

# The dynamics of tidal tails

(or how to do cosmology with the Galaxy)

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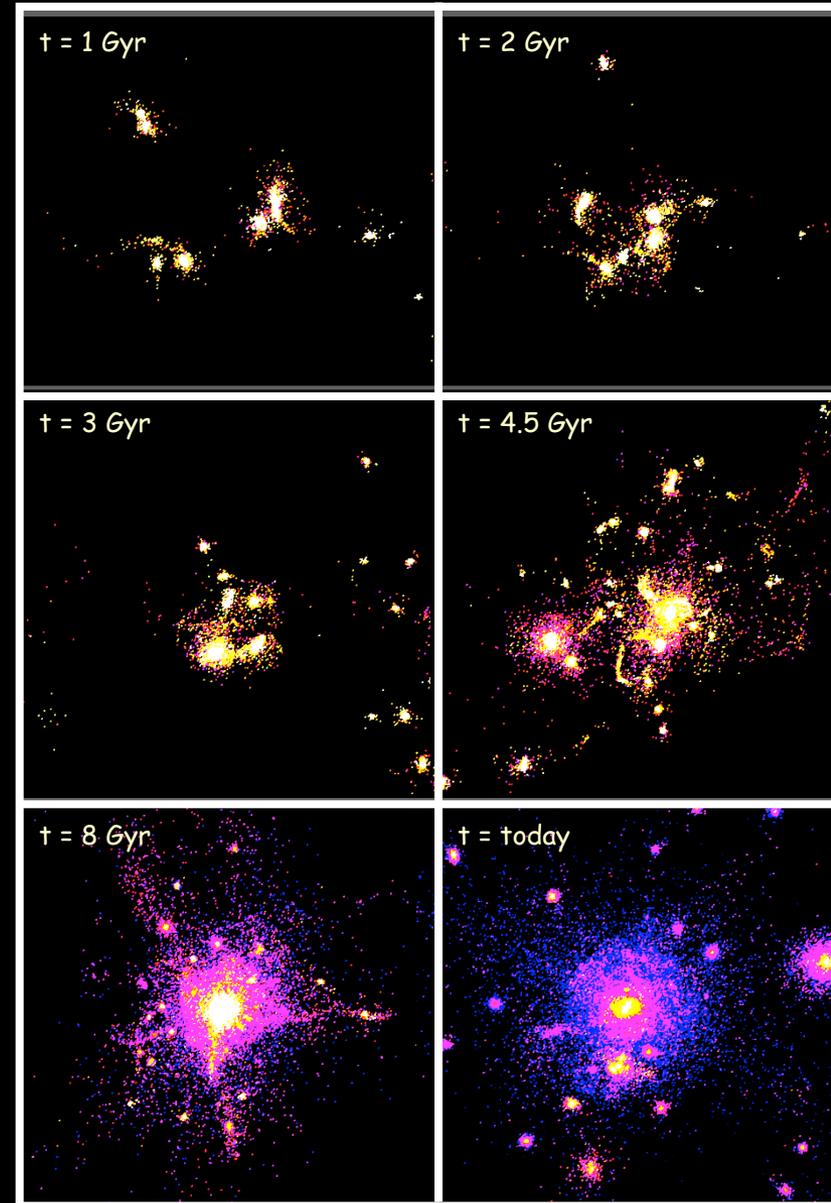
university of  
groningen

faculty of mathematics  
and natural sciences

kapteyn astronomical  
institute

# Testing the hierarchical paradigm. I. Mergers

- Stellar halo contains direct imprints of merger history
- **Tidal streams/substructures**
  - We need to find them and understand (model) their behaviour
  - Were mergers important for Milky Way?
  - How often and when did they happen?
  - What do they tell us about the building blocks? What were their properties?



# Testing the hierarchical paradigm. II

Is this “picture” correct?



- Are galaxies like the Milky Way embedded in dark matter halos like those predicted by the cosmological model?

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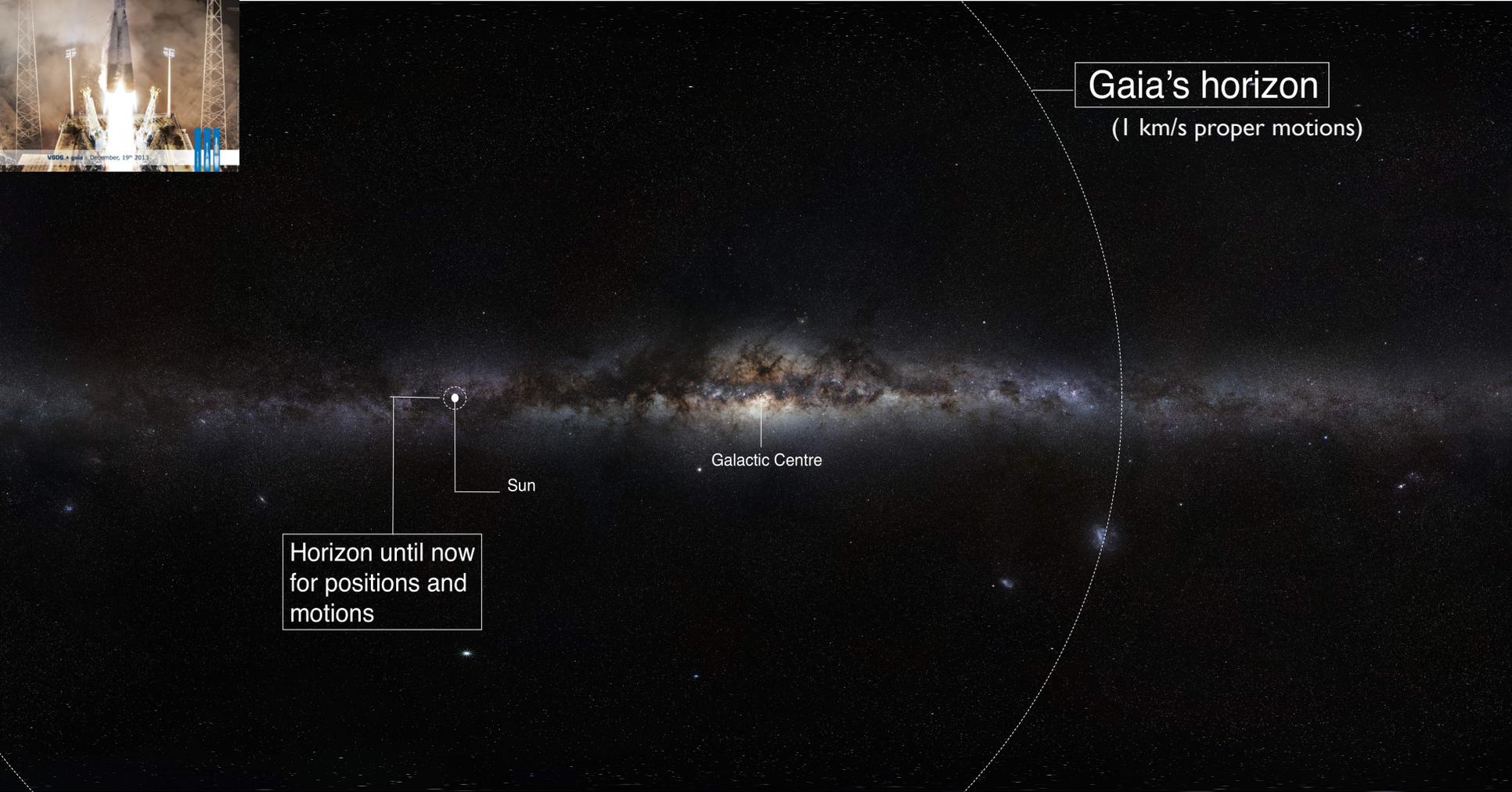
# Testing the hierarchical paradigm. II

Is this “picture” correct?



- Are galaxies like the Milky Way embedded in dark matter halos like those predicted by the cosmological model?
- How much dark matter is there?
  - how is it distributed? Shape, density profile, granularity, time-evolution
  - what is the dark matter?

# The Gaia revolution: starting now!



Gaia's horizon

(1 km/s proper motions)

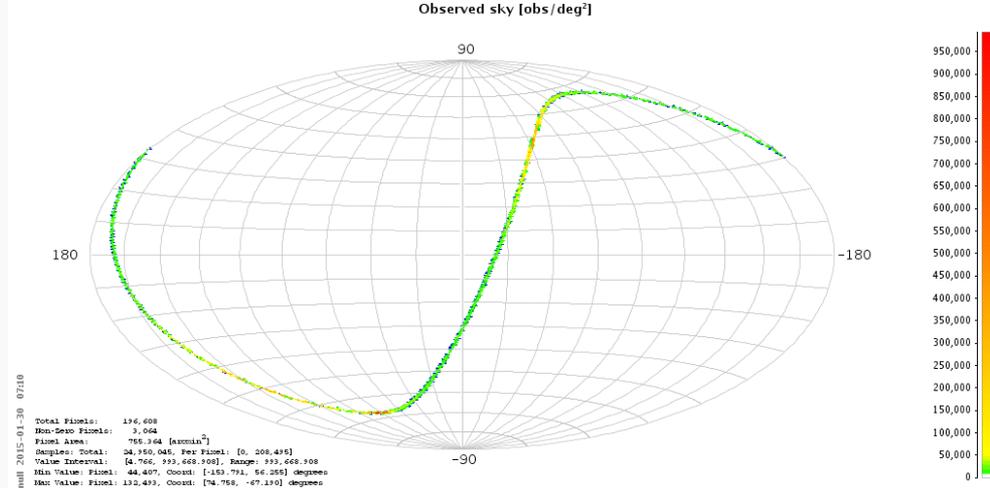
Sun

Galactic Centre

Horizon until now  
for positions and  
motions

Gaia will measure positions and motions of stars for  $10^9$  stars (10,000 x larger than predecessor); over a volume 100,000 larger; 1,000 more precisely → transformational

- Simultaneous astrometry, photometry, spectroscopy
- Complete to  $G = 20$  ( $V = 20-22$ ),  $G = 16$  for spectroscopy
- Whole sky already observed!
- First data release in mid-2016 (positions +  $G$  magnitude)
- DR2 in Jan 2017: full phase-space



up to 21 million objects/deg<sup>2</sup>  
By Jan. 2015, 16 billion photom/astrom transits,  
1.6 billion spectroscopic

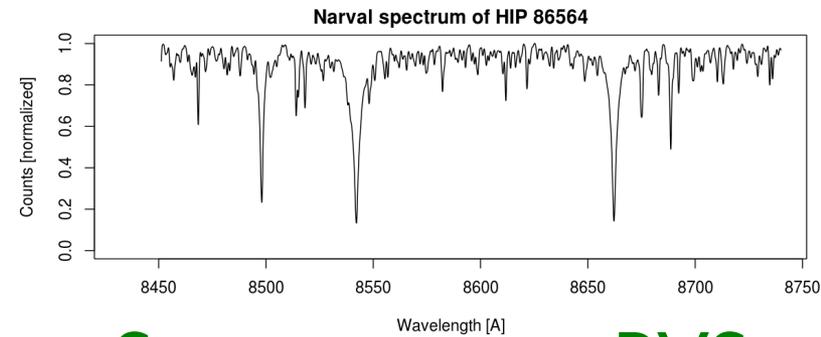
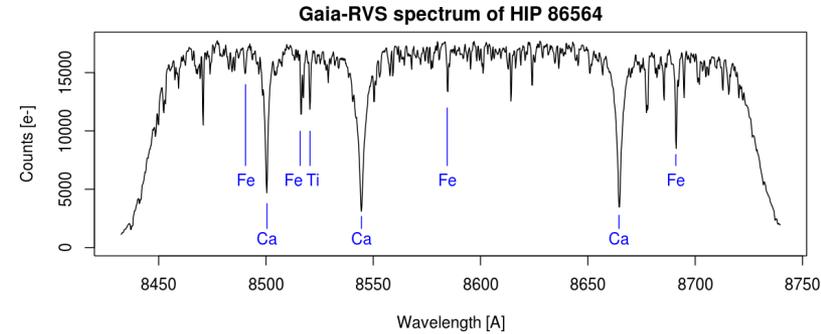
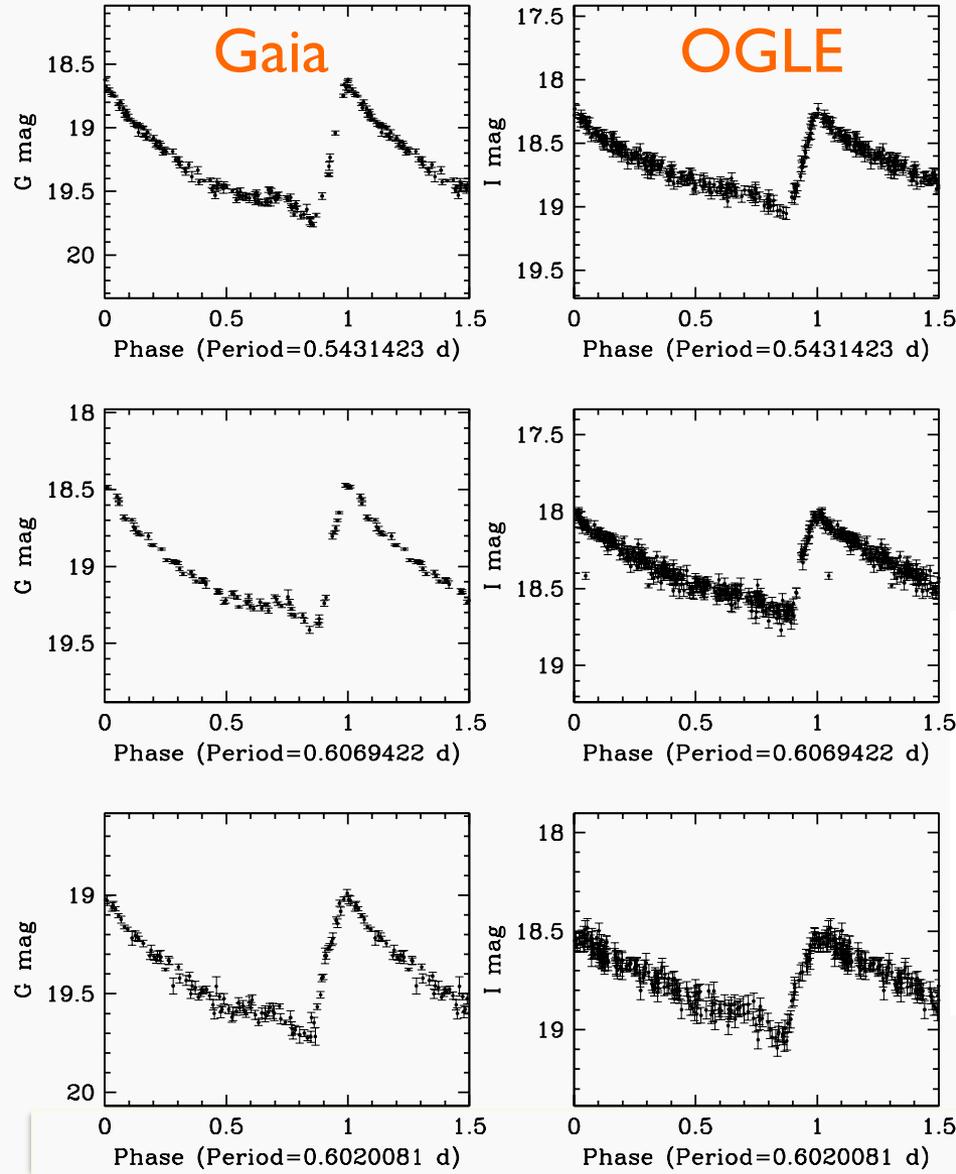
Performance predictions for G2V star			
V magnitude	Astrometry (parallax)	Photometry (BP/RP integrated)	Spectroscopy (radial velocity)
3 to 12	5–14 $\mu\text{as}$	4 mmag	
3 to 12.3			1 km s <sup>-1</sup>
15	24 $\mu\text{as}$	4 mmag	
15.2			15 km s <sup>-1</sup>
20	540 $\mu\text{as}$	60 (RP) – 80 (BP) mmag	

Calculations by: Airbus DS, D. Katz, C. Jordi, L. Lindegren, J. de Bruijne

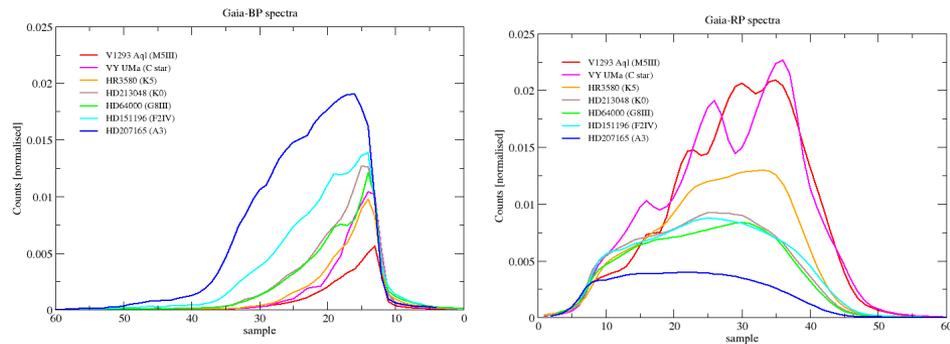
Up-to-date information always at:  
<http://www.cosmos.esa.int/web/gaia/science-performance>

Courtesy of  
Anthony  
Brown &  
Gaia/DPAC

# Photometry RR Lyrae in the LMC



## Spectroscopy: RVS



## Spectro-photometry

astrophysical parameters

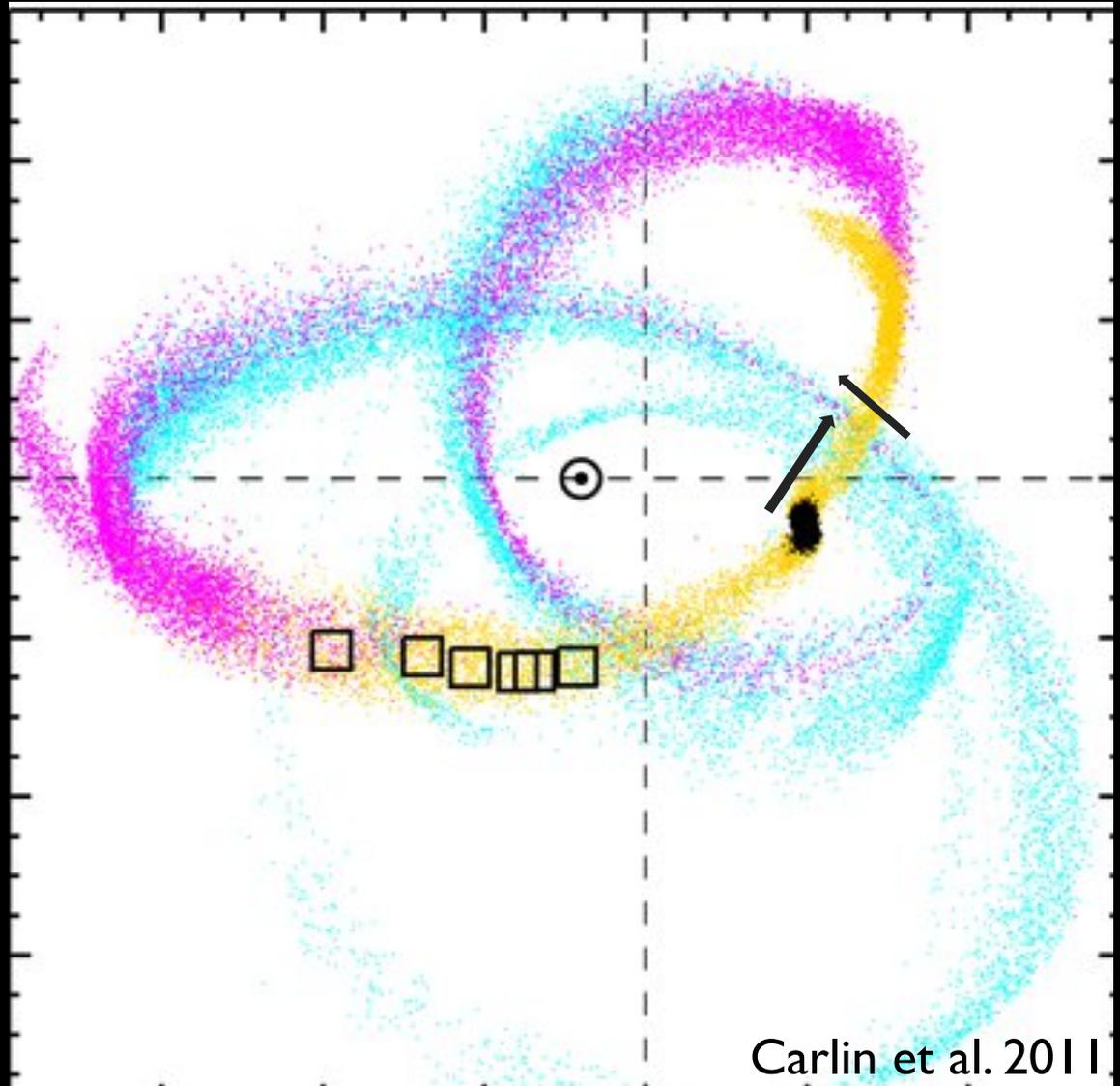
Back to streams

# Streams in physical space

A single object can give rise to multiple, spatially crossing streams

We can speak of leading or trailing streams if mapping is close to continuous (connect the pieces)

A priori we might not know if two structures/streams in space have the same parent



# Streams in action-angle space

- Action-angle evolution is simple:

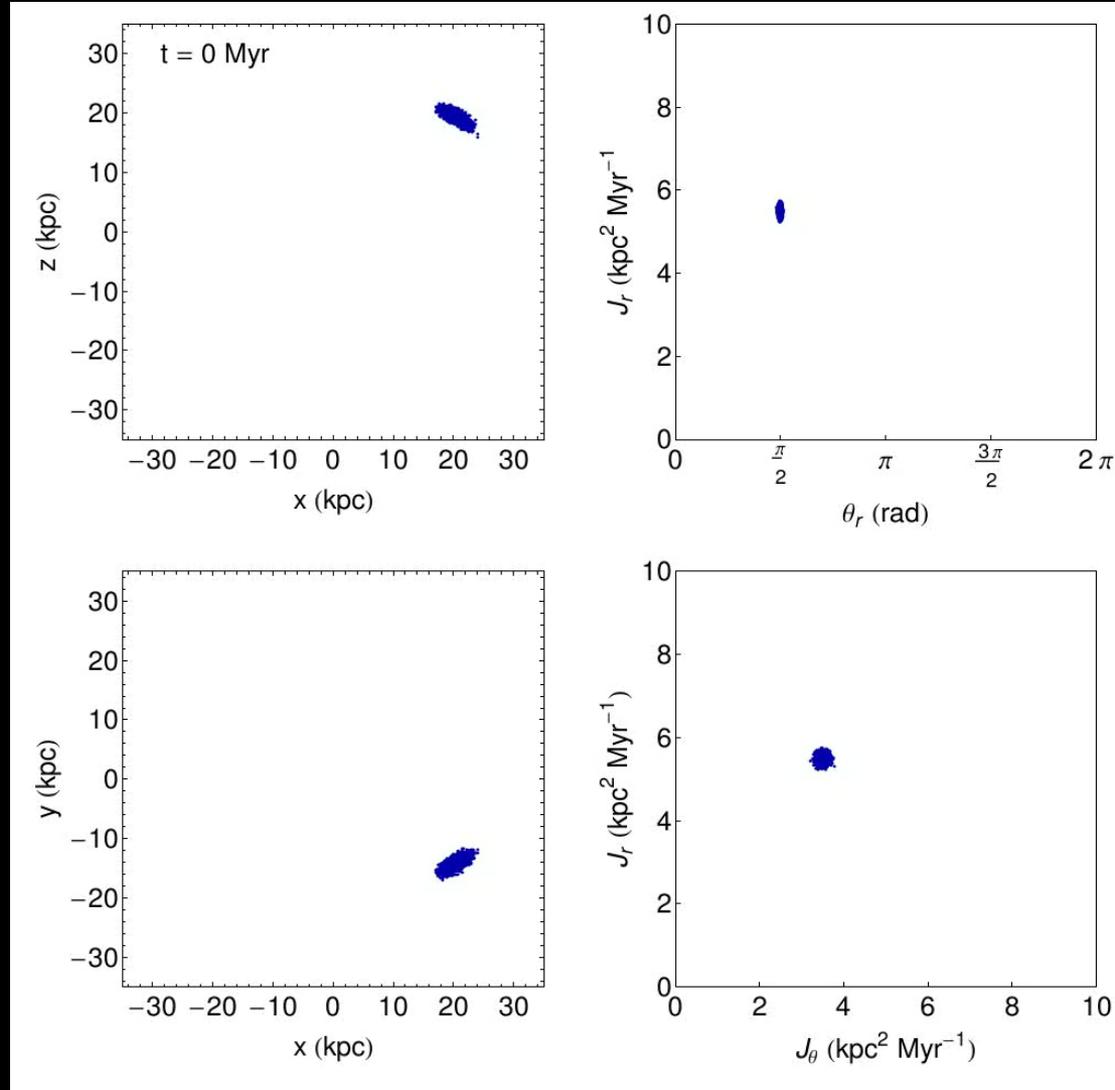
$$\theta = \theta_0 + \Omega(J) t$$
$$J = J_0$$

- streams spread out in angle
- actions are adiabatic invariants

- Behaviour is very simple in action-angle space

- difficulty is to find actions/angles for any non-spherical potential (Bovy 2014; Sanders & Binney 2013, 2014)
- Caveat: assume stars feel only host after released

- Stars from same object should be maximally clustered in action-space in right potential (talk by Sanderson)
  - even if potential changed with time



# How do we understand the evolution?

Principle:

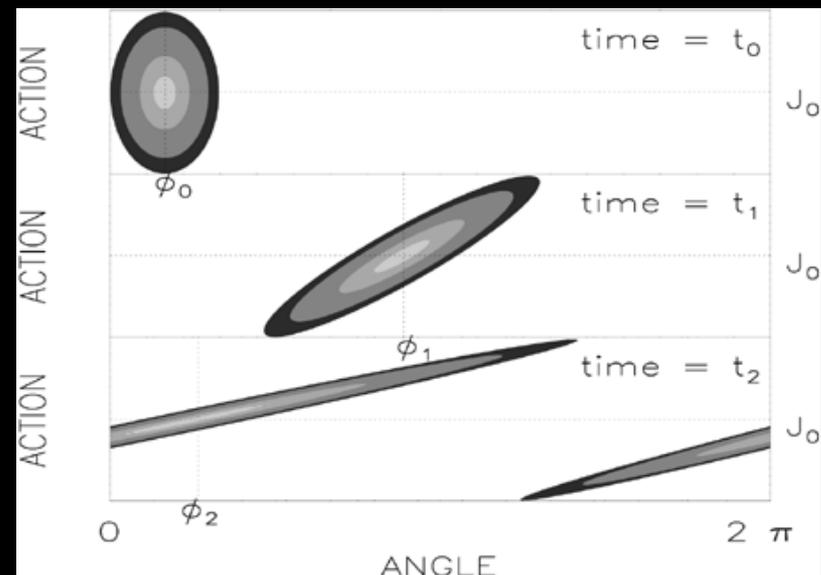
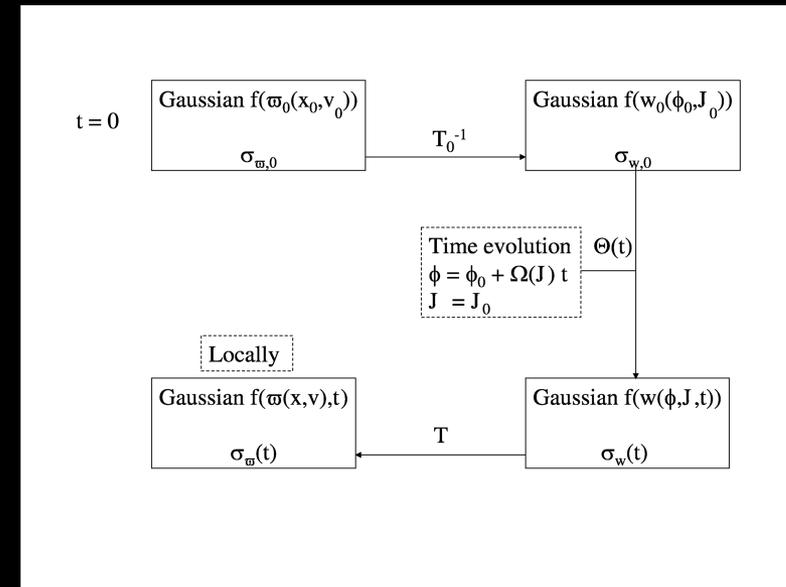
Follow  $df$  evolution in action-angle space

$$\Delta\theta_i \sim \Delta\Omega_i t \sim \frac{\partial\Omega_i}{\partial\mathbf{J}} \Delta\mathbf{J} t$$

$$\Delta\theta = \mathbf{H} \Delta\mathbf{J} t$$

Predict properties in observable space:

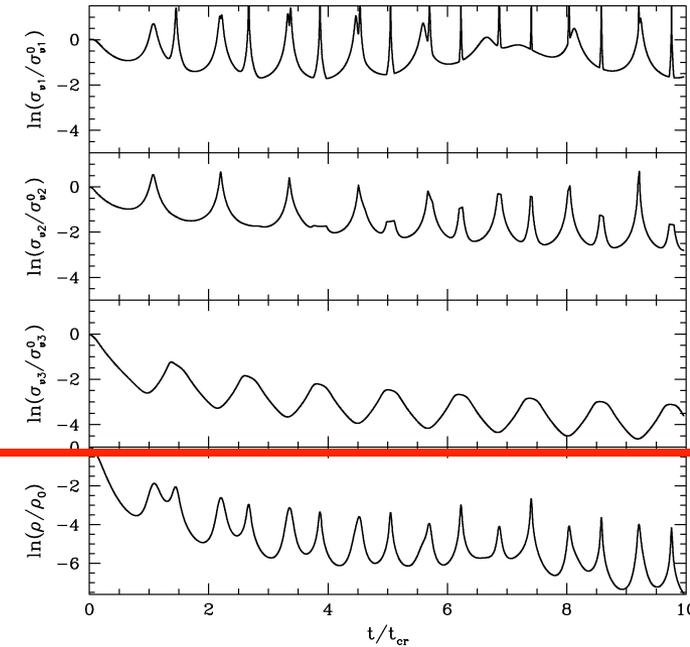
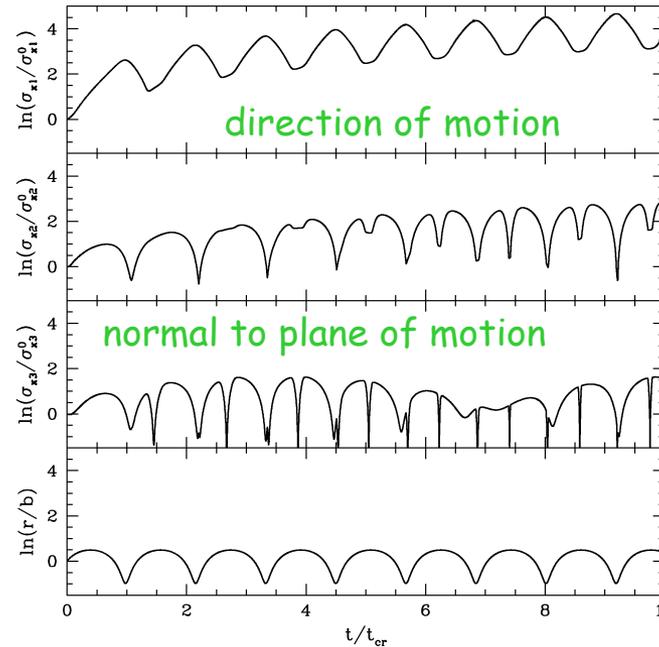
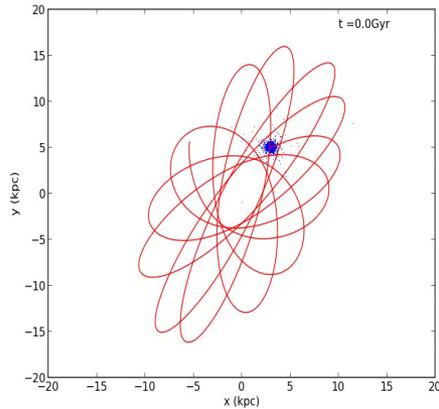
- Perform local linear coordinate transformation to  $(x,v)$
- Determine the width, extent and velocity dispersion along a stream as  $f(t)$



# Evolution of streams in a spherical potential

spatial properties

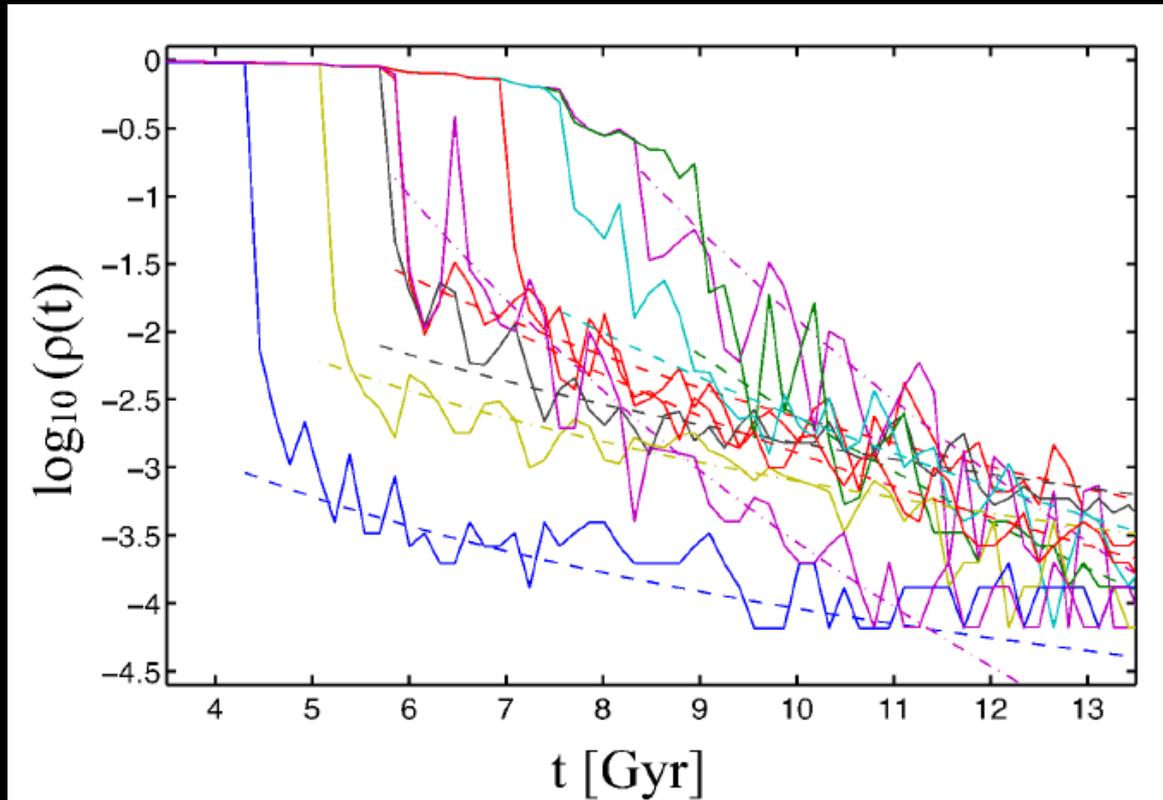
velocity dispersion



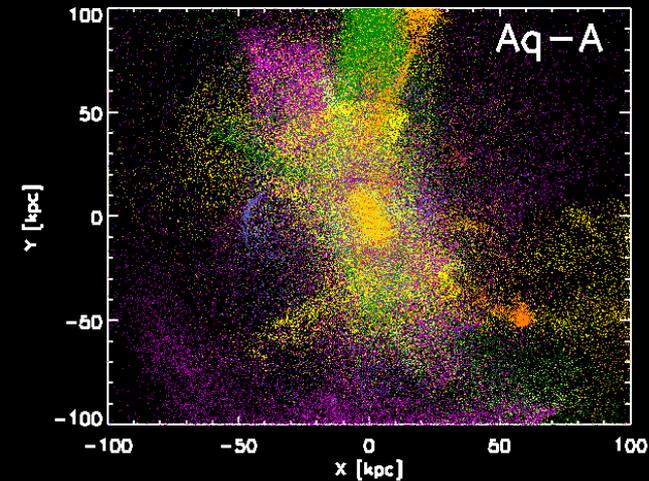
Helmi & Gomez 2007

- Stream elongated along direction of motion, and thicker in plane of motion
- Width of stream normal to plane of motion is  $\sim$  constant (spherical pot.)
- Velocity dispersion decreases as  $1/t$  (conservation of phase-space density)
- Density decreases as  $1/t^2$  (2D problem; axisym or triaxial  $1/t^3$ )

# Streams in cosmological simulations?



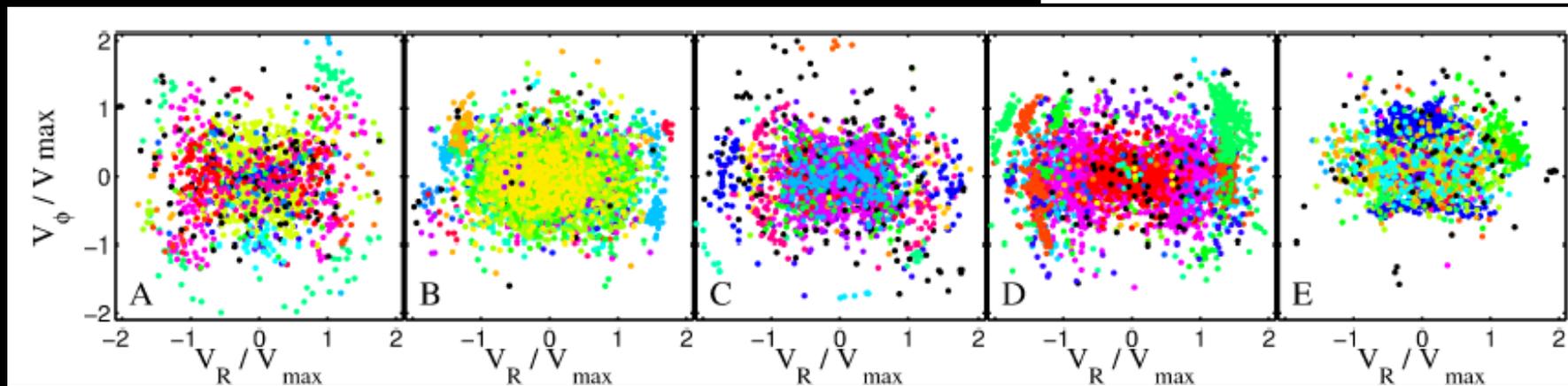
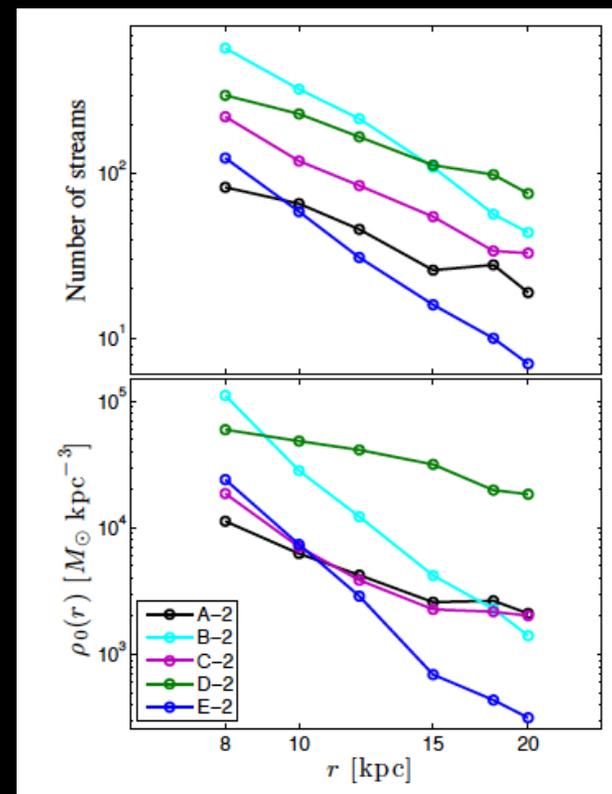
Gomez et al. (2014)



- Cosmological simulations show similar behaving streams
- No strong chaos, power law rather than exponential divergence of orbits  
(poster Maffione)

# Inner/nearby stellar halo in Aquarius

- Few objects contribute here: 75% of stars near Sun from 3-5 parents
- Memory in kinematics (despite “chaotic” build-up)
  - ~ 400 streams crossing Solar neighbourhood
  - Should be identifiable with Gaia



# Streams and the potential

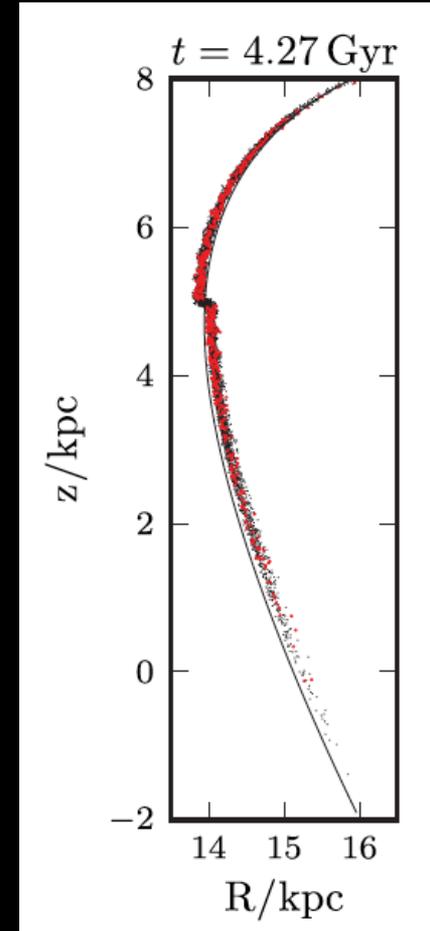
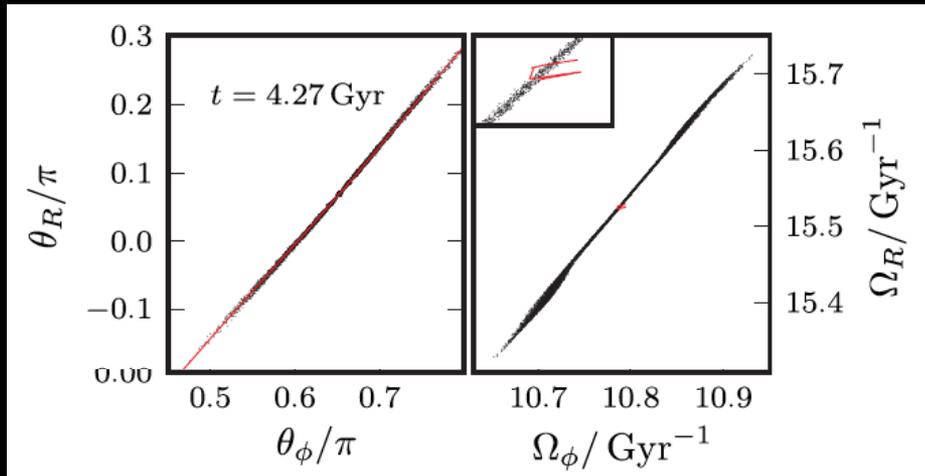
- Computation of angles, actions and frequencies depends on potential assumed

$$\Delta\theta_r \sim \Delta\Omega_r t$$

$$\Delta\theta_\phi \sim \Delta\Omega_\phi t$$

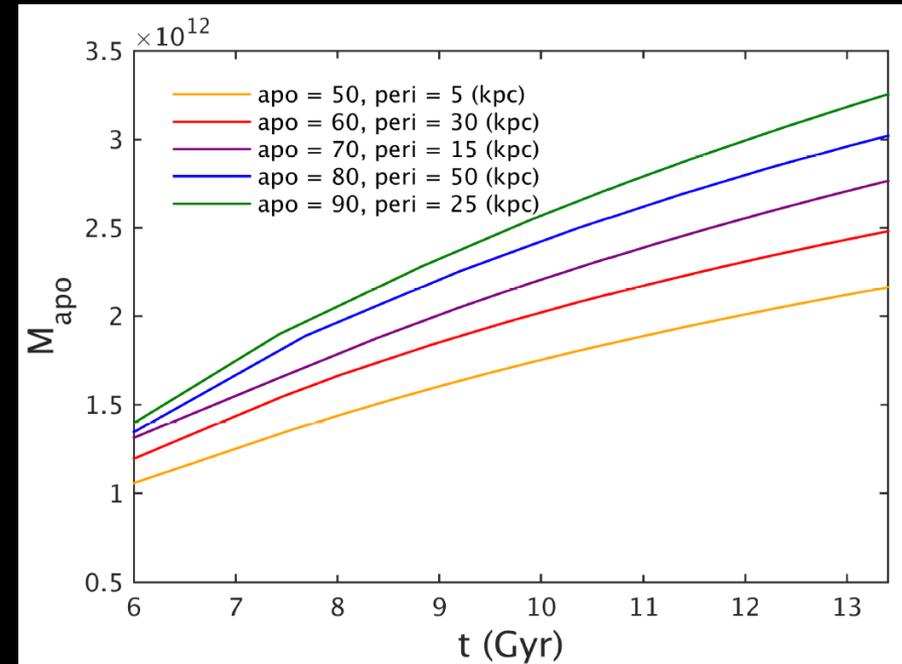
$$\frac{\Delta\theta_r}{\Delta\theta_\phi} = \frac{\Delta\Omega_r}{\Delta\Omega_\phi}$$

- In true potential, **streams on straight lines with same slope** in angle and in frequency space (Sanders & Binney 2014)

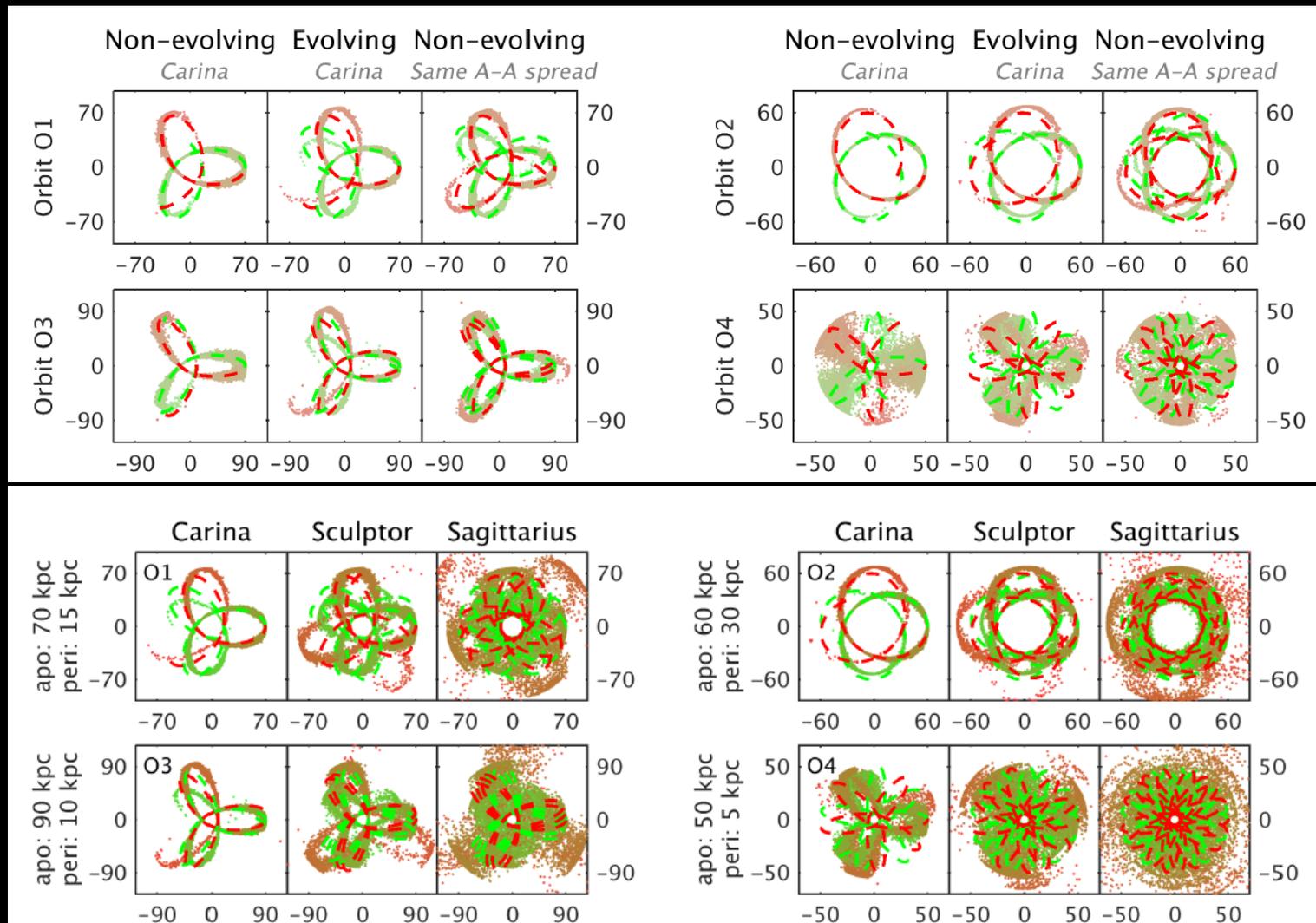


# Streams and time-evolution

- What are the signatures of time-evolution? Can it be measured?
- Model growth of a spherical halo:
  - inside out, cosmological mass-growth  $M \sim \exp(-a_g z)$
  - doubles its mass with orbits considered
  - numerical simulations and analytic formalism based on A-A variables
- Different progenitors + different orbits



# Numerical simulations: imprints of time-evolution



Buist & Helmi, 2015

- Precession in orbital plane differs and misalignment is seen,  $\pm 10$ deg
- To see impact of time evolution: need long streams, preferably on radial orbits

# Analysis in action-angle space

- With time-dependence one cannot use original A-A variables
- Actions are adiabatic invariants (depending on orbit)
- Frequencies and angles are not
- Angles:
- With present-day potential, compute angles and frequencies
- For an ensemble of particles, streams no longer on same straightlines in angle and in frequency space
- Differences are small,  $\sim 0.01 - 0.025$  depending on growth rate

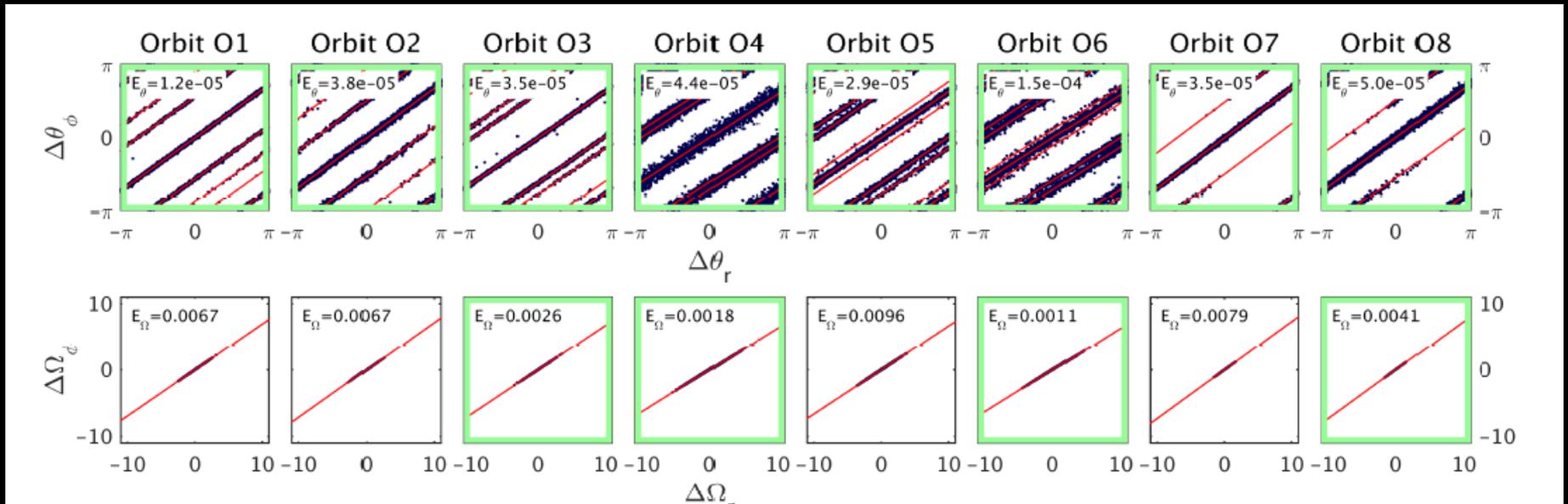
$$J_i = -\frac{\partial H'}{\partial \theta_i} = -\dot{\alpha} \frac{\partial}{\partial \theta_i} \frac{\partial W}{\partial \alpha}(\mathbf{J}, \boldsymbol{\theta}, \alpha),$$
$$\dot{\theta}_i = \frac{\partial H'}{\partial J_i} = \Omega_i(\mathbf{J}, \alpha) + \dot{\alpha} \frac{\partial}{\partial J_i} \frac{\partial W}{\partial \alpha}(\mathbf{J}, \boldsymbol{\theta}, \alpha).$$

$$\langle \dot{\theta}_i \rangle \approx \Omega_i(\mathbf{J}, \alpha) + O(\dot{\alpha}^2, \ddot{\alpha}).$$

$$\theta_i(t) \approx \theta_i(0) + \int_0^t \Omega_i(\mathbf{J}, \alpha(t)) dt,$$

$$\frac{\Delta \theta_r}{\Delta \theta_\phi} = \frac{\int \Delta \Omega_r dt}{\int \Delta \Omega_\phi dt} \neq \frac{\Delta \Omega_r}{\Delta \Omega_\phi}$$

# Measurable?



- Error convolution in observable space:  $\varepsilon_{\text{los}} \sim 10 \text{ km/s}$ ,  $\varepsilon_\pi \sim \varepsilon_\mu \sim 1\%$
- Streams behave well, slope difference is still measurable for most experiments
  - frequency space more strongly affected by errors
  - **PASS** if difference between original and error-convolved slope  $< 0.005$

# Measurable with more realistic errors?

Errors now

$$\varepsilon_{\pi} \sim \varepsilon_{\mu} \sim 10\%$$

Frequency space strongly affected

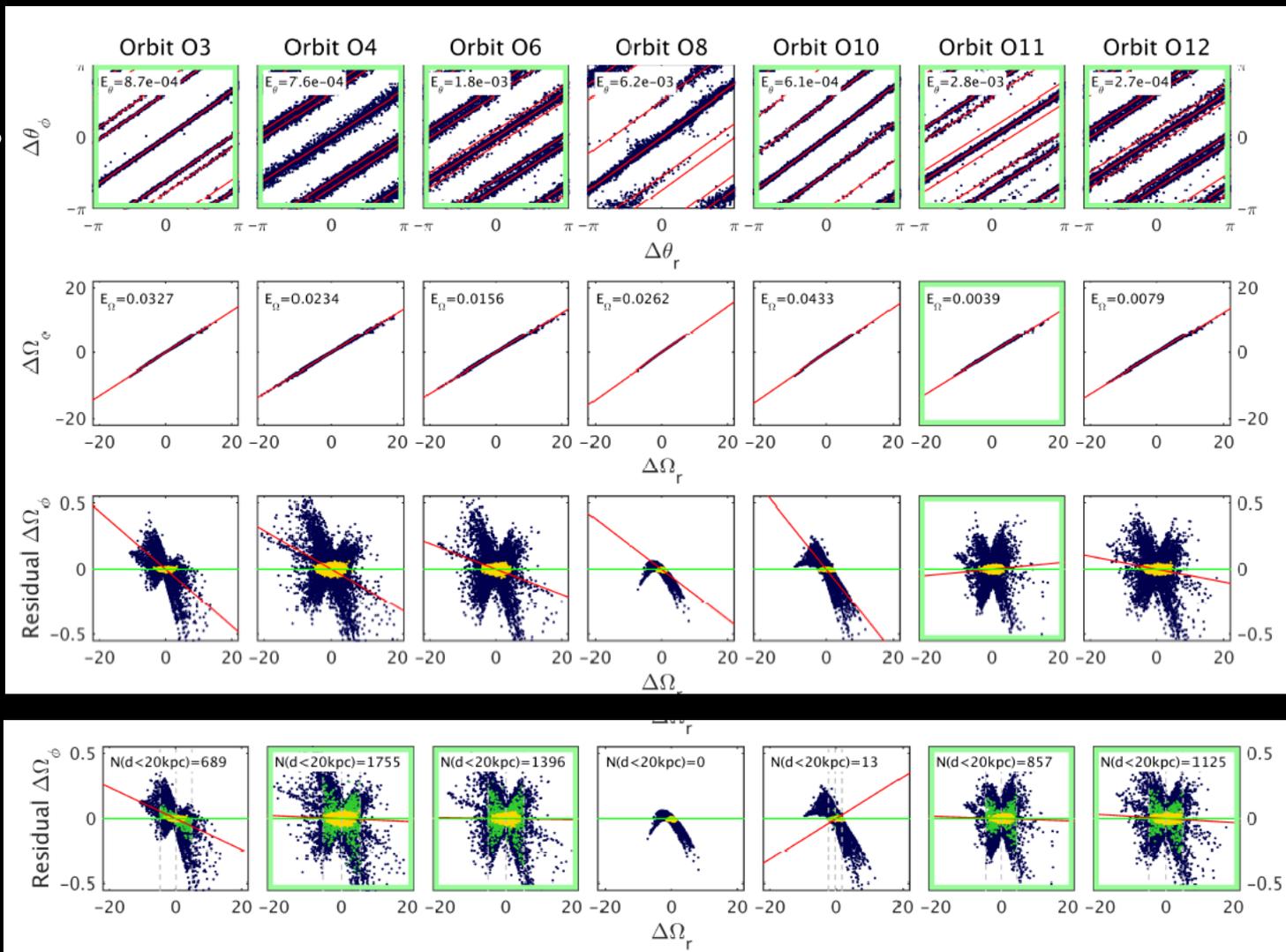
Very few streams pass

Restrict dataset

$$\varepsilon_{\pi} \sim \varepsilon_{\mu} \sim 10\%$$

$$\varepsilon_d < 2 \text{ kpc}$$

$$|\Omega_r - \langle \Omega_r \rangle| < \sigma_{\Omega}$$



More streams can be used and growth can be measured

# Summary

- Dynamics of stellar streams best understood using action-angle
  - Streams on straightlines in angle and in frequency space if true potential
  - Constrain Galactic potential parameters
  - Time-evolution imprinted in differences in straightlines slopes
  - Appear to be measurable in foreseeable future
  
- What's next
  - Finding hundreds of streams predicted by LCDM in Gaia
  - Formation of the stellar halo (in-situ vs accreted, timescales, progenitors)
  - Better understanding of signatures of subhalos on streams as ultimate test of LCDM

Thank you!

