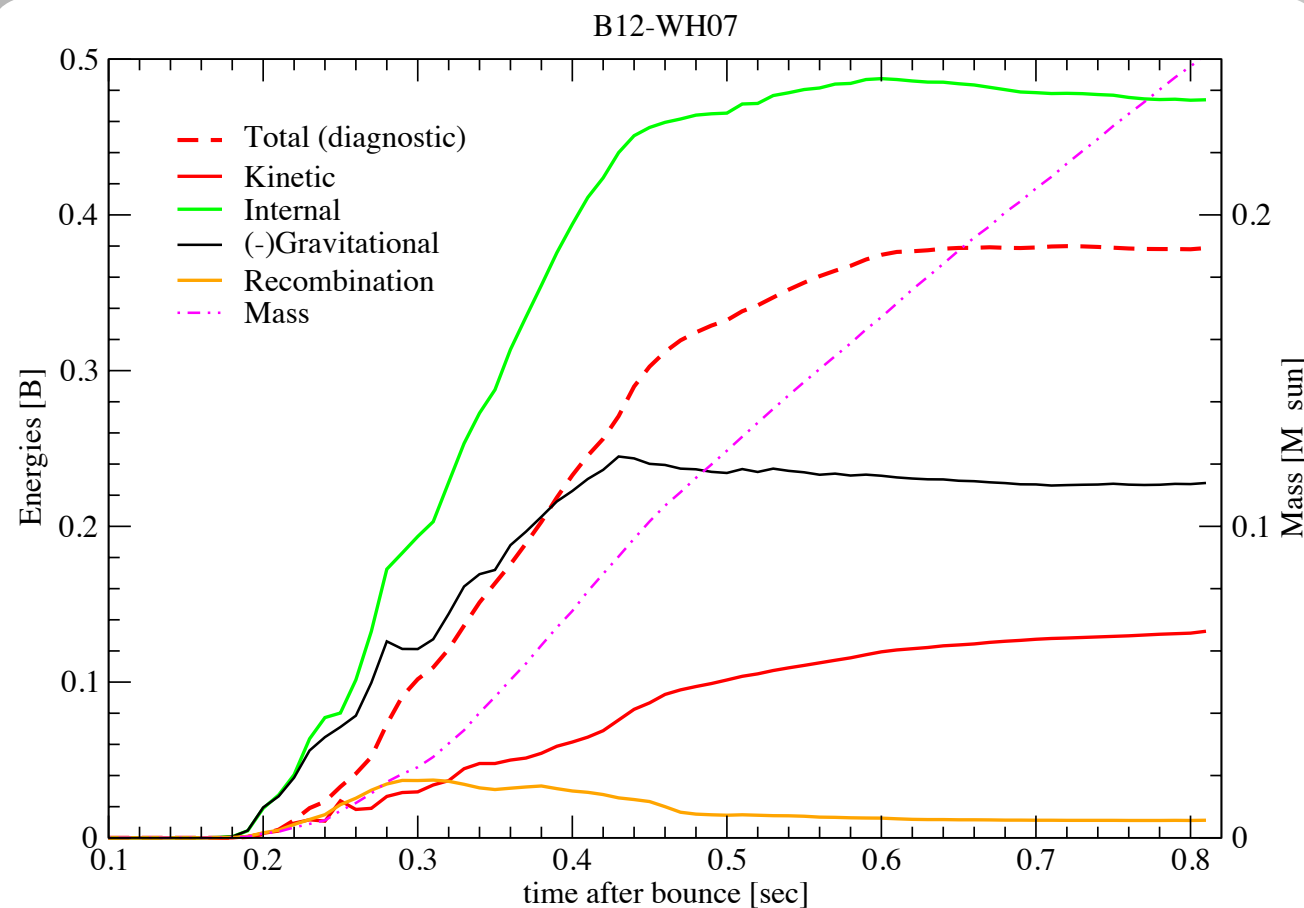


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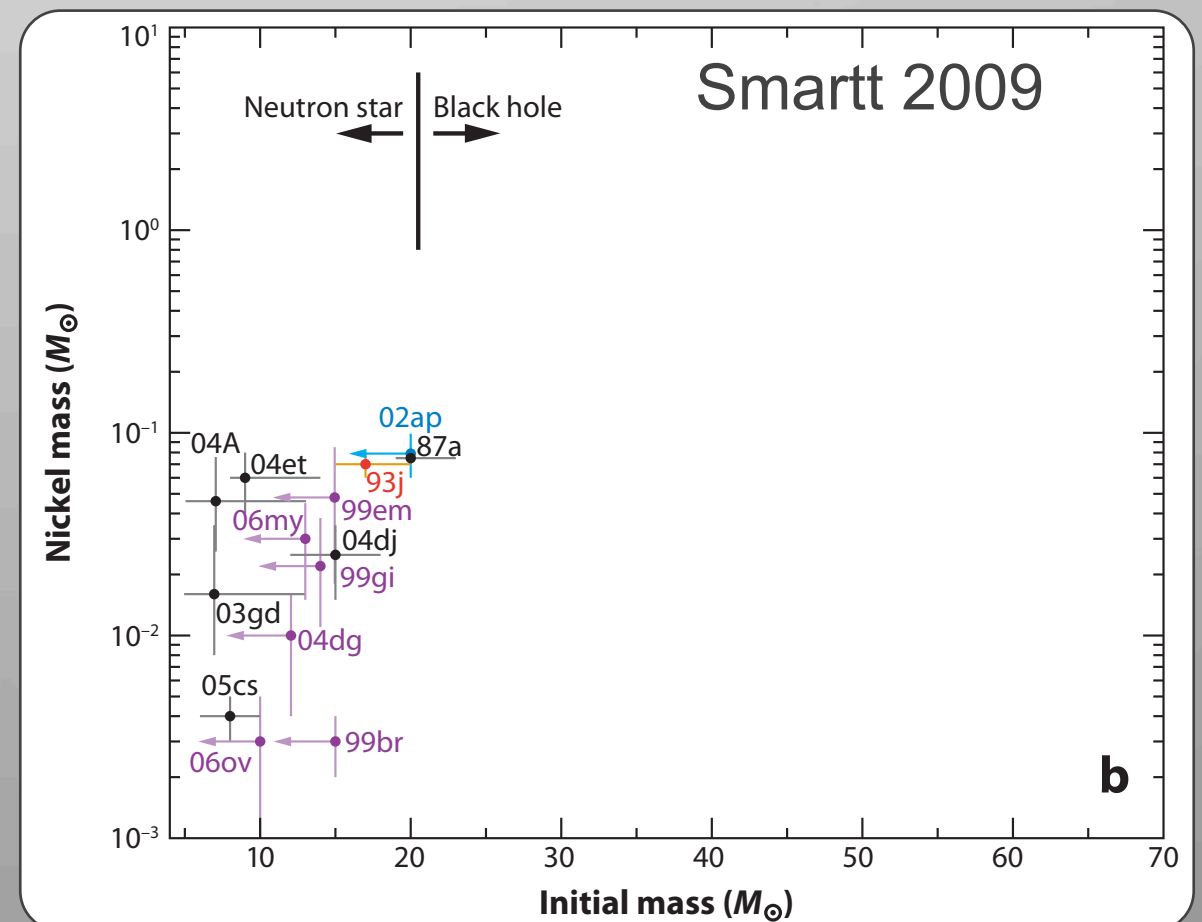
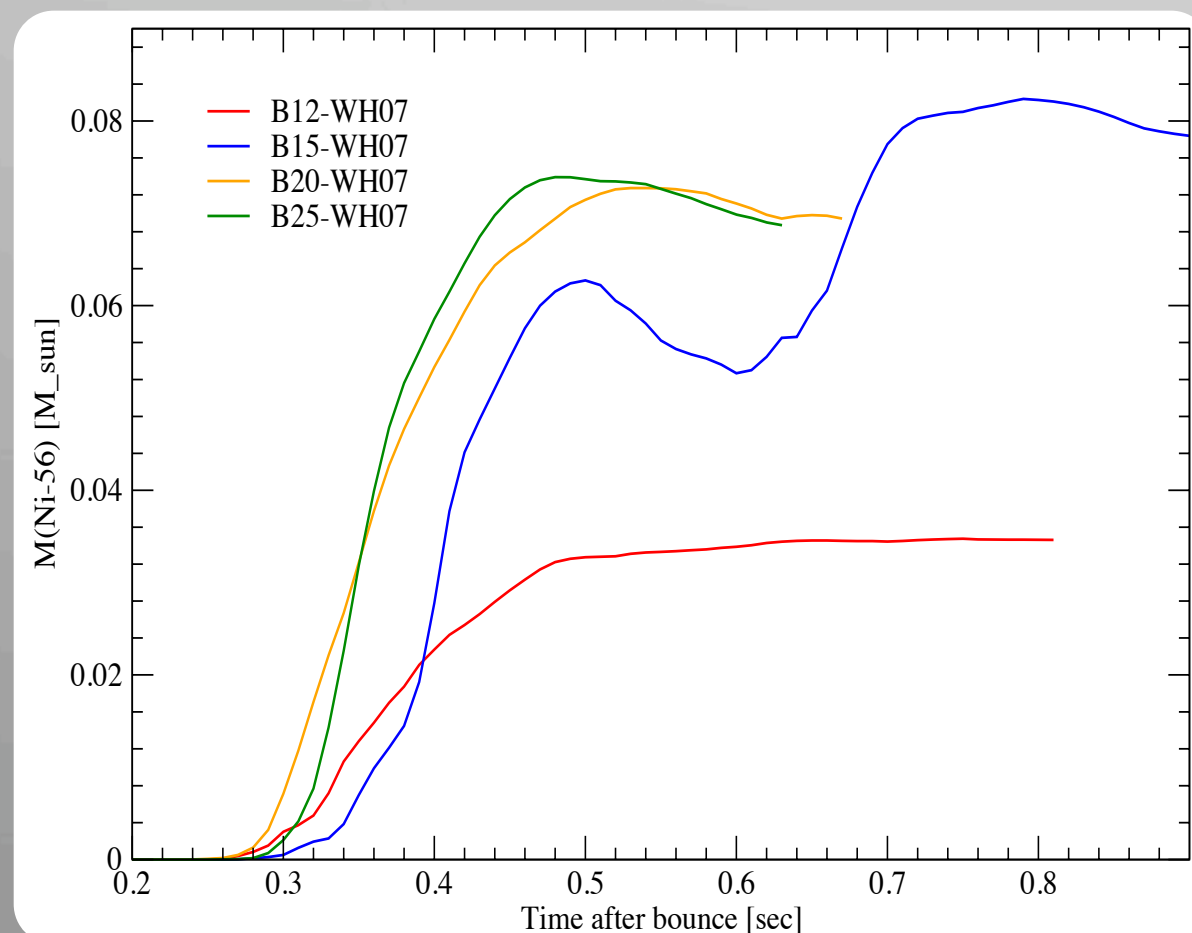
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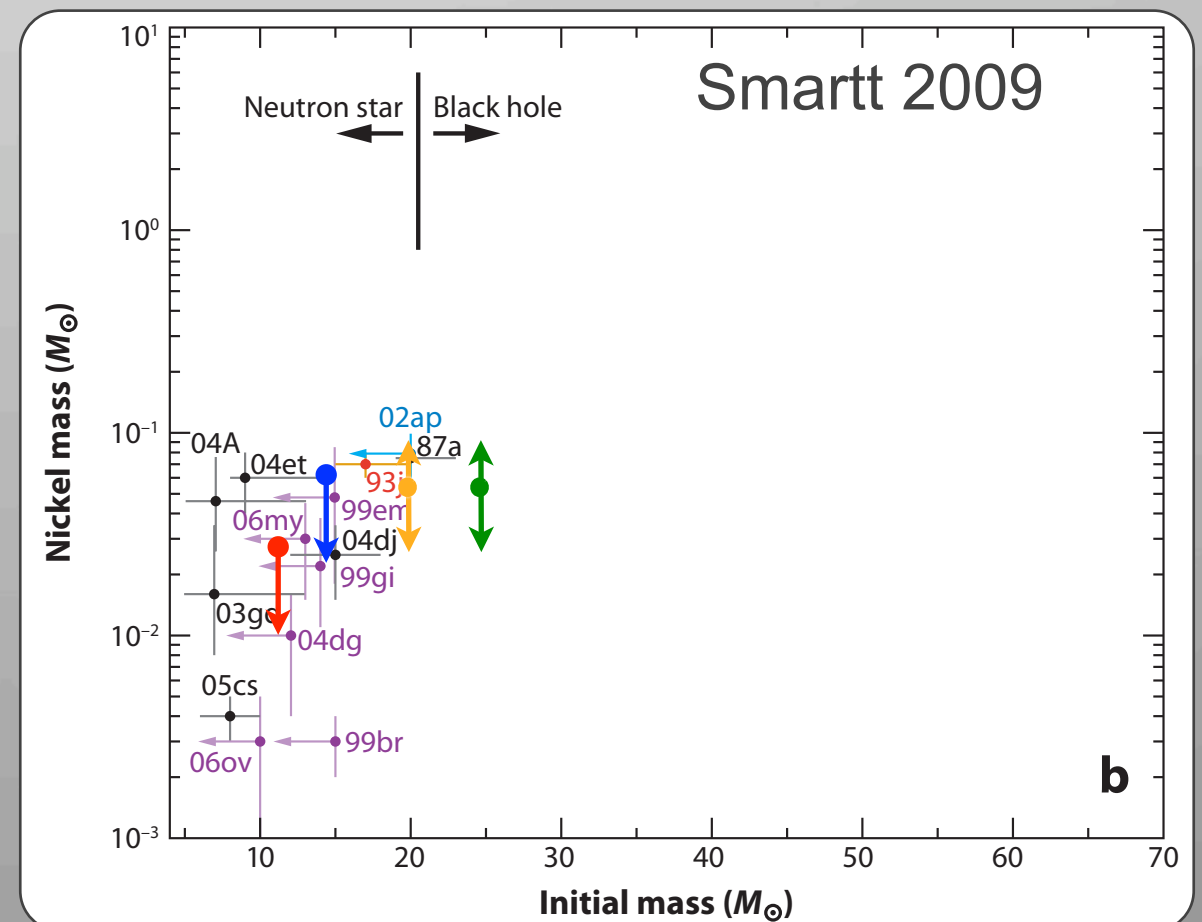
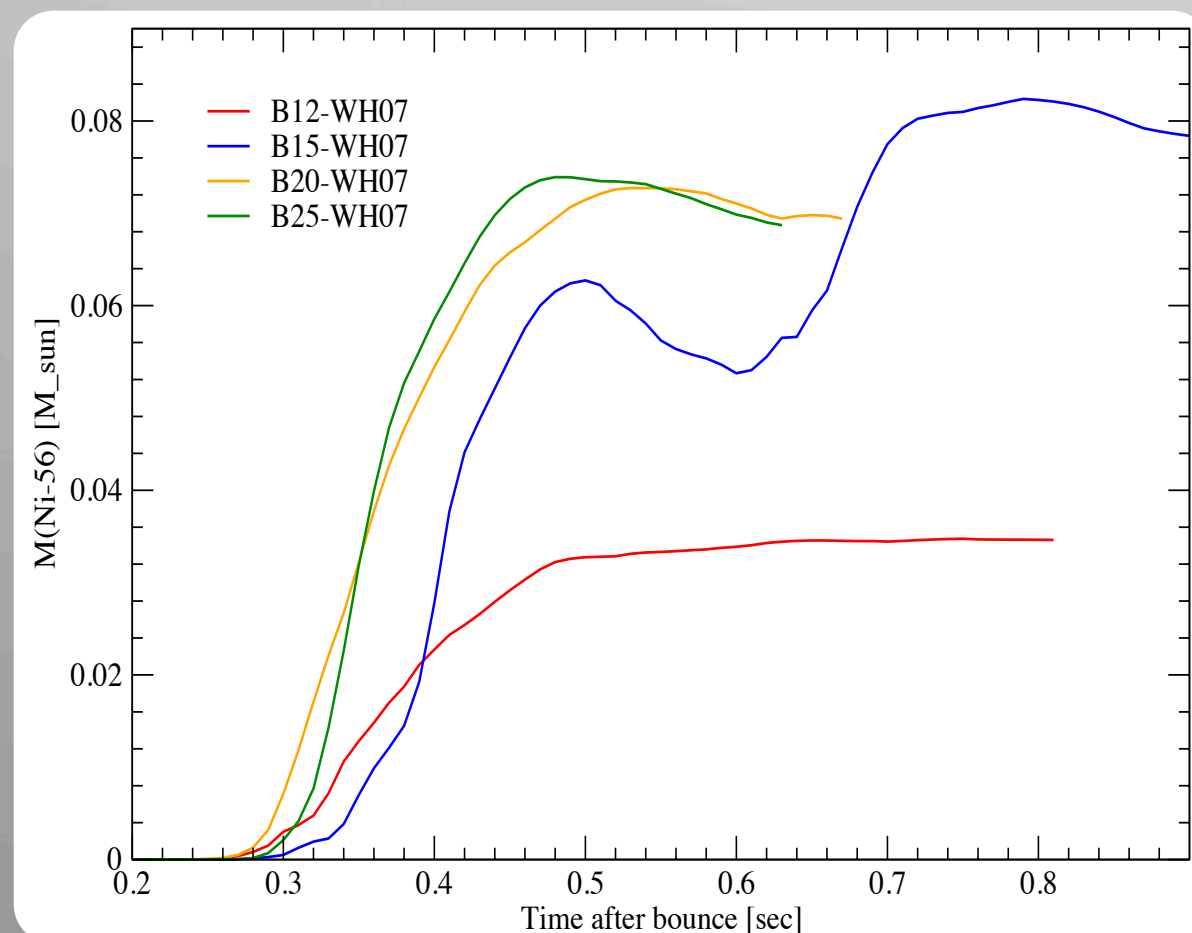
# Nickel mass

- Another important observable, related to the explosion energy and very relevant to the nucleosynthesis, is the mass of  $^{56}\text{Ni}$ .
- Only in the  $12 M_{\odot}$  case has the  $^{56}\text{Ni}$  mass saturated.
- Mass of other iron-peak species is comparable to  $^{56}\text{Ni}$ .
- Results are reasonable, though fallback over longer timescales is uncertain. Recent studies are finding differing results on fallback.



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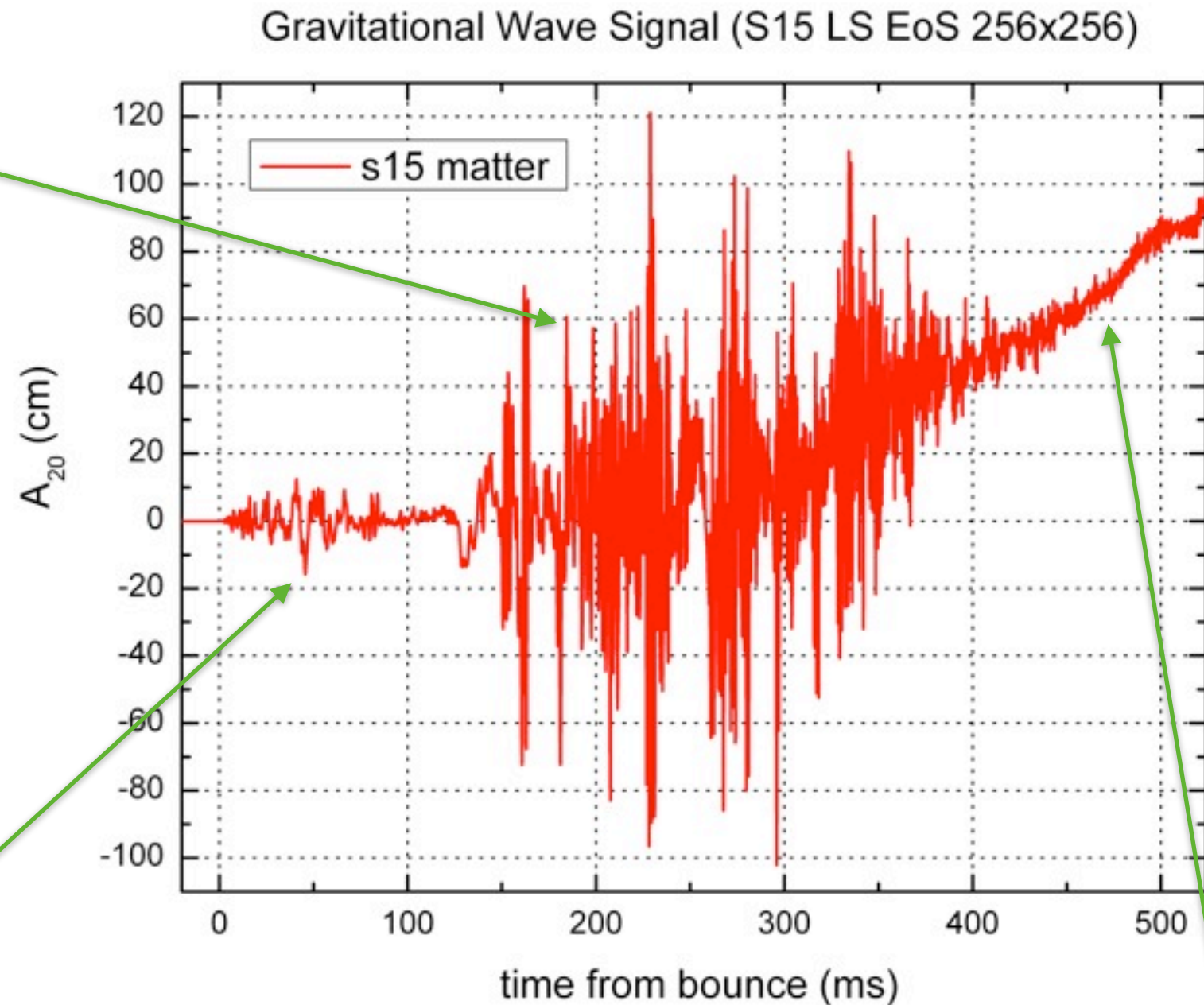
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# Example of multi-messenger observables: Anatomy of a GW signature

Yakunin et al. *Class. Quantum Grav.* 27 **194005** (2010)

- Lower-frequency envelope: SASI-induced shock excursions
- Higher-frequency variations: Impingement of downflows on PNS from neutrino-driven convection and SASI



- Prompt Convection
- Early Shock Deceleration

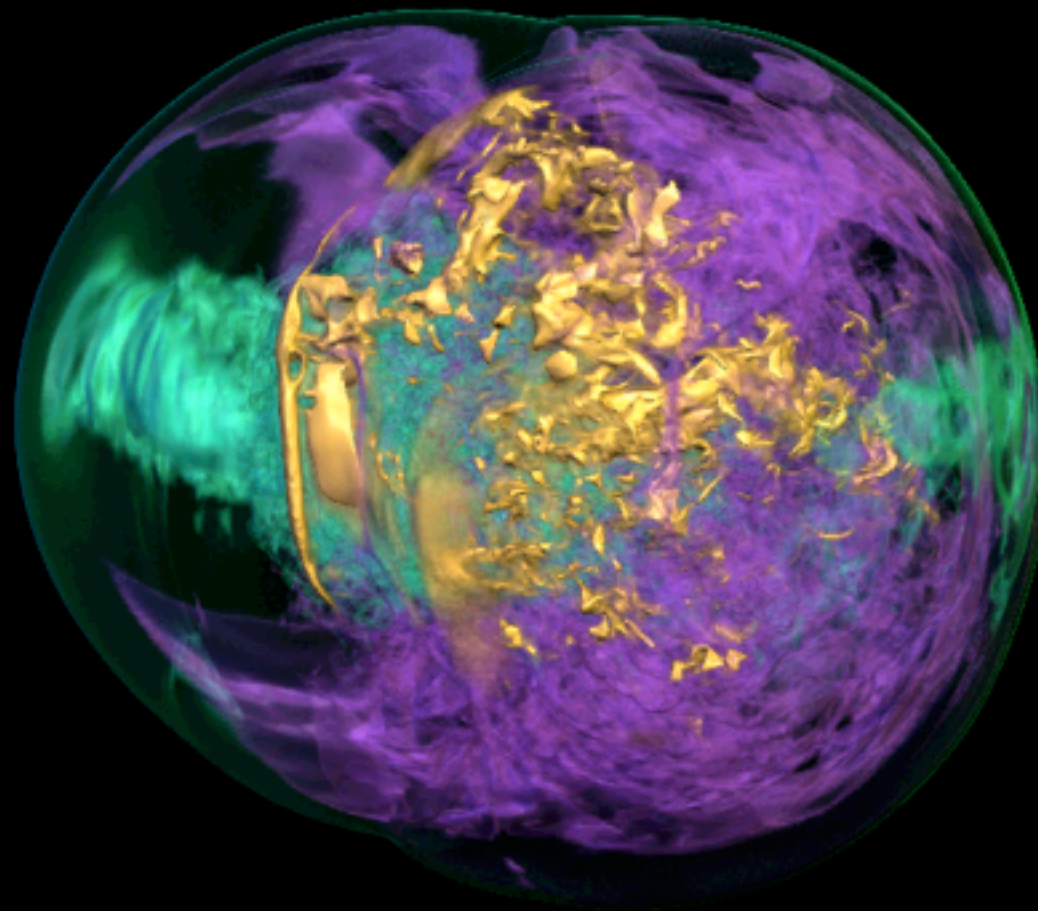
- Later Rise: Prolate Explosion/Deceleration at Shock



# SASI in 3D

Blondin & Mezzacappa *Nature* **445**, 58 (2007)

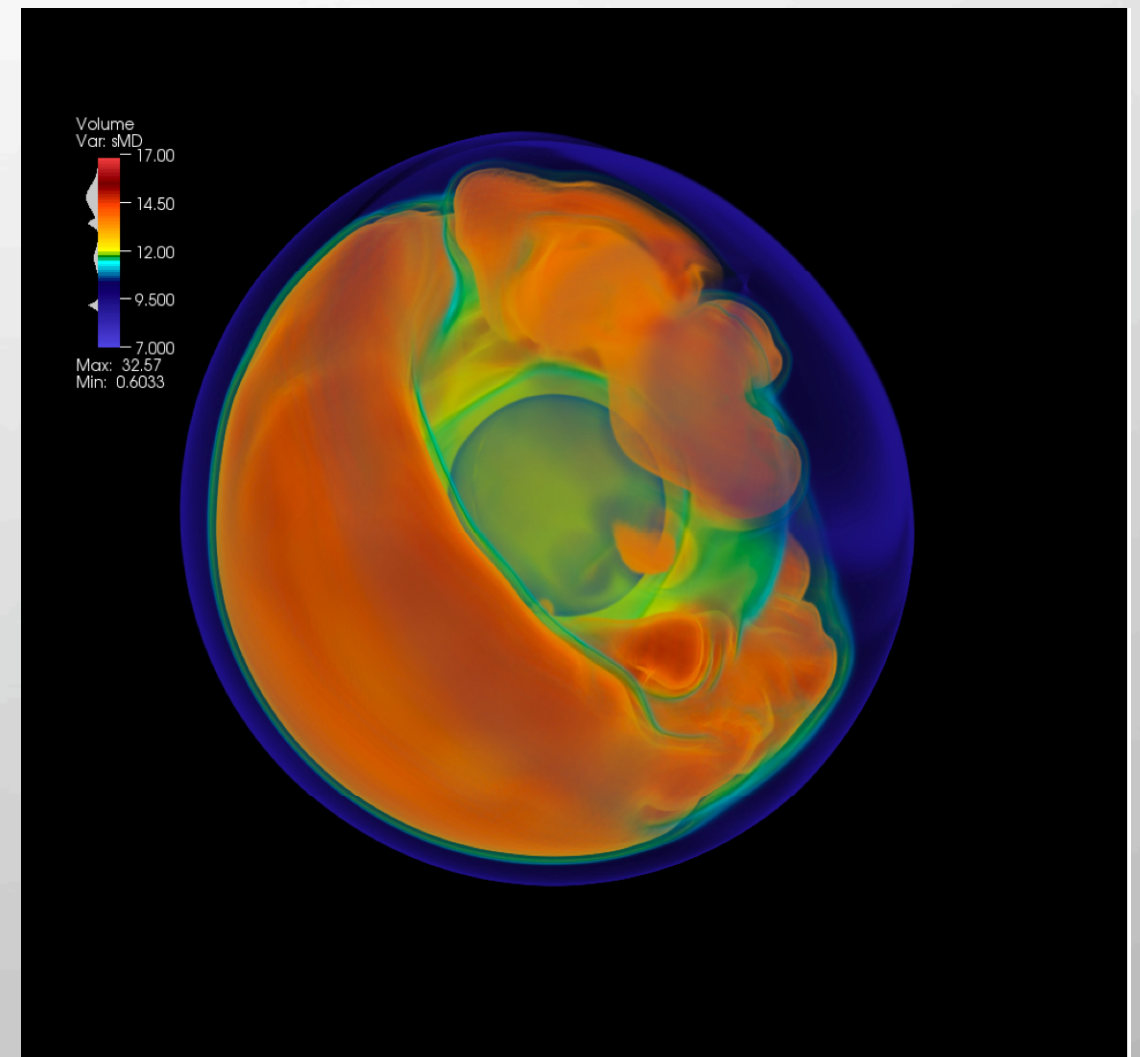
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Blondin & Mezzacappa *Nature* **445**, 58 (2007)

# 3D simulations

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  - GR aberration (in flux limiter)
- 3D PPM Hydrodynamics
  - GR time dilation, effective gravitational potential
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  - 180 MeV nuclear compressibility
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## Resolution

304 X 76 X 152

⇒ 11,552 MPI tasks

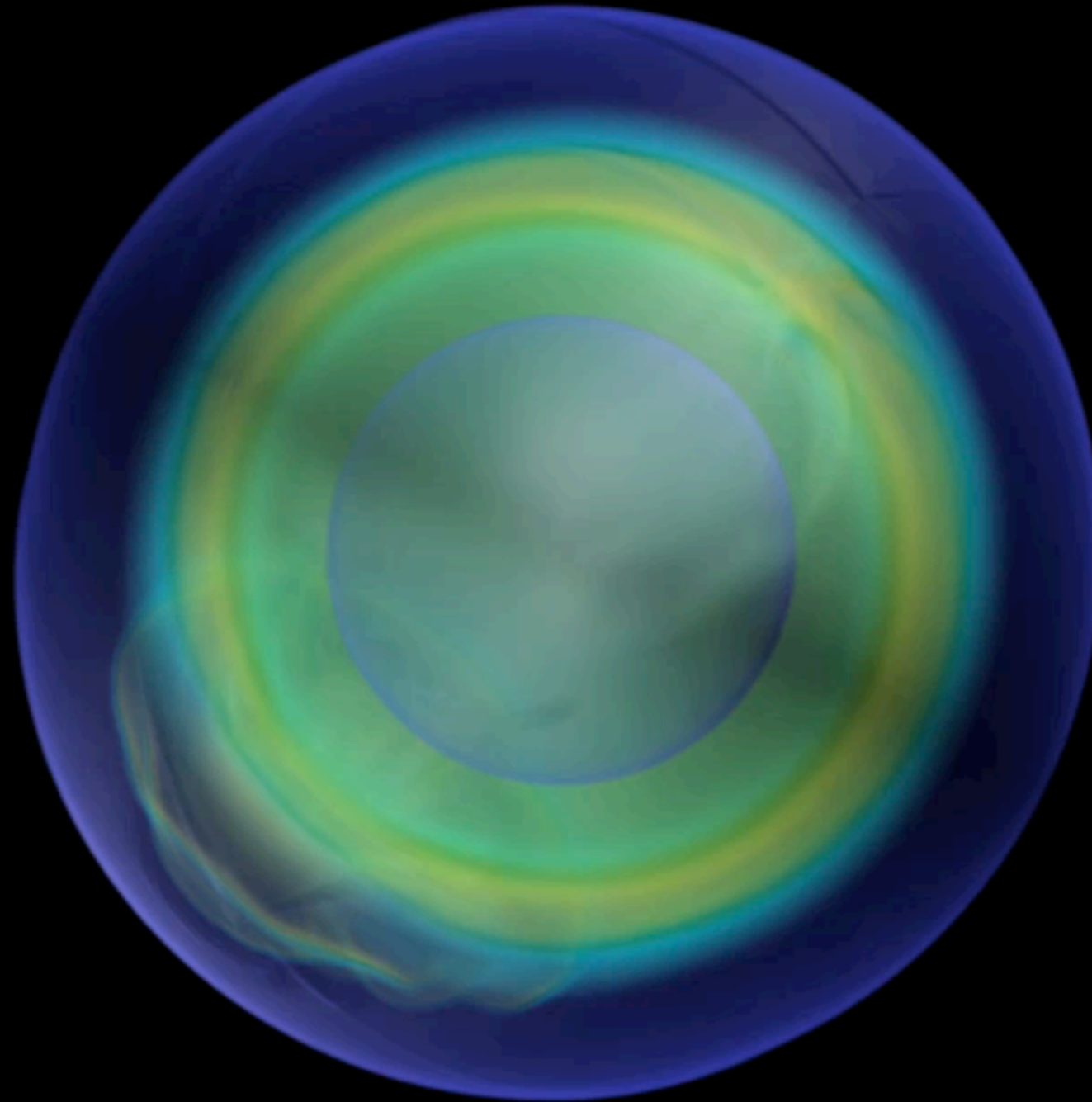
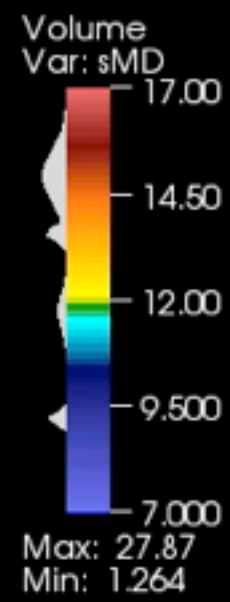
576 X 96 X 192 (current production size)

⇒ 18,432 MPI tasks

512 X 256 X 512

⇒ 131,072 MPI tasks





Time=0.268844

# Summary

- Ongoing CHIMERA models confirm successful prolate explosions across a range of progenitors from 12-25  $M_{\odot}$  driven by neutrino heating and SASI.
- Though differences persist with simulations from Garching group, self-consistent CHIMERA simulations point to a successful neutrino-reheating mechanism, with the explosion delayed by 300 ms or more after bounce, **at least in 2D**.
- Self-consistent 3D simulations, while very expensive, are possible. They are critical to teach us the value of our 2D simulations.