

# Unconventional views of stellar populations

## Part II Statistical properties of stellar populations

Alberto Buzzoni  
INAF - Oss. Astronomico di Bologna, Italy

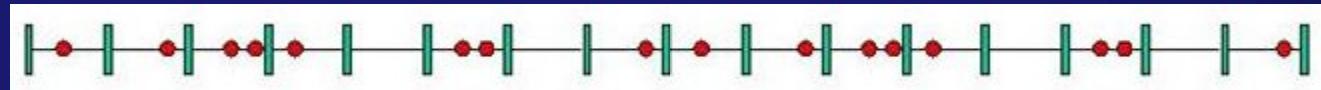
# What a Photometric Entropy theory is for?

Entropy is a measure of the intrinsic “variance” of a stellar aggregate along the different spectral range of observation.

- Surface-brightness Fluctuations
- Crowding
- Diagnostics from Narrow-band Spectroscopy

## Some Fundamentals

$$p(x) = \frac{e^{-\lambda} \lambda^x}{x!} \quad \text{for } \lambda > 0 \quad \text{and } x = 0, 1, 2, \dots$$



1, 2, 3, .....

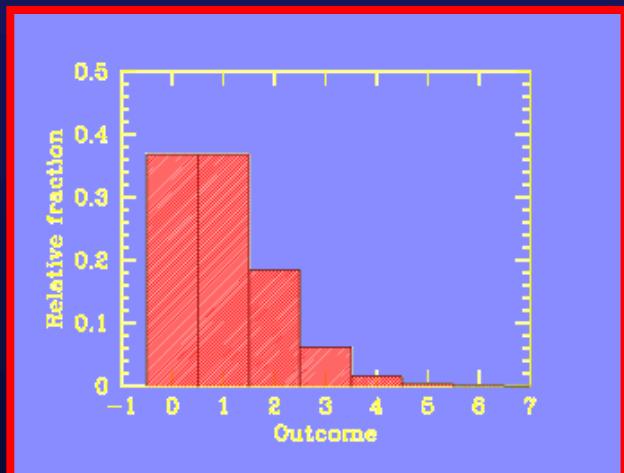
.....  $N_{\text{tot}}$

→  $N = 1 \pm 1$  for each cell

$$\sigma(N_{\text{tot}}) = \sqrt{\sum 1} = \sqrt{N_{\text{tot}}}$$

$$L_{\text{tot}} = \sum \ell_* = N_{\text{tot}} \ell_*$$

$$\sigma(L_{\text{tot}}) = \sqrt{\sum \ell_*^2} = \ell_* \sqrt{N_{\text{tot}}}$$



$$\sigma(L_{\text{tot}})/L_{\text{tot}} = 1/\sqrt{N_{\text{tot}}}$$

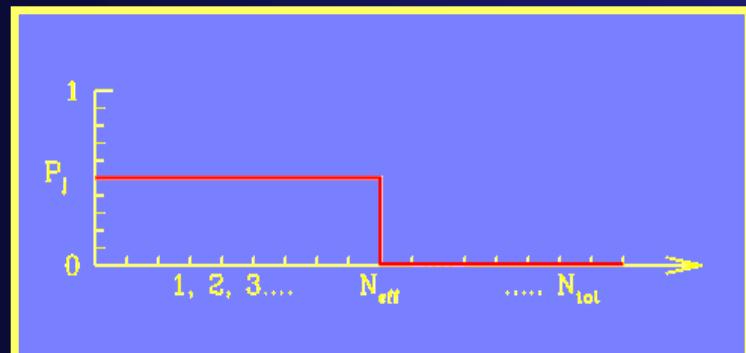
More generally, if  $\ell_*$  is NOT a constant, we can still define

$$\sigma(L_{\text{tot}})/L_{\text{tot}} = 1/\sqrt{N_{\text{eff}}}$$

where, always,

$$N_{\text{eff}} \leq N_{\text{tot}}$$

→  $N_{\text{eff}}$  will depend on  $\lambda$  as  $\ell_*$  depends on  $\lambda$



$$S = \text{Log} (N_{\text{eff}}/N_{\text{tot}})$$

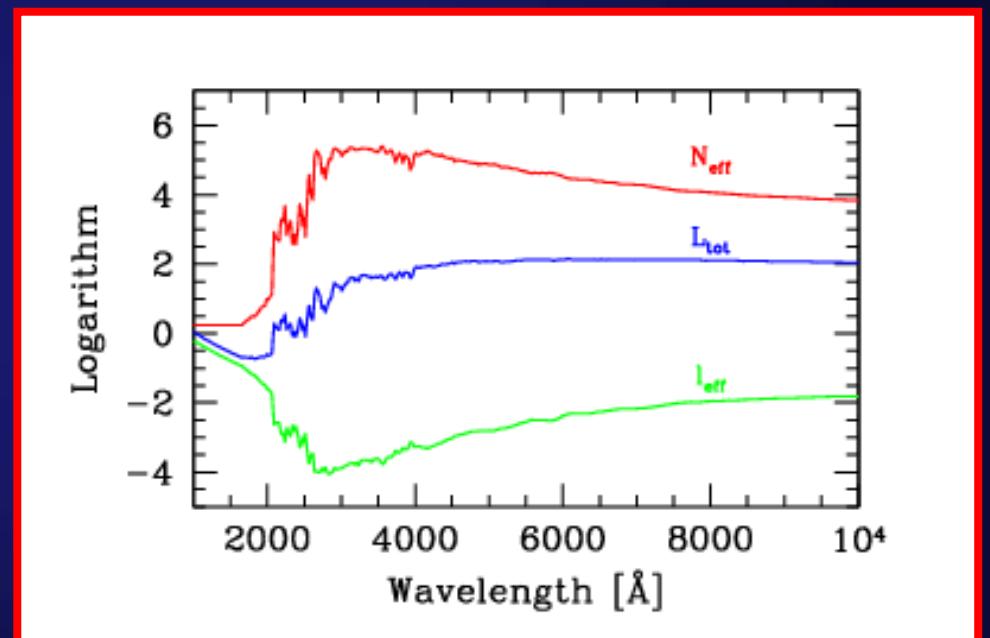
Quite importantly,  $S = S(\lambda)$

In order to fix  $N_{\text{eff}}$  (and Entropy)  
we need a photometric argument:

$$\sigma^2(L_{\text{tot}}) / L_{\text{tot}} = \sum \ell_*^2 / \sum \ell_* = \ell_{\text{eff}}$$

At every  $\lambda$ , it must be:

$$N_{\text{eff}} \times \ell_{\text{eff}} = L_{\text{tot}}$$



Buzzoni (1993), A&Ap, 275, 433

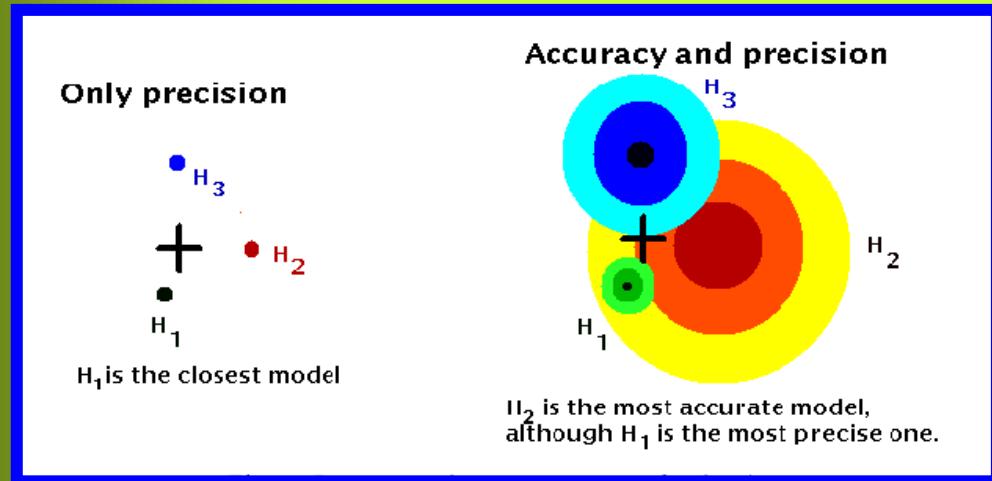
Buzzoni (2005), Astro-ph/0509602

Cerviño et al. (2002), A&Ap, 381, 51

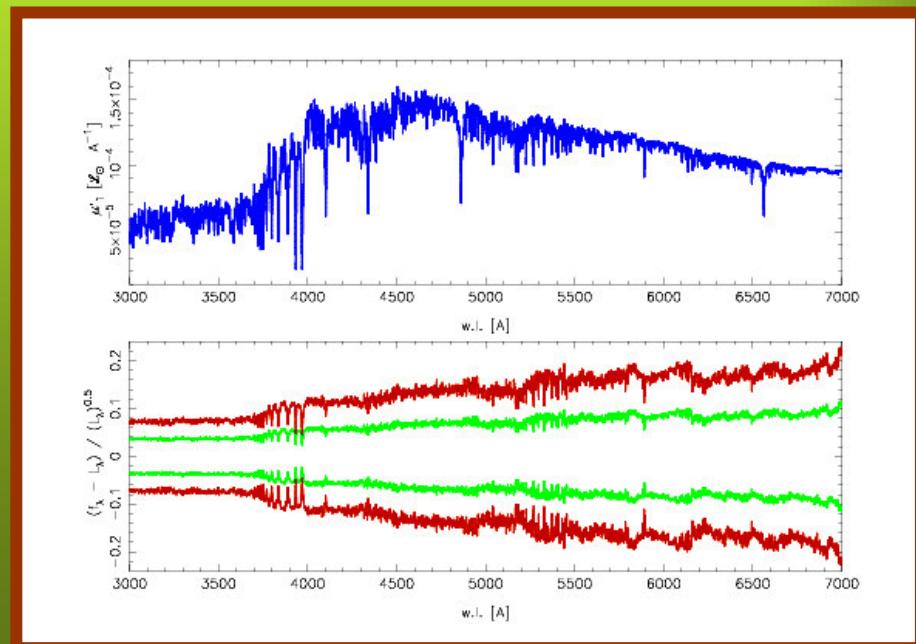
Cerviño & Luridiana (2007), Astro-ph/0711.1355

Buzzoni (1993)

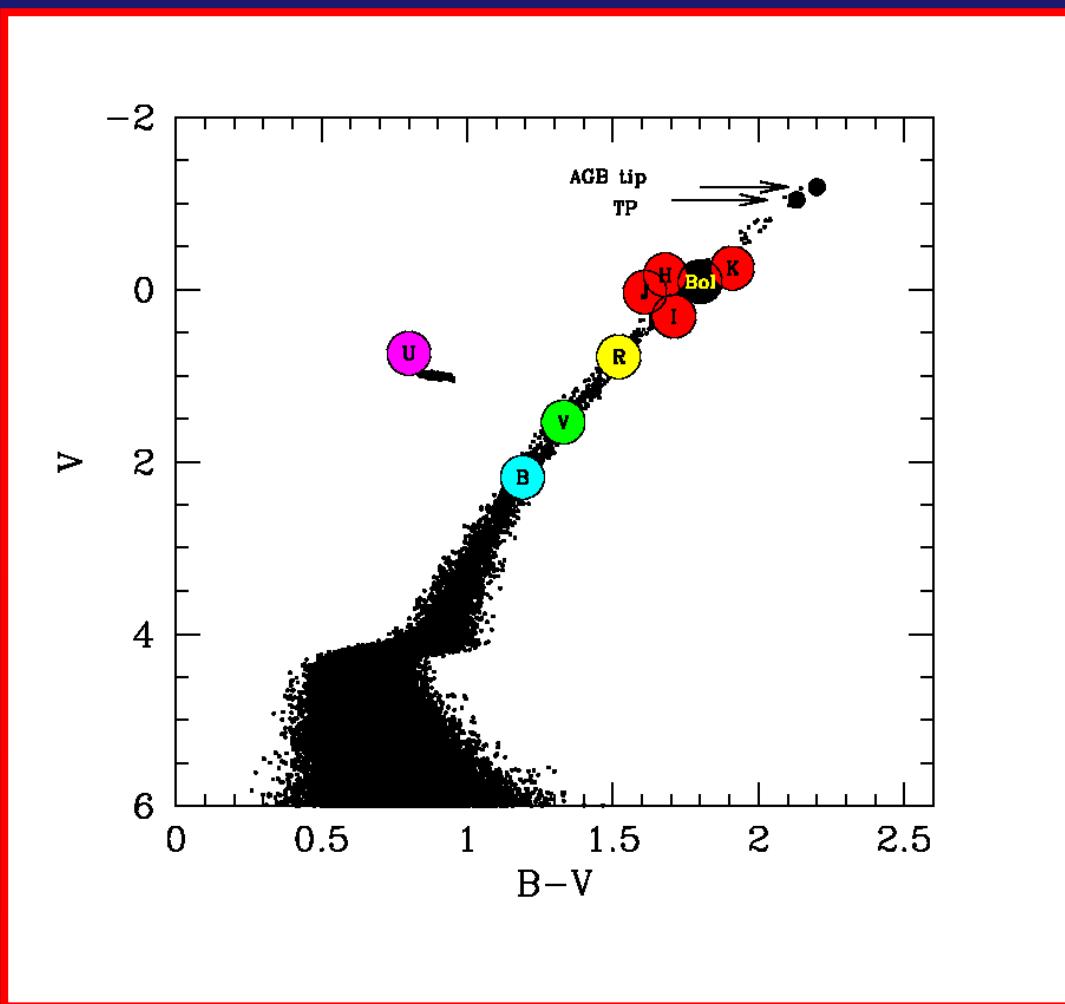
# Accuracy vs. Precision



Cerviño & Luridiana (2007)



# Brightness fluctuations & stellar “barycenter”



Buzzoni & González-Lópezlira (2008)

# Surface-Brightness Fluctuations: an Alternative Approach for the Case of M53



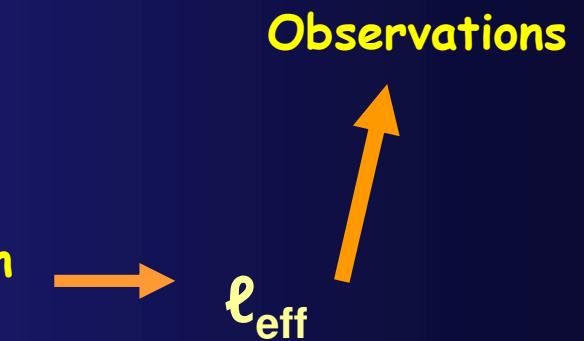
2.12m @Cananea (Mexico)  
6.5'x10' LFOSC (R band)

3141.8	3201.5
2885.5	3323.3

First application of the theory to  
galx's: Tonry & Schneider (1988)  
and Tonry (1991)

$$\sigma^2(L_{\text{tot}}) / L_{\text{tot}} = \sum \ell_*^2 / \sum \ell_* = \ell_{\text{eff}}$$

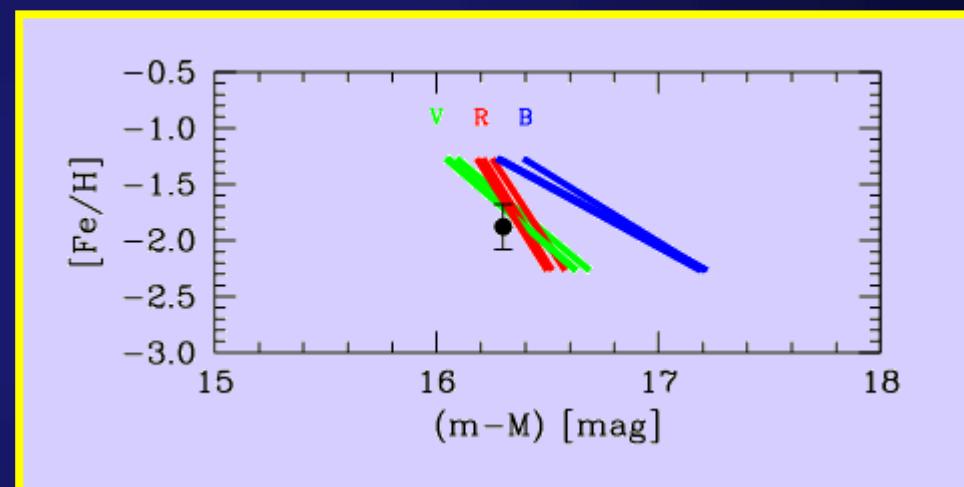
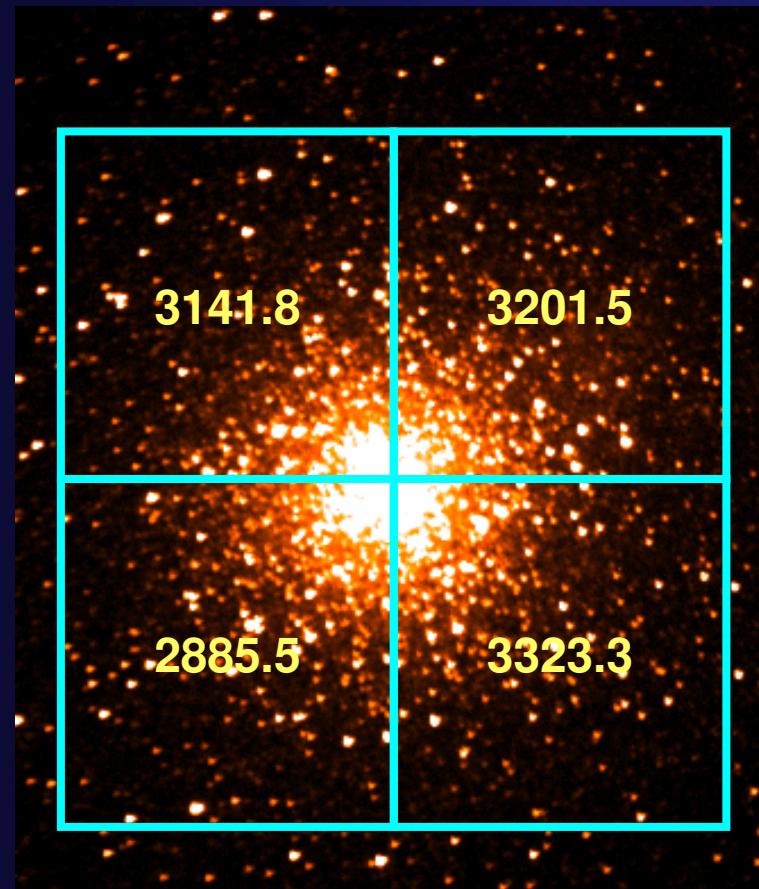
Theory: Population  
synthesis models



$$L_{(\text{quad})} = 3138 \pm 184$$

# Surface-Brightness Fluctuations: an Alternative Approach for the Case of M53

M 53 (NGC 5024)

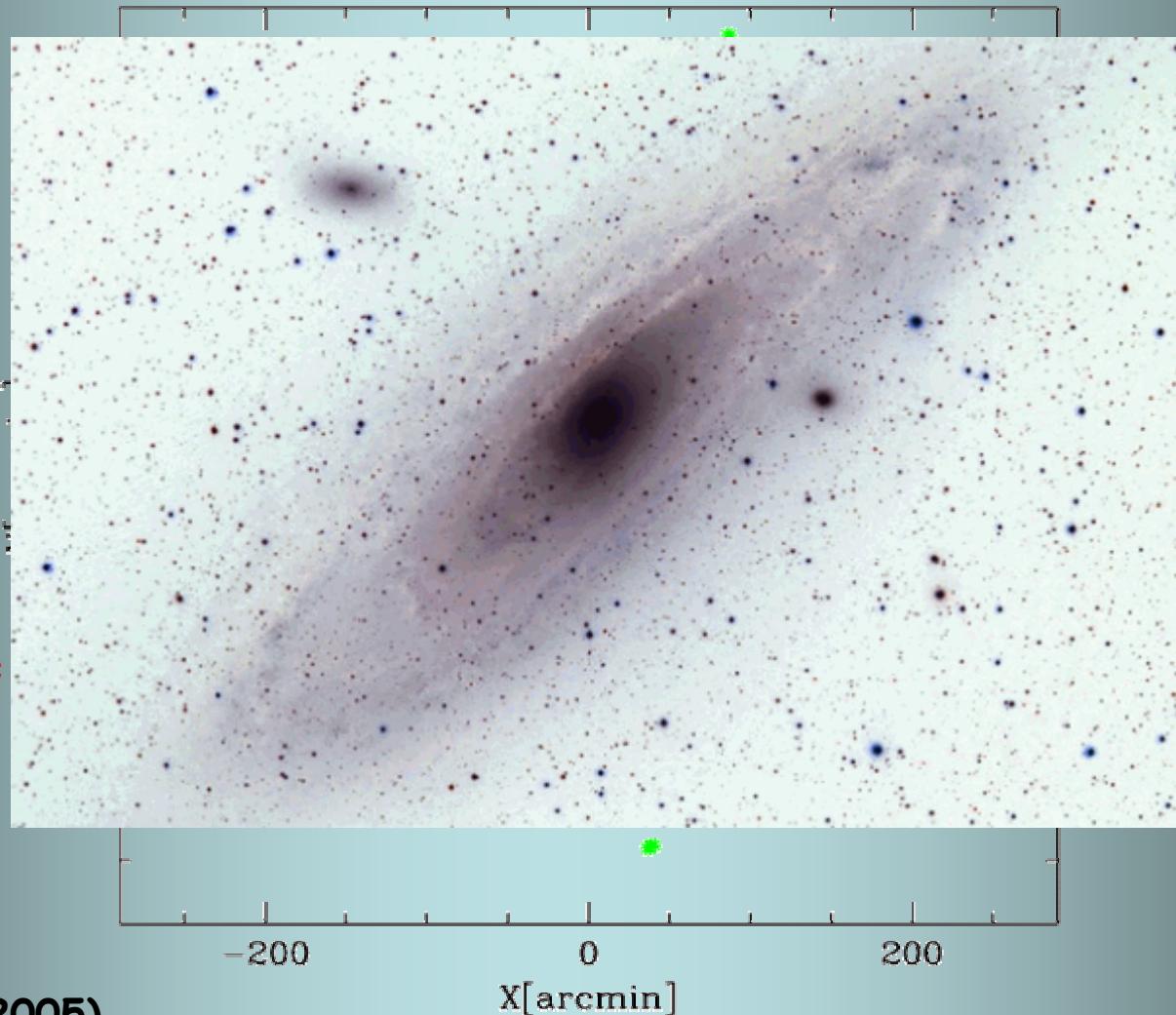


$[\text{Fe}/\text{H}] = -1.88 \pm 0.2 \text{ dex}$  (Santos & Piatti, 2004)

$(m-M) = 16.3 \text{ mag}$  (Harris 1996)

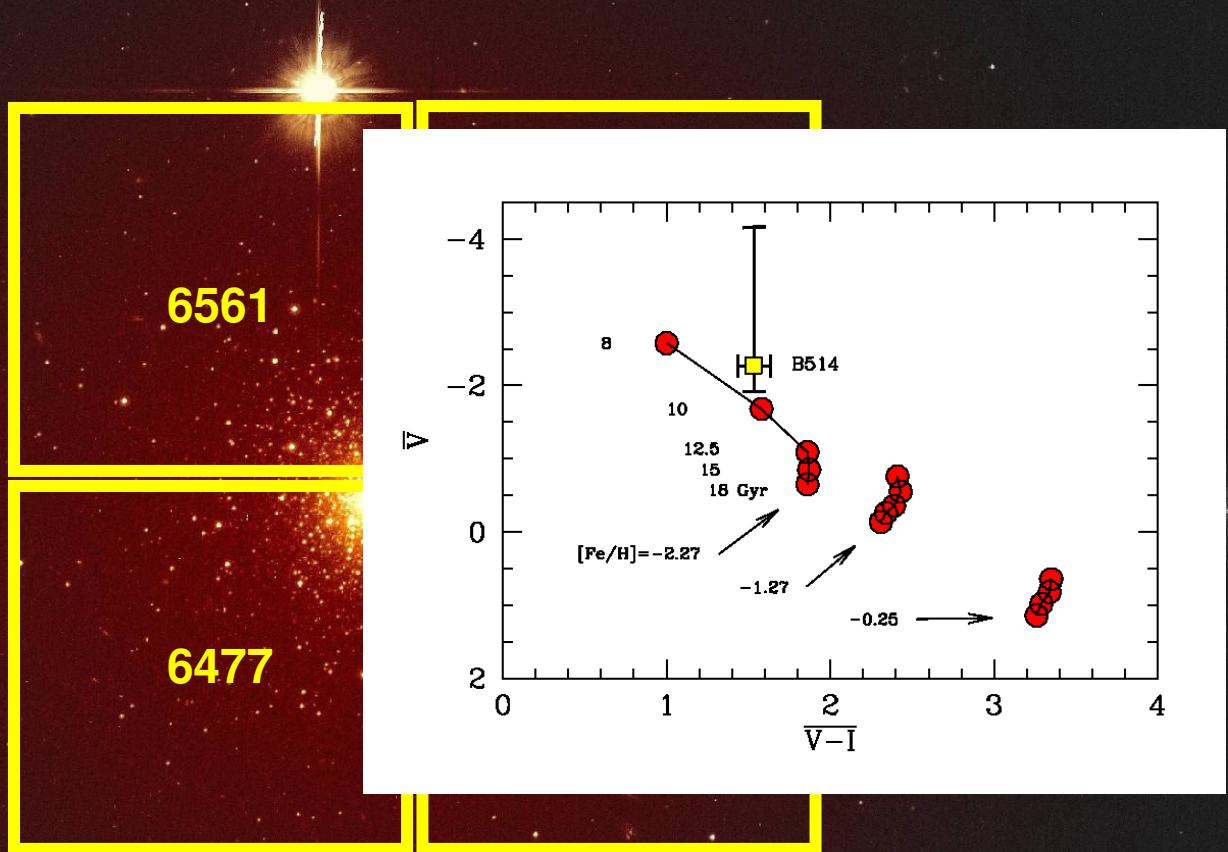
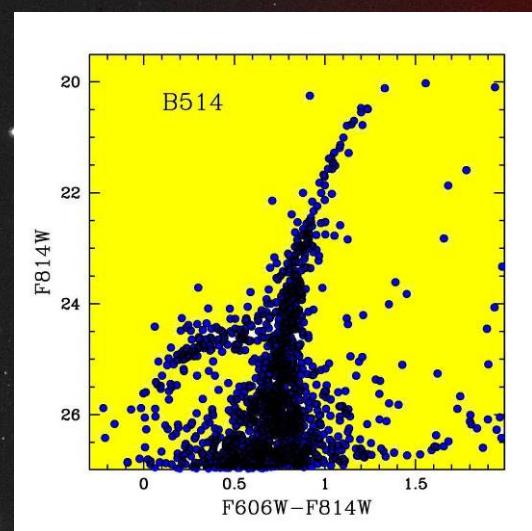
$L_{(\text{quad})} = 3138 \pm 184$

# Far, far away...(around M31)



Galleti et al. (2005)

# B514 - the farthest globular cluster of M31



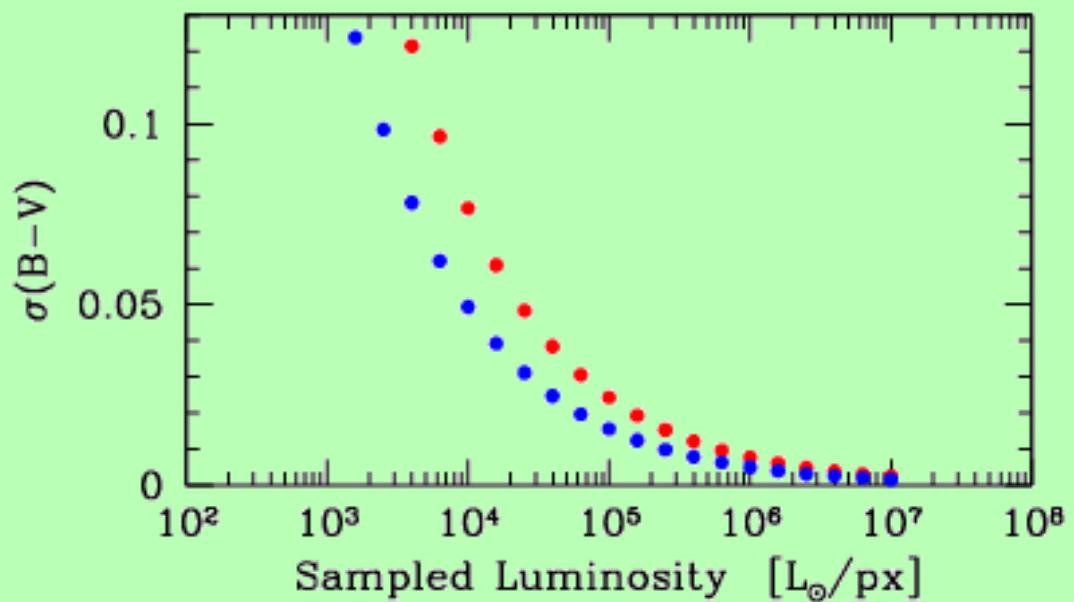
$$\sigma^2(L_{\text{tot}}) / L_{\text{tot}} = 507.8^2 / 6128.5 = \ell_{\text{eff}}$$

Galleti et al. (2006)

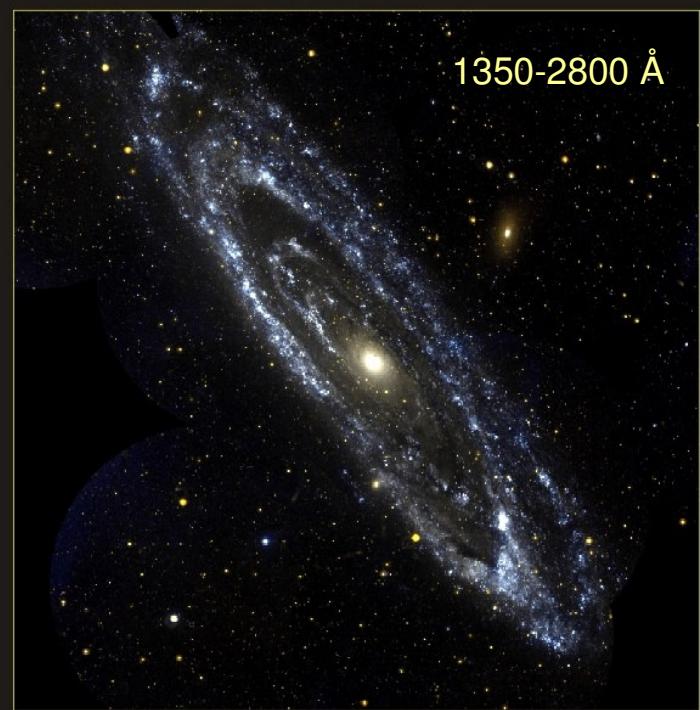
# Luminosity Sampling and Intrinsic Color Fluctuations

$$\Delta\text{mag} = \sigma(L_{\text{tot}})/L_{\text{tot}} = 1/\sqrt{N_{\text{eff}}}$$

$$\sigma(B-V) = [\sigma(B)^2 + \sigma(V)^2]^{1/2} = (1/N_{\text{eff}}^B + 1/N_{\text{eff}}^V)^{1/2}$$



# Crowd!



Andromeda Galaxy  
GALEX

Thilker et al. (2005)

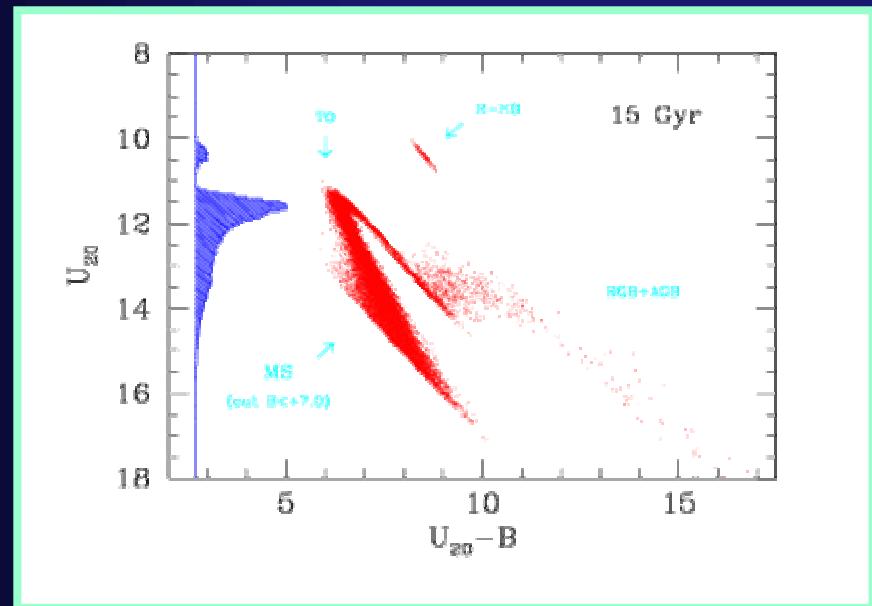


Andromeda Galaxy  
Visible light image (John Gleason)

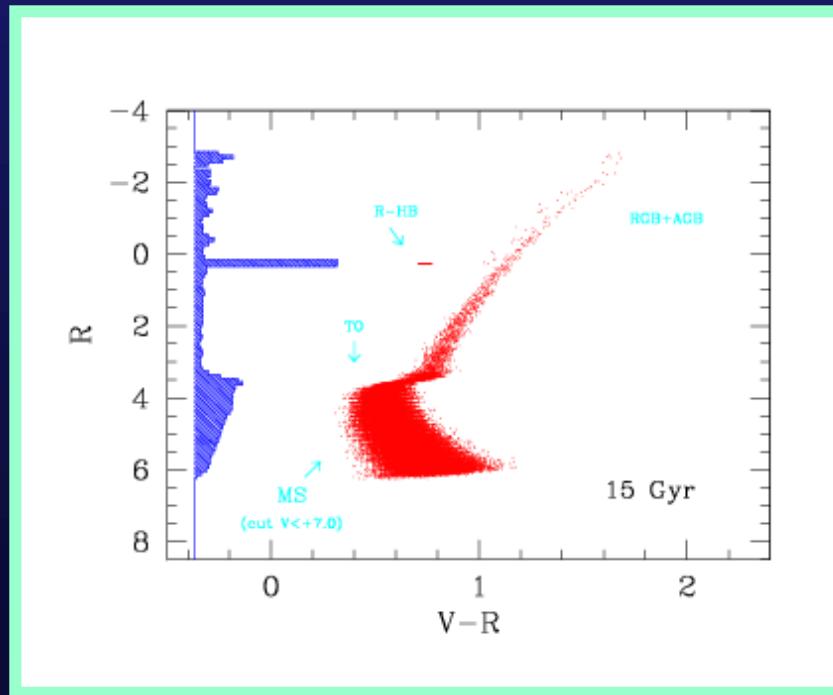
Credits: Flickr.com

# Oligarchy vs. Democracy

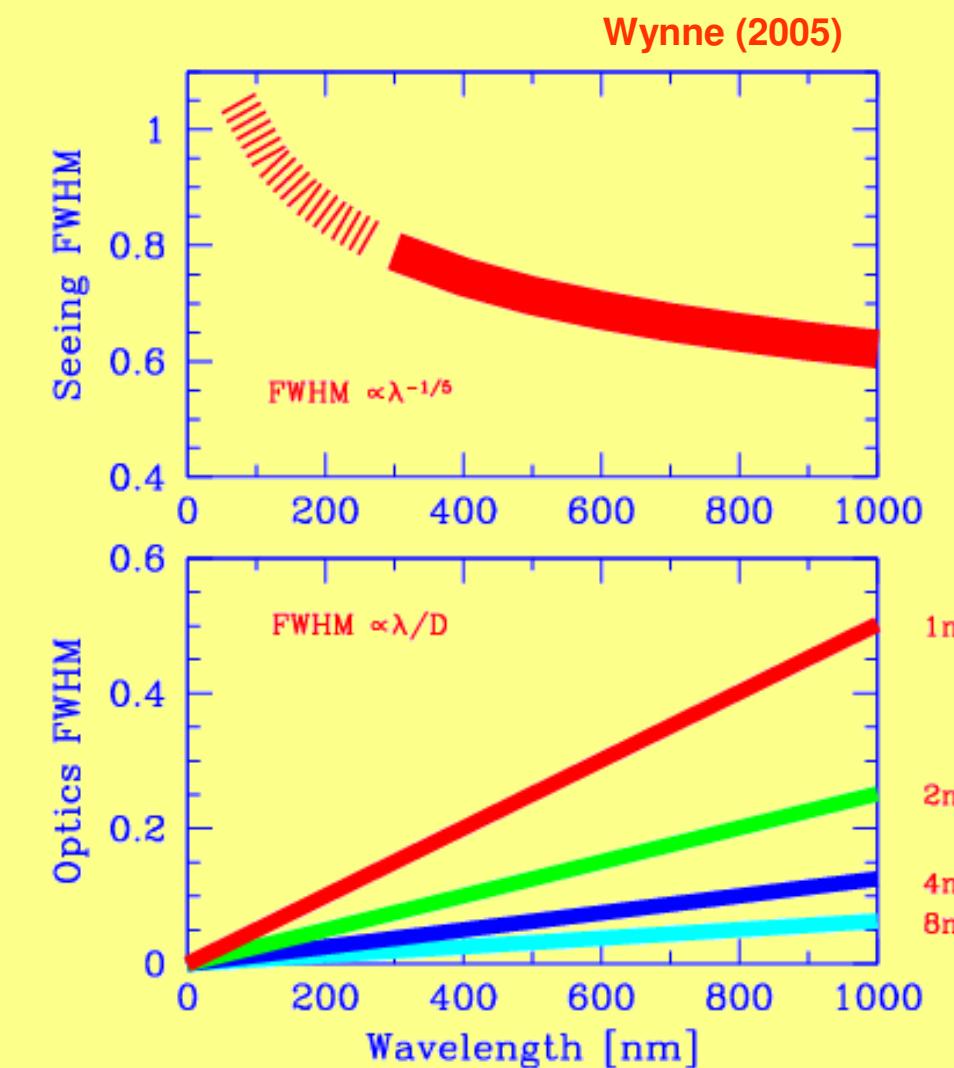
2000 Angstroms



7000 Angstroms



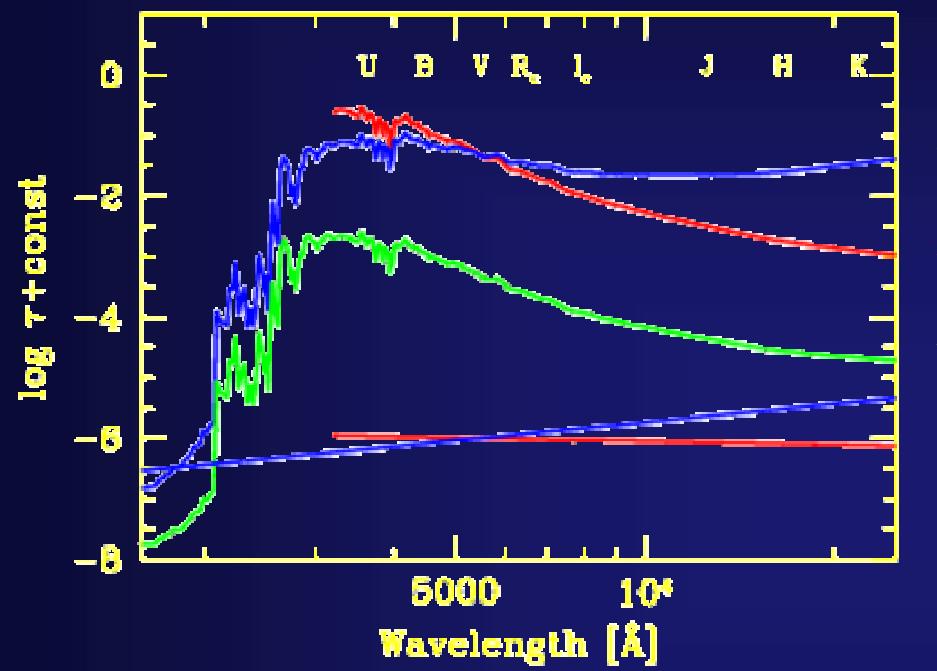
Buzzoni (2002)



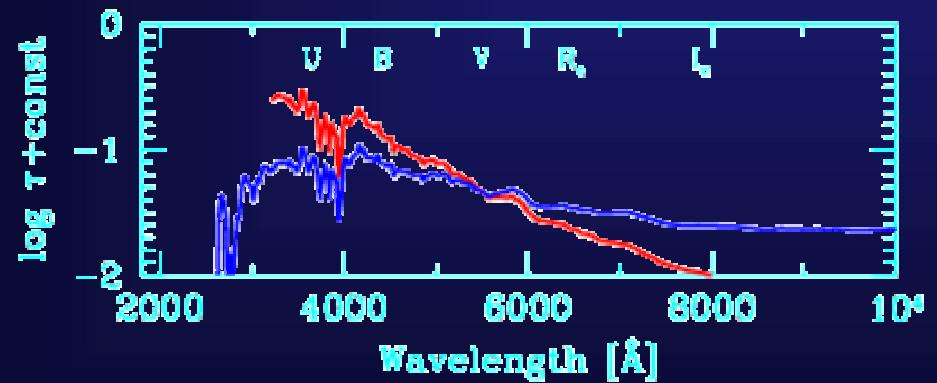
Seeing

Diffraction

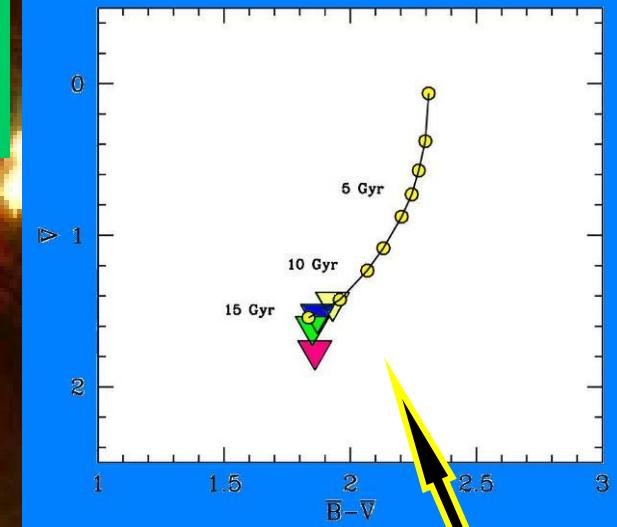
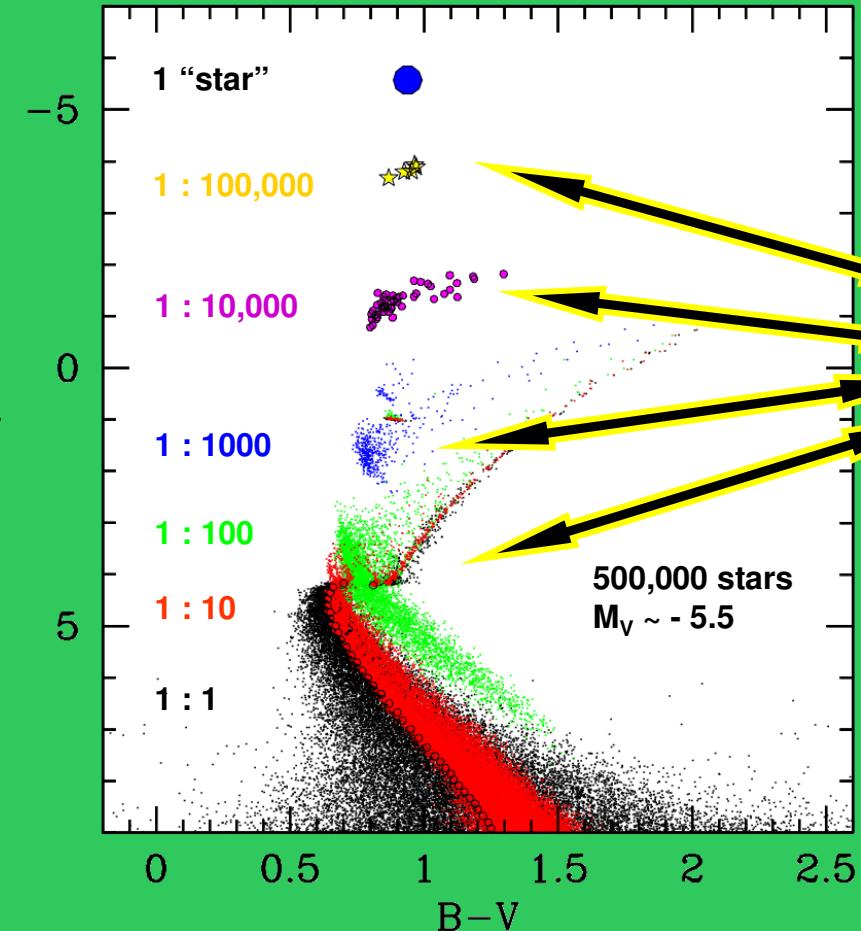
# Crowding & Opacity



- ← from Space
- ← from Ground
- ← Entropy ( $N_{\text{eff}}$ )
- ← Telescope Diffraction
- ← Seeing



# Crowding, photometric entropy & surface-brightness fluctuations



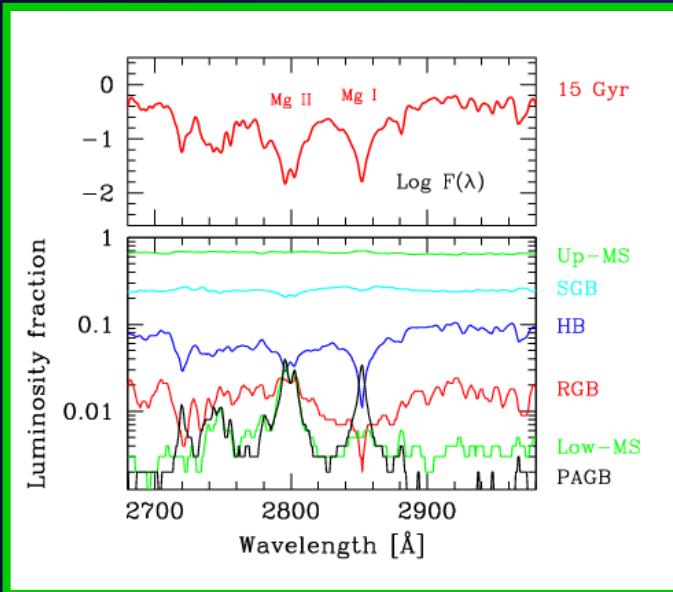
$$\sigma(L_{\text{tot}})/L_{\text{tot}} = 1/\sqrt{N_{\text{eff}}}$$

$$S = \log(N_{\text{eff}}/N_{\text{tot}})$$

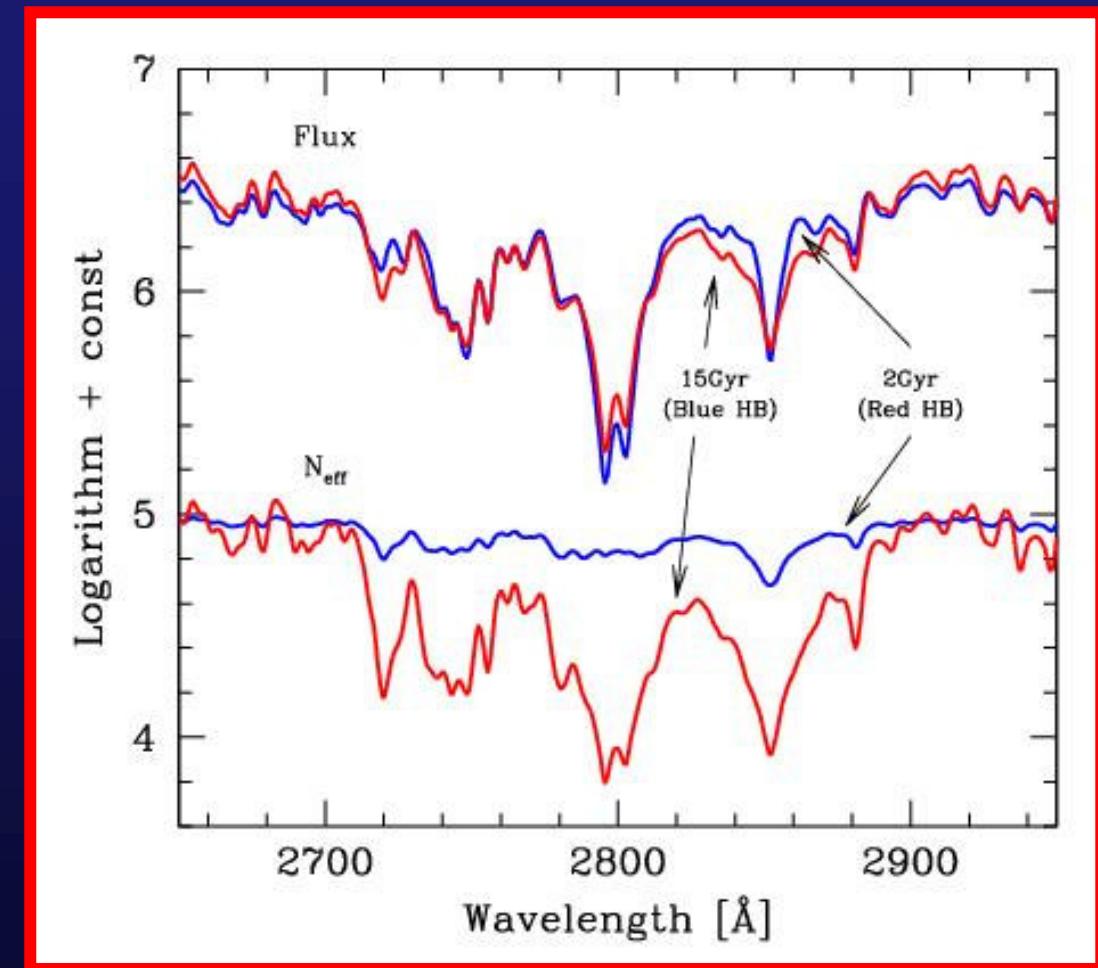
$$\sigma^2(L_{\text{tot}})/L_{\text{tot}} = \sum \ell_*^2 / \sum \ell_* = \ell_{\text{eff}}$$

$$N_{\text{eff}} \times \ell_{\text{eff}} = L_{\text{tot}}$$

# An illustrative example: the 2800 Å Mg feature



Buzzoni (2008)



The End (Part II)