

# Unconventional views of stellar populations



## Part I Fundamentals of stellar population synthesis

Alberto Buzzoni  
INAF - Oss. Astronomico di Bologna, Italy

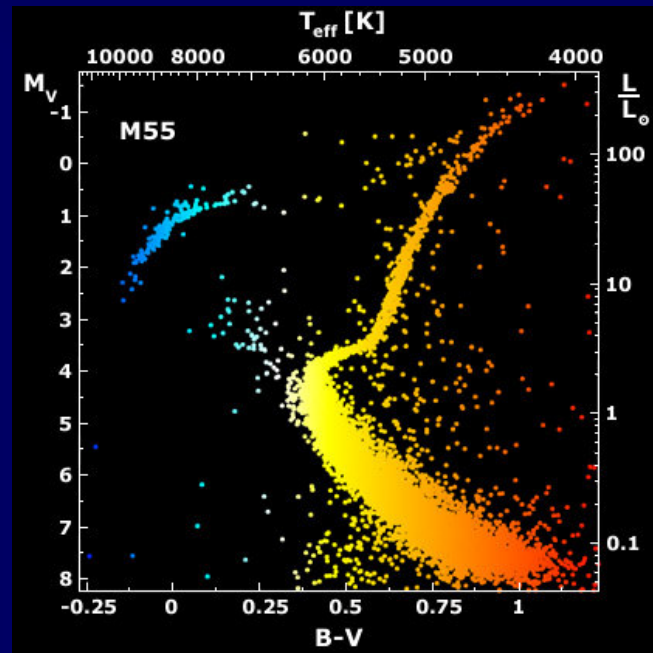
# Star Trackers



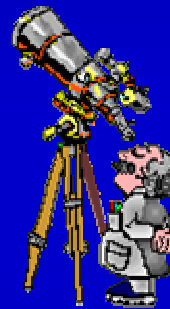
**Ejnar Hertzsprung**  
**Denmark (1873-1957)**



**Henry Norris Russell**  
**USA (1877-1957)**



# From stars to star clusters



← Psychology  
Sociology →



# The "Color-Luminosity Array" (1915)

TABLE 2  
COLOR LUMINOSITY ARRAY IN MESSIER 13

Limits of Photovisual Magnitude	b0 to b5	b5 to a0	a0 to a5	a5 to f0	f0 to f5	f5 to g0	g0 to g5	g5 to k0	k0 to k5	k5 to m0	All Colors
11.80-.99											6
12.00-.19								1	3	2	2
.20-.39									1	1	5
.40-.59								3	2		5
.60-.79				1	1		1	2			5
.80-.99							4	2			6
13.00-.19	1					1	8	6			13
.20-.39						1	4	2	1		8
.40-.59						1	6	1			8
.60-.79						2	3	1		1	7
.80-.99		3		2	8	14	5	2			33
14.00-.19			1		1	9	3	2			15
.20-.39			1			10	13	4			28
.40-.59		1	1	7	3	24	16	4			56
.60-.79			6	2	1	6	12	1	1		29
.80-.99		5	3		2	5	8	2			25
15.00-.19		24	9	3	3	19	10	2			70
.20-.39	10	21	7	5	12	28	15				98
.40-.59	4	11	6	4	11	11	5	1	1		54
.60-.79	1	5	3	3	10	4	1				27
.80-.99											
Total	16	70	36	27	50	135	115	33	9	4	495

evidence that the giant red stars were much brighter than the giant blue stars in the globular cluster Messier 13, that attention was called at once to the contrast between this color-luminosity diagram and the one



**Harlow Shapley**  
**USA (1885-1972)**

(1930)

manent in spectral composition. Is this because the time units we use in measuring stellar evolution are still too anthropocentric, or because the clusters are timeless?



5 October 1956, Volume 124, Number 3223

# SCIENCE

## Origin of the Elements in Stars

F. Hoyle, William A. Fowler,  
G. R. Burbidge, E. M. Burbidge

Experimental (1, 1a) and observational (2-6) evidence has continued to accumulate in recent years in support of the theory (7-10) that the elements have been and are still being synthesized in stars. Since the appearance of a new and remarkable analysis by Suess and Urey (11) of the abundances of the elements, we have found it possible to explain, in a general way, the abundances of practically all the isotopes of the elements from hydrogen through uranium by synthesis in stars and supernovae. In this article we wish to outline in a qualitative fashion the essentially separate mechanisms which are required in stellar synthesis (12).

### Thermal Conversion of Pure Hydrogen through Helium to Iron

As long as extremely high temperatures in excess of  $5 \times 10^8$  degrees Kelvin are not under consideration, the general tendency of nuclear reactions inside stars is to increase the average binding energy per nucleon. For a given temperature and density and for a given time scale of op-

in some cases by resonance penetration. Since barrier effects become less severe as the temperature increases, it follows that the binding energies increase with temperature. This will become clear from the following examples.

At temperatures from about  $10^7$  to  $5 \times 10^7$  degrees in main-sequence stars, hydrogen is transformed to helium,  $4\text{H}^1 \rightarrow \text{He}^4$ , with an average binding energy of 7.07 million electron volts (Mev) per nucleon. We emphasize that the proton-proton sequence of reactions makes possible the production of helium starting only with hydrogen. The recent discovery of the free neutrino as reported by Cowan *et al.* (1a) leads to increased confidence in the existence of the primary proton-proton interaction which proceeds through prompt electron-neutrino emission. At temperatures from  $10^8$  to  $2 \times 10^8$  degrees in red giant stars,  $\text{He}^4$  is transformed principally to  $\text{C}^{12}$ ,  $\text{O}^{16}$ , and  $\text{Ne}^{20}$  with an average binding energy of 7.98 Mev per nucleon. The important roles of the ground state of  $\text{Be}^9$  and of the second excited state of  $\text{C}^{12}$  in expediting the primary process of helium fusion,  $3\text{He}^4 \rightarrow \text{C}^{12}$ , have recently been

appreciably greater atomic weight than  $\text{Fe}^{56}$ .

The situation, then, is that a thermal "cooking" of pure hydrogen yields principally  $\text{He}^4$  and the  $\alpha$ -particle nuclei with  $A = 4n$ ,  $Z = 2n$ ,  $n = 3, 4, 5, 6, 7, 8, 9$ , and 10 ( $\text{C}^{12}$  to  $\text{Ca}^{40}$ ), to be centered around  $\text{Fe}^{56}$ , the most abundant nuclei. More abundances that have been observed for these nuclei, and particularly the 20-odd isotopes of the iron-group elements, chromium, manganese, nickel, show good agreement with the abundances calculated by the statistical theory. The abundances have been considerably improved by taking into account the low-lying excited states of the iron-group nuclei and the active nuclei which undergo  $\beta$ -decay to them, and by statistical calculations according to the state of the nucleus that is expected on nucleosynthesis. Typical results for the abundances of the chromium and iron group at  $3.8 \times 10^8$  degrees are in good agreement with the observed abundances.

We regard results similar to those presented in Table 1 as giving support to the view that the elements were synthesized in stars and that they became distributed in space, either from late-type giants or from explosion, as for instance in the case of the

### Thermal Reactions of Hydrogen and Helium with Lighter Elements

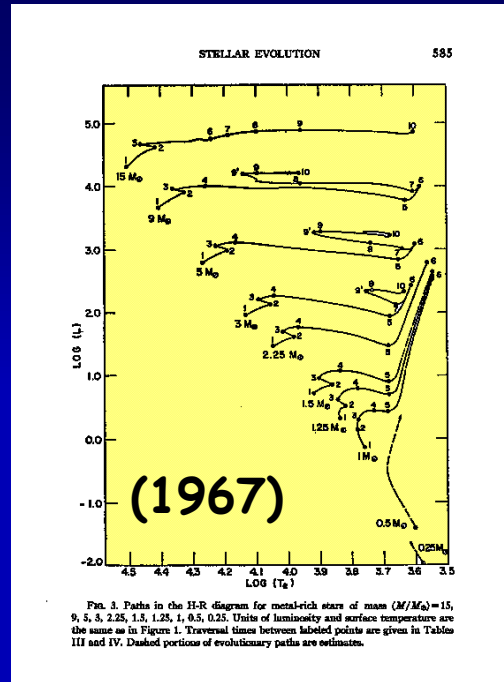
More complicated effects arise when the thermal cooking is considered, not of completely pure hydrogen, but of hydrogen adulterated with a small proportion of the elements mentioned in the previous paragraphs. When a second-generation

B<sup>2</sup>FH (1956)



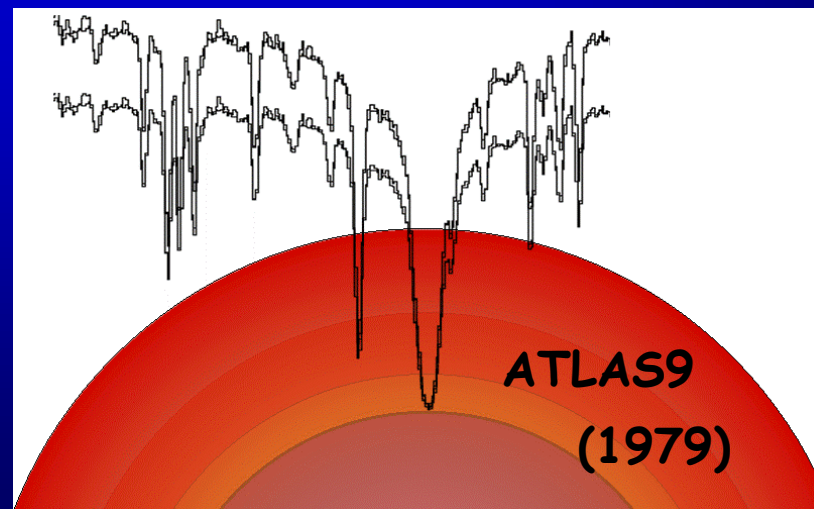
Scanned at the American Institute of Physics

# Star builders



Icko Iben USA (1931- )

Robert L. Kurucz USA (1946- )



# Star synthesizers



Beatrice M. Tinsley  
New Zealand/USA  
(1941-1981)



Sandra M. Faber (USA)



'90

Leitherer (et al.), 1999  
Maraston, 1998, 03, 05  
Granato & Silva, 1998  
Vazdekis (et al.), 1997, 99, 01, 03  
Poggianti (et al.), 1996, 97, 03  
Bressan & Chiosi (et al.), 1994, 96  
Worthey, 1994  
Fritze v. Alvensleben (et al.), 1992, 95, 99  
Brocato (et al.), 1990

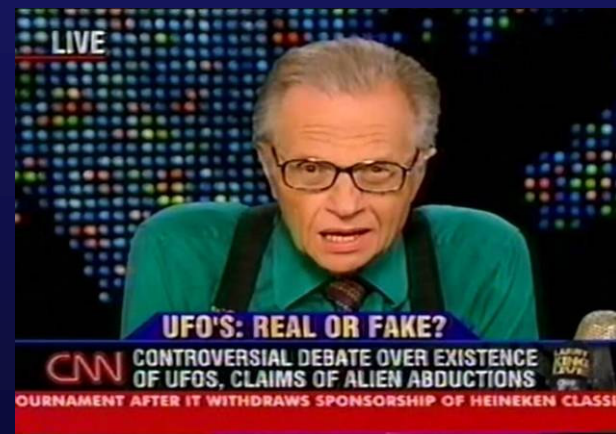
'80

Barbaro & Olivi, 1989  
Buzzoni, 1989, 95, 02, 05  
Bica (et al.), 1988, 90  
Rocca-Volmerange (et al.), 1988, 97  
Arimoto & Yoshii, 1986, 87  
Pickles, 1985  
Bruzual (& Charlot), 1983, 93, 03, 07

'70

Tinsley (et al.), 1976, 78  
O'Connell, 1976, 80  
Faber, 1972  
Spinrad & Taylor, 1969, 71

## Most popular synthesis codes (→ 2008)





# The synthesis approach...

$$F(\lambda) = \int^* f(\lambda)_{T,L} [\text{HR diagram}]_{T,L}$$

Input



Output

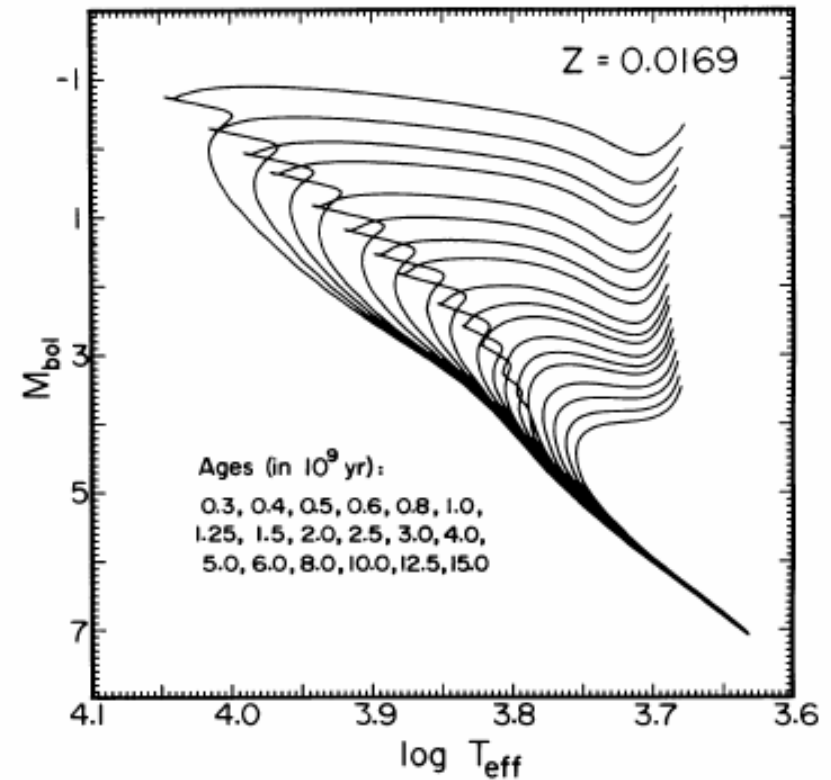
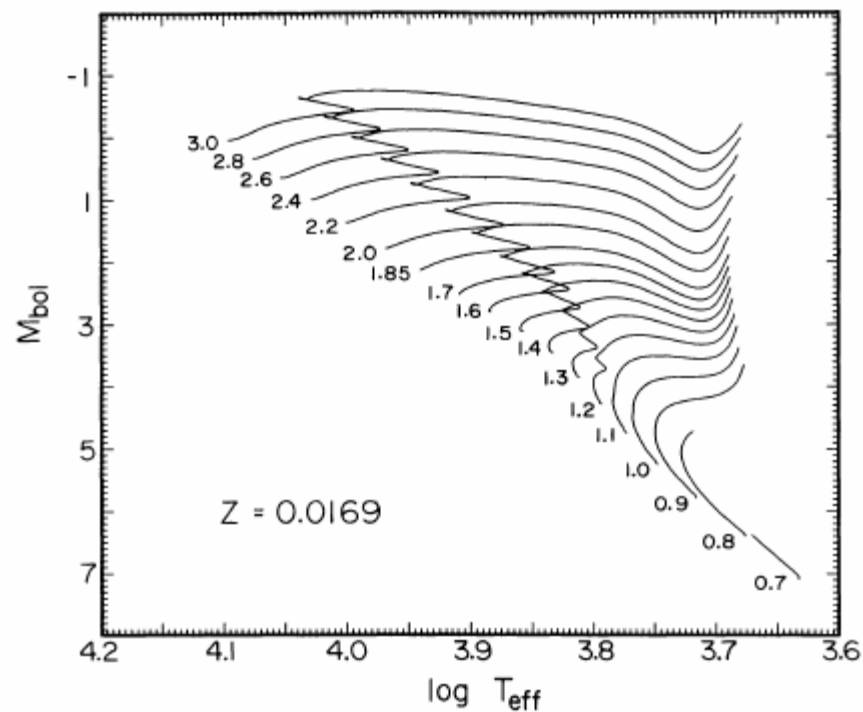
Output



Input

# Stellar tracks & Isochrones

Vandenbergh (1985)



## A Simple Stellar Population (SSP) is...

- Any coeval sample of stars
- With fixed distinctive properties (other than stellar mass)
- Its c-m diagram can be described theoretically by an isochrone

Composite Stellar  
Populations (CSPs)

$$\text{CSP}(t) = \int_0^t \text{SSP}(\tau) \otimes \text{SFR}(t - \tau) d\tau$$

# Evolutionary regimes

High-mass stars ( $M > 7 M_{\text{sun}}$ ):

End up as SN II

Intermediate-mass stars  
( $2 < M < 7 M_{\text{sun}}$ ):

Helium ignites in a non-  
degenerate core

No HB (blue loops) No AGB

Nucleosynthesis up to C-O

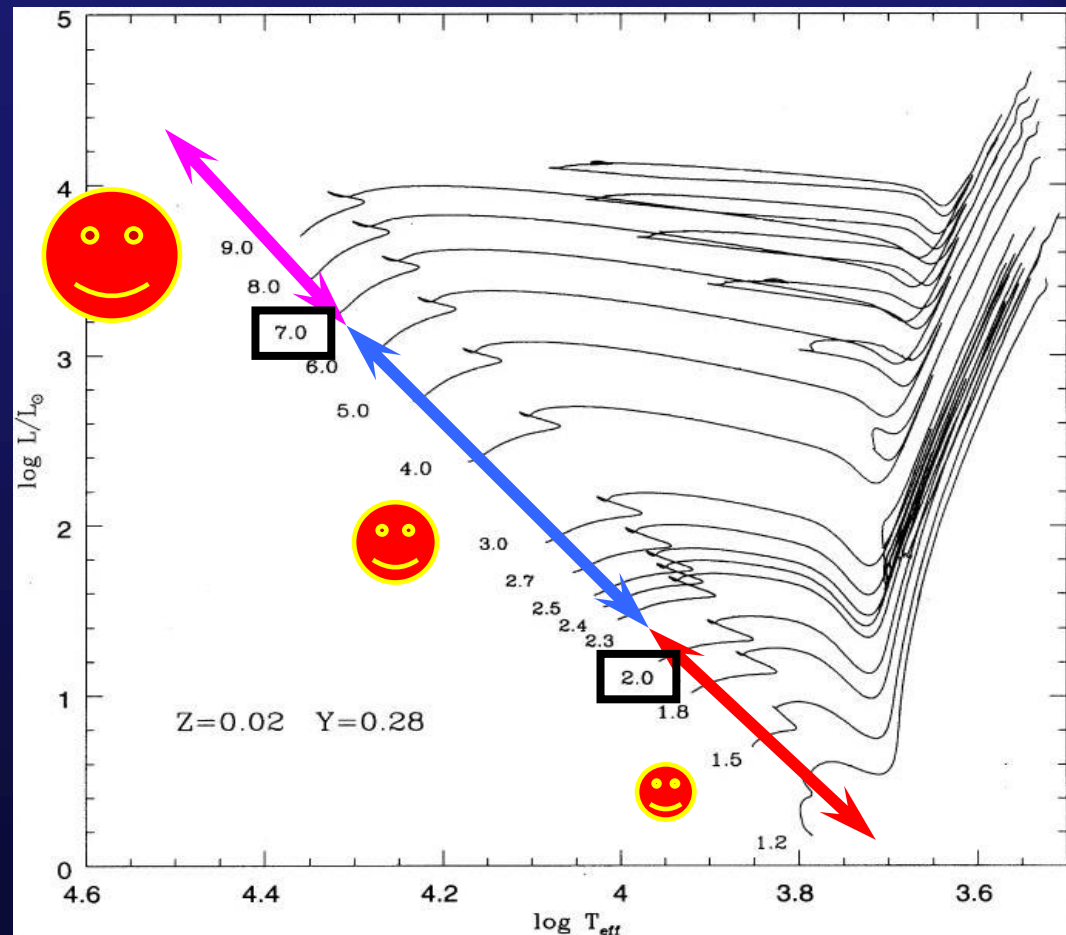
Low-mass stars ( $M < 2 M_{\text{sun}}$ ):

Helium ignites in a degenerate  
core (He flash)

Full HB - Full AGB

Nucleosynthesis up to C

Dominguez, Chieffi, Limongi, & Straniero (1999)





# The Fuel Consumption Theorem

Renzini & Buzzoni (1986)

Post-MS luminosity contribution:  $L = \int \ell_* N(M) dM$

IMF  $\rightarrow N(M) dM = A M^{-s} dM$

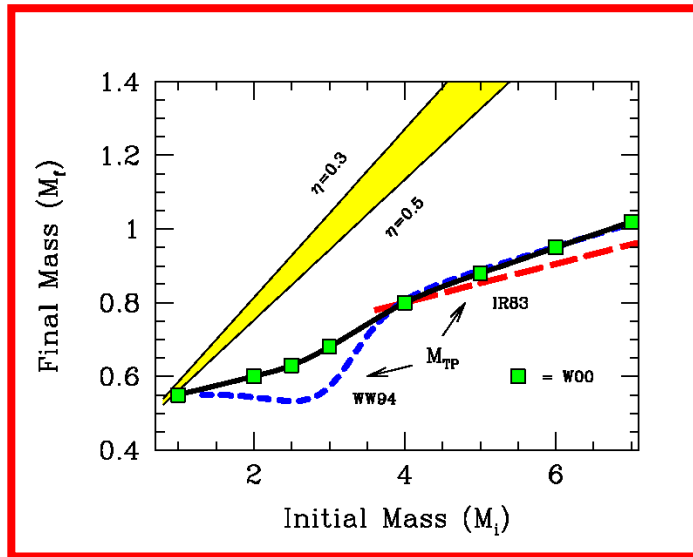
$$L_{PMS} = \int \ell_* [A M^{-s}_{TO} dM/dt] d\tau$$

$A \rightarrow M_{tot}$        $L_{PMS} = A M^{-s}_{TO} dM/dt \int \ell_* d\tau$

Evolutionary flux (b) ↑

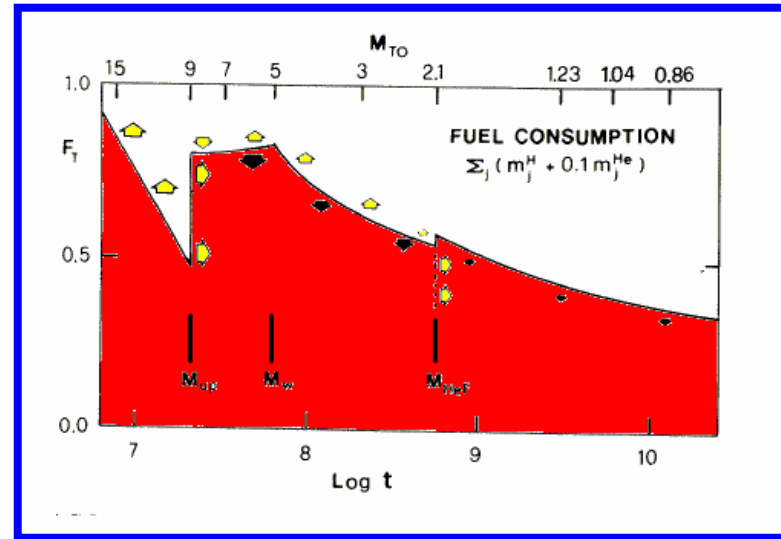
$L_{PMS} / L_{TOT} = B \text{ Fuel}$  ↑

$B = b/L_{TOT}$  (Specific evolutionary flux)



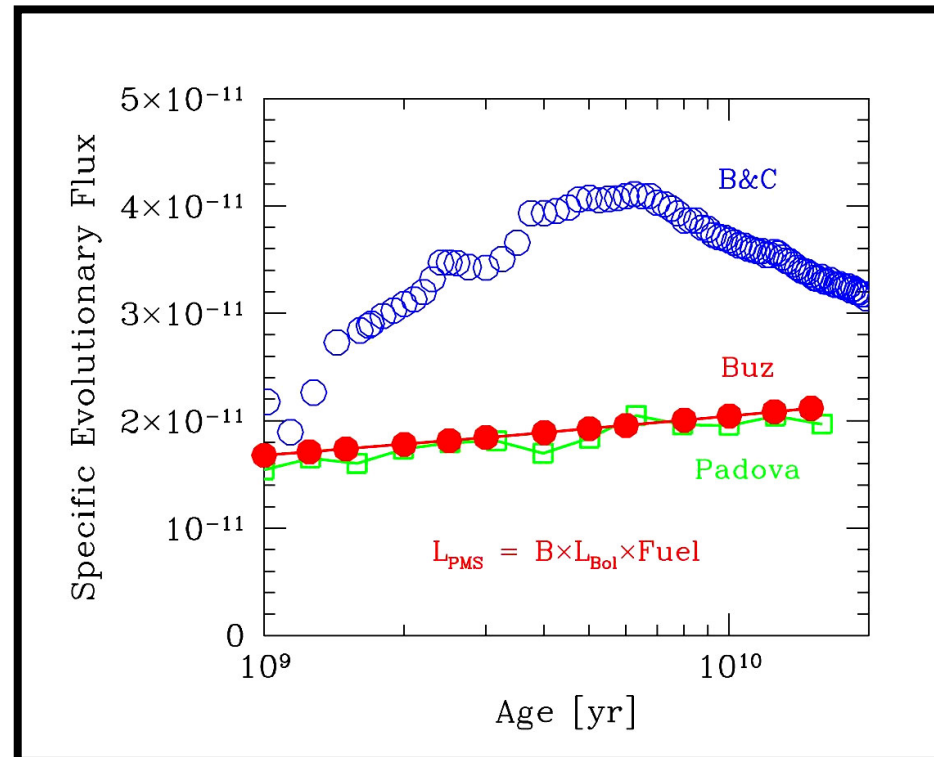
Buzzoni, Arnaboldi & Corradi (2006)

**Clock, Fuel...**  
**& Energy**  
**conservation!...**




**Fuel**

**B**



...a straightforward consequence on  
number counts....

$$N_{\text{PMS}} = AM^{-s} dM = \left[ AM_{\text{TO}}^{-s} \frac{dM_{\text{TO}}}{dt} \right] \tau = b \times \tau$$

$$N_{\text{PMS}} = \left[ \frac{AM_{\text{TO}}^{-s} \frac{dM_{\text{TO}}}{dt}}{L_{\text{TOT}}} \right] L_{\text{TOT}} \tau = B \times L_{\text{TOT}} \times \tau$$


$$1.7 (\pm 0.3) 10^{-11} \quad (\text{Buzzoni 1989})$$

$$\frac{dt}{t} \approx -2.5 \frac{dM_{\text{TO}}}{M_{\text{TO}}}$$

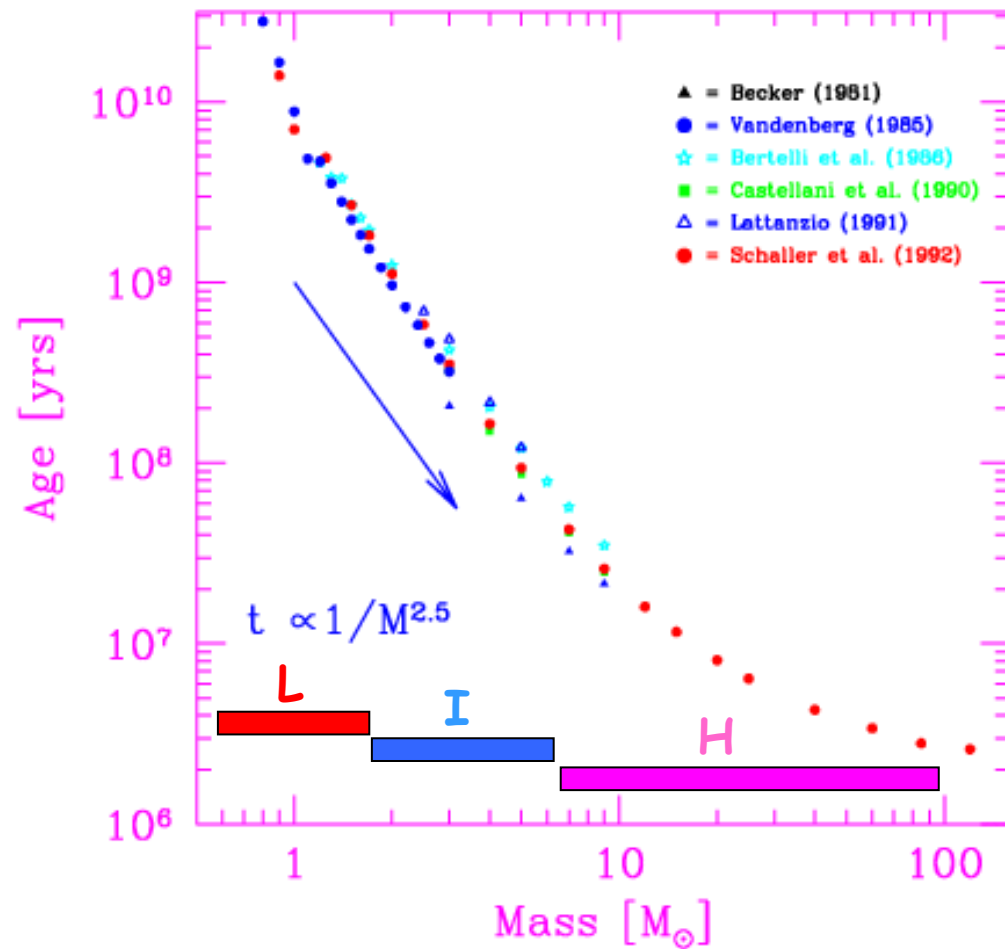
So



$$0.1 M_{\text{sun}} \approx \sim 3 \text{ Gyr}$$

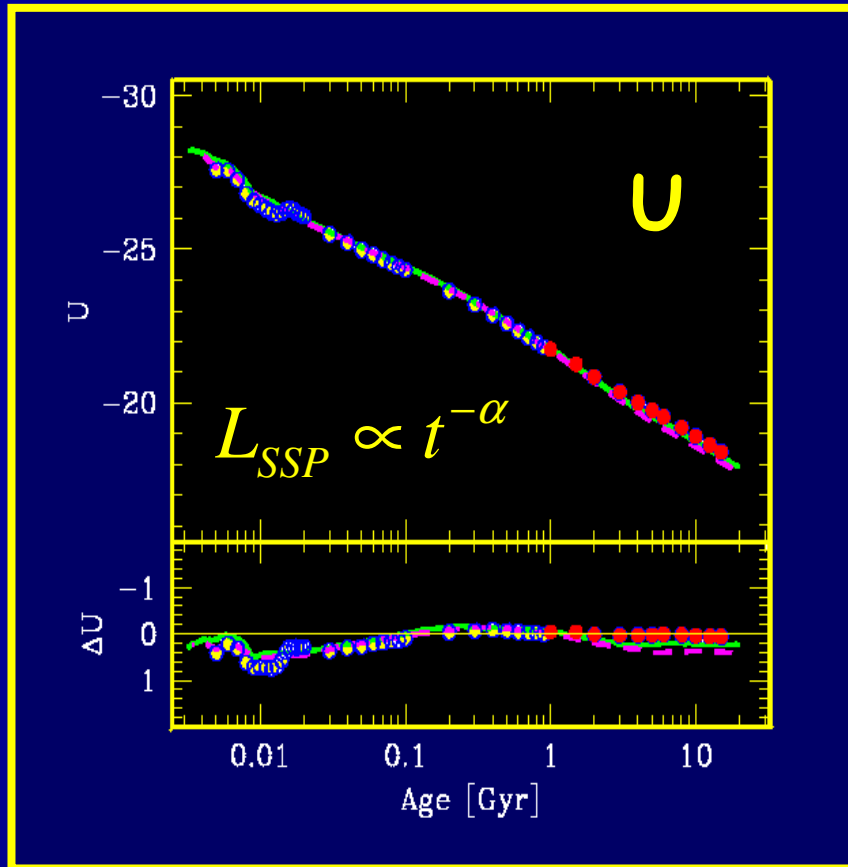


## The Clock



Buzzoni (2002)

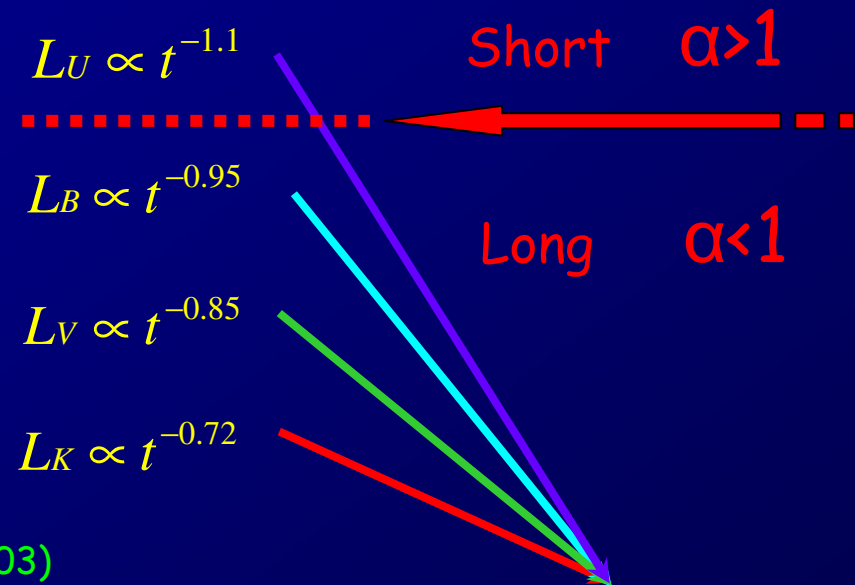
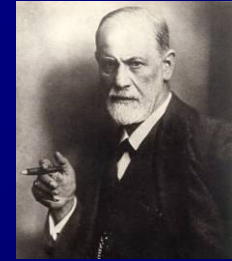




- Buzzoni (2005)      ● Bruzual & Charlot (2003)
- Bressan et al. (1994)    ● Leitherer et al. (1999)

$$L_{CSP}(t) = \int_{t_{\min}}^t L_{SSP}(\tau) SFR(\tau - t) d\tau$$

## Short-term vs. Long-term memory



$$L_{DISK} \propto [t^{(1-\alpha)} - t_{\min}^{(1-\alpha)}]$$

**The End (Part I)**