



Unconventional views of stellar populations



Part I Fundamentals of stellar population synthesis

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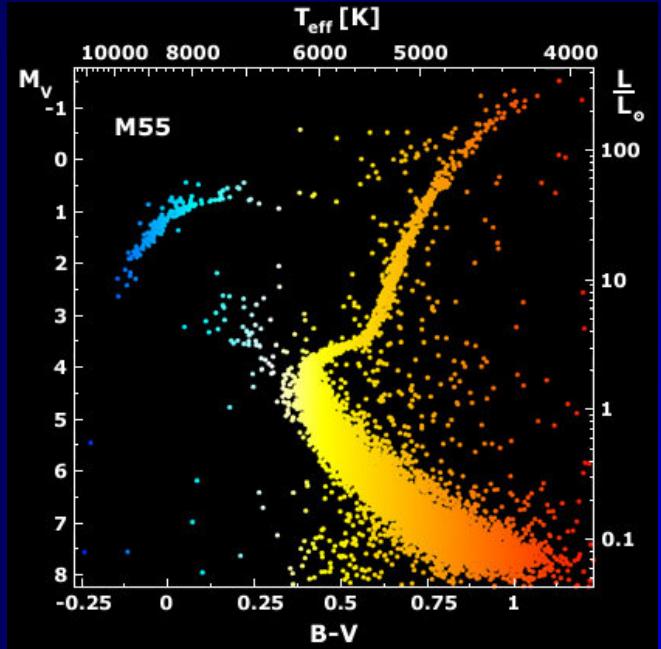
Star Trackers



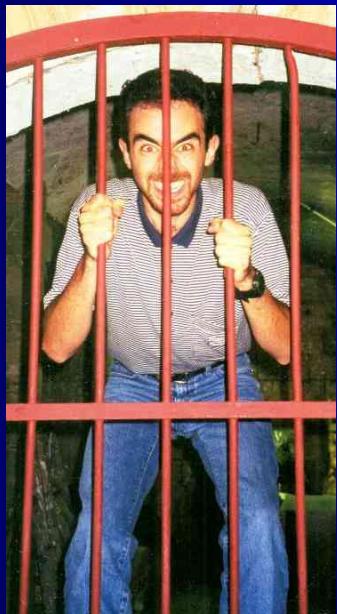
Ejnar Hertzsprung
Denmark (1873-1957)



Henry Norris Russell
USA (1877-1957)



From stars to star clusters



← Psychology
Sociology →



The “Color-Luminosity Array” (1915)

Limits of Photovisual Magnitude	Color-Class											All Colors
	b0 to b5	b5 to a0	a0 to a5	a5 to f0	f0 to f5	f5 to g0	g0 to g5	g5 to k0	k0 to k5	k5 to m0		
11.80-.99												
12.00-.19								1	3	2		6
.20-.39								1	1	1		2
.40-.59								3				5
.60-.79							1	2				5
.80-.99							4	2				6
13.00-.19	1					1	8	3				13
.20-.39						1	4	2				8
.40-.59						1	6	1				8
.60-.79						2	3	1				7
.80-.99						14	5	2				33
14.00-.19		3				1	9	3	2			15
.20-.39		1				10	13	4				28
.40-.59		1				24	16	4				56
.60-.79		6				1	6	12	1	1		29
.80-.99		3				2	5	8	2			25
15.00-.19	5	24	9	3	3	19	10	2				70
.20-.39	10	21	7	5	12	28	15					98
.40-.59	4	11	6	4	11	11	5	1	1			54
.60-.79	1	5	3	3	10	4	1					27
.80-.99												
Total	16	70	36	27	50	135	115	33	9	4	495	

evidence that the giant red stars were much brighter than the giant blue stars in the globular cluster Messier 13, that attention was called at once to the contrast between this color-luminosity diagram and the one



Harlow Shapley
USA (1885-1972)

(1930)

manent in spectral composition. Is this because the time units we use in measuring stellar evolution are still too anthropocentric, or because the clusters are timeless?

B²FH (1956)

Origin of the Elements in Stars

F. Hoyle, William A. Fowler,
G. R. Burbidge, E. M. Burbidge

Experimental (*1, 1a*) and observational (*2–6*) evidence has continued to accumulate in recent years in support of the theory (*7–10*) that the elements have been and are still being synthesized in stars. Since the appearance of a new and remarkable analysis by Suess and Urey (*11*) of the abundances of the elements, we have found it possible to explain, in a general way, the abundances of practically all the isotopes of the elements from hydrogen through uranium by synthesis in stars and supernovae. In this article we wish to outline in a qualitative fashion the essentially separate mechanisms which are required in stellar synthesis (*12*).

Thermal Conversion of Pure Hydrogen through Helium to Iron

As long as extremely high temperatures in excess of 5×10^9 degrees Kelvin are not under consideration, the general tendency of nuclear reactions inside stars is to increase the average binding energy per nucleon. For a given temperature and density and for a given time scale of op-

in some cases by resonance penetration. Since barrier effects become less severe as the temperature increases, it follows that the binding energies increase with temperature. This will become clear from the following example.

At temperatures from about 10^7 to 5×10^7 degrees in main-sequence stars, hydrogen is transformed to helium, $4\text{H}^1 \rightarrow \text{He}^4$, with an average binding energy of 7.07 million electron volts (Mev) per nucleon. We emphasize that the proton-proton sequence of reactions makes possible the production of helium starting only with hydrogen. The recent discovery of the free neutrino as reported by Cowan *et al.* (*1a*) leads to increased confidence in the existence of the primary proton-proton interaction which proceeds through prompt electron-neutrino emission. At temperatures from 10^8 to 2×10^8 degrees in red giant stars, He^4 is transformed principally to C^{12} , O^{16} , and Ne^{20} with an average binding energy of 7.98 Mev per nucleon. The important roles of the ground state of Be^8 and of the second excited state of C^{12} in expediting the primary process of helium fusion, $3\text{He}^4 \rightarrow \text{C}^{12}$, have recently been

appreciably greater atomic weight than Fe^{56} .

The situation, then, is that a thermal "cooking" of pure hydrogen yields principally He^4 and the α -particle nuclei with $A = 4n$, $Z = 2n$, $n = 3, 4, 5, 6, 7, 8, 9$, and 10 (C^{12} to Ca^{40}), to be centered around Fe^{56} . More abundant nuclei that have abundances that have been measured for these nuclei, and particularly the 20-odd isotopes of titanium, chromium, manganese, and nickel, show good agreement between observed abundances. The calculations by Fowler have been considerably improved by taking into account the low-lying states of the iron-group nuclei, active nuclei which undergo beta decay, and by statistical calculations according to its state according to its temperature. Typical results for the abundances of the chromium isotopes at 3.8×10^8 degrees are as follows:

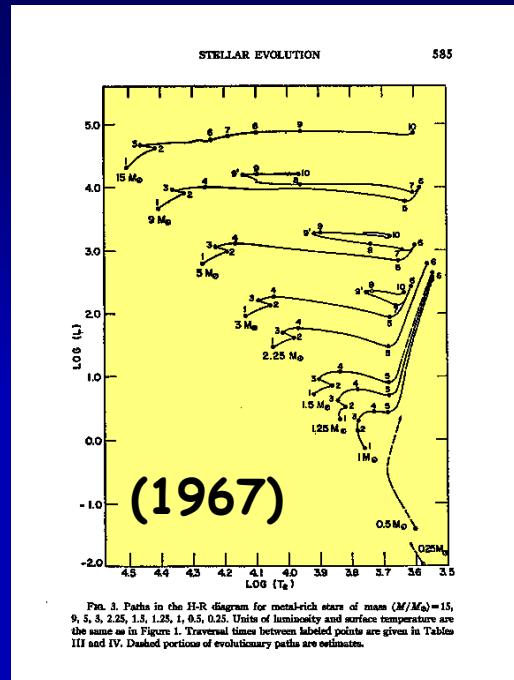
We regard results similar to those presented in Table I as giving strong support to the view that the elements heavier than silicon were synthesized in stars and that they became distributed in space, either from supernova explosion, as for instance



Scanned at the American Institute of Physics
Thermal Reactions of Hydrogen with Helium and Light Elements

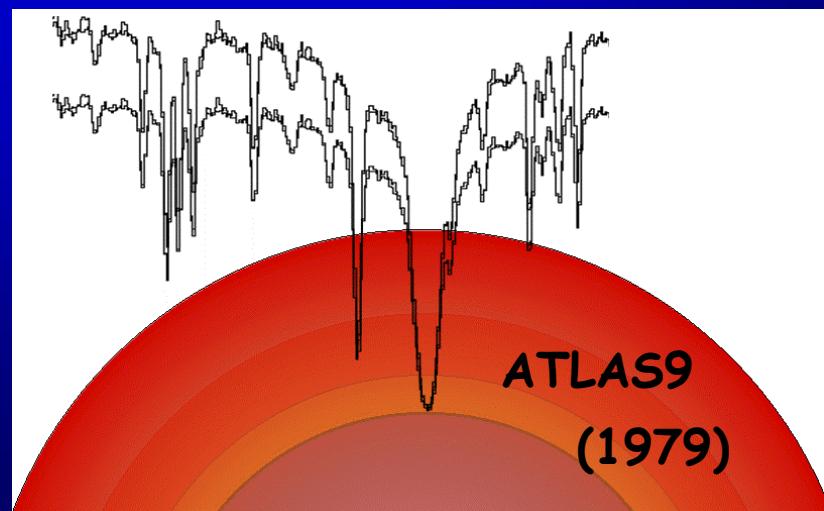
More complicated effects arise when the thermal cooking is considered, not of completely pure hydrogen, but of hydrogen adulterated with a small proportion of the elements mentioned in the previous paragraphs. When a second-generation

Star builders



Icko Iben USA (1931-)

Robert L. Kurucz USA (1946-)



Star synthesizers



Beatrice M. Tinsley
New Zealand/USA
(1941-1981)



Sandra M. Faber (USA)

'90

- Leitherer (et al.), 1999
- Maraston, 1998, 03, 05
- Granato & Silva, 1998
- Vazdekis (et al.), 1997, 99, 01, 03
- Poggianti (et al.), 1996, 97, 03
- Bressan & Chiosi (et al.), 1994, 96
- Worthey, 1994
- Fritze v. Alvensleben (et al.), 1992, 95, 99
- Brocato (et al.), 1990

'80

- Barbaro & Olivi, 1989
- Buzzoni, 1989, 95, 02, 05
- Bica (et al.), 1988, 90
- Rocca-Volmerange (et al.), 1988, 97
- Arimoto & Yoshii, 1986, 87
- Pickles, 1985
- Bruzual (& Charlot), 1983, 93, 03, 07

'70

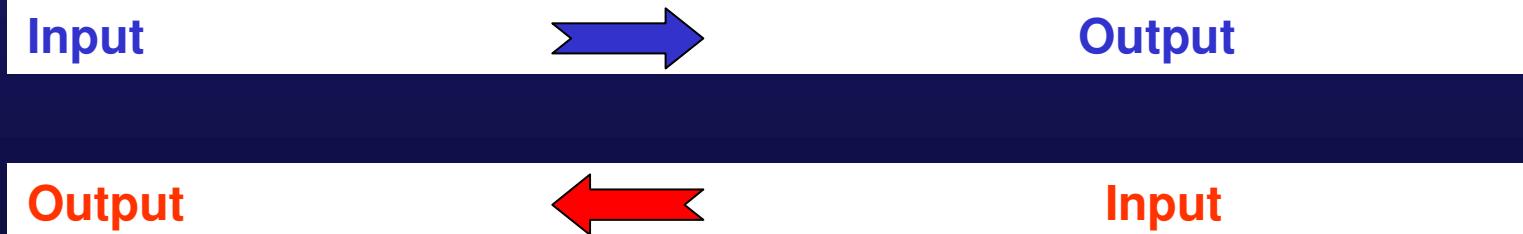
- Tinsley (et al.), 1976, 78
- O'Connell, 1976, 80
- Faber, 1972
- Spinrad & Taylor, 1969, 71

Most popular synthesis codes (→ 2008)



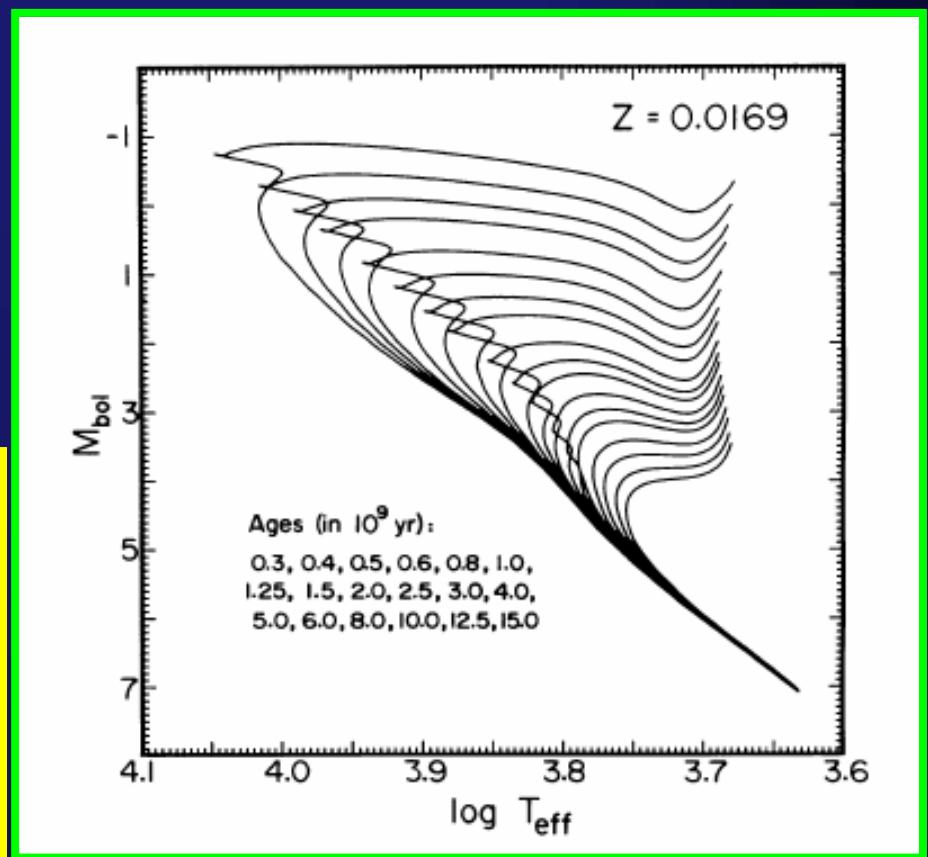
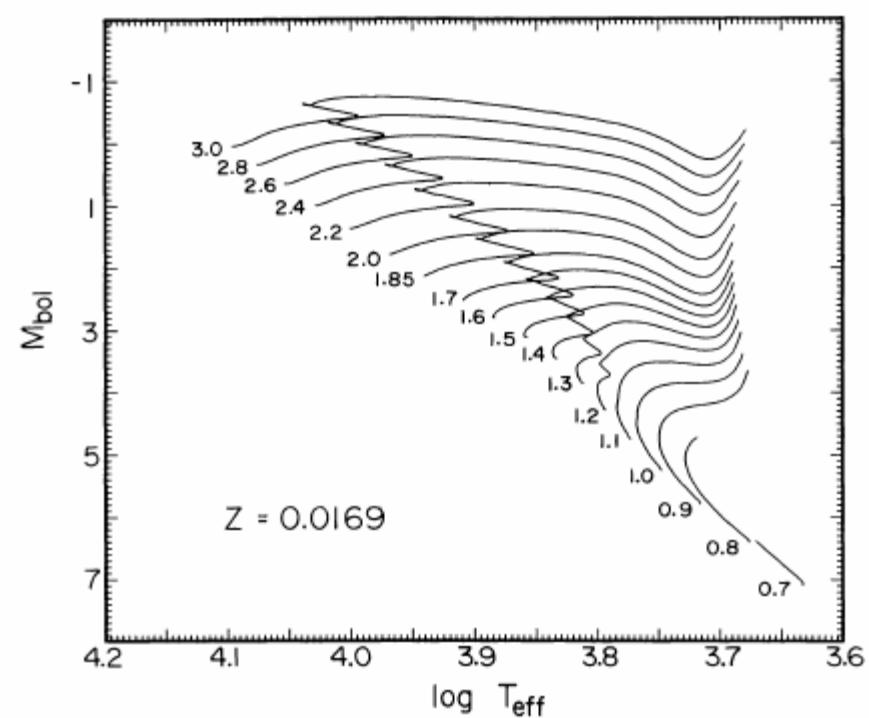
The synthesis approach...

$$F(\lambda) = \int^* f(\lambda)_{T,L} [HR\text{ diagram}]_{T,L}$$



Stellar tracks & Isochrones

Vandenbergh (1985)



A Simple Stellar Population (SSP) is...

- Any coeval sample of stars
- With fixed distinctive properties (other than stellar mass)
- Its c-m diagram can be described theoretically by an isochrone

Composite Stellar Populations (CSPs)

$$\text{CSP}(t) = \int_0^t \text{SSP}(\tau) \otimes \text{SFR}(t - \tau) d\tau$$

High-mass stars ($M > 7 M_{\text{sun}}$):

End up as SN II

Intermediate-mass stars
($2 < M < 7 M_{\text{sun}}$):

Helium ignites in a non-degenerate core

No HB (blue loops) No AGB

Nucleosynthesis up to C-O

Low-mass stars ($M < 2 M_{\text{sun}}$):

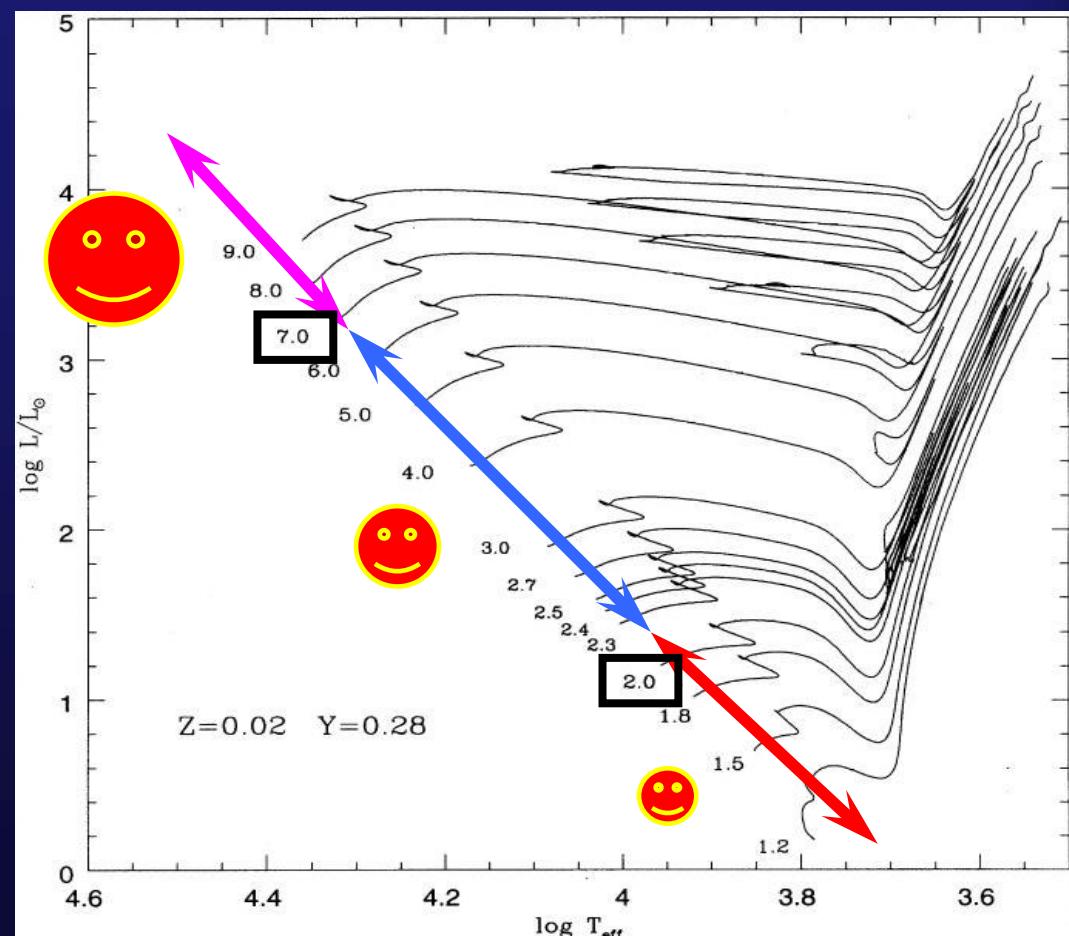
Helium ignites in a degenerate core (He flash)

Full HB - Full AGB

Nucleosynthesis up to C

Evolutionary regimes

Dominguez, Chieffi, Limongi, & Straniero (1999)



The Fuel Consumption Theorem

Renzini & Buzzoni (1986)

Post-MS luminosity contribution: $L = \int \ell_* N(M) dM_*$
IMF $\rightarrow N(M) dM = A M^{-s} dM$

$$L_{\text{PMS}} = \int \ell_* [A M^{-s}_{\text{TO}} dM/dt] d\tau$$

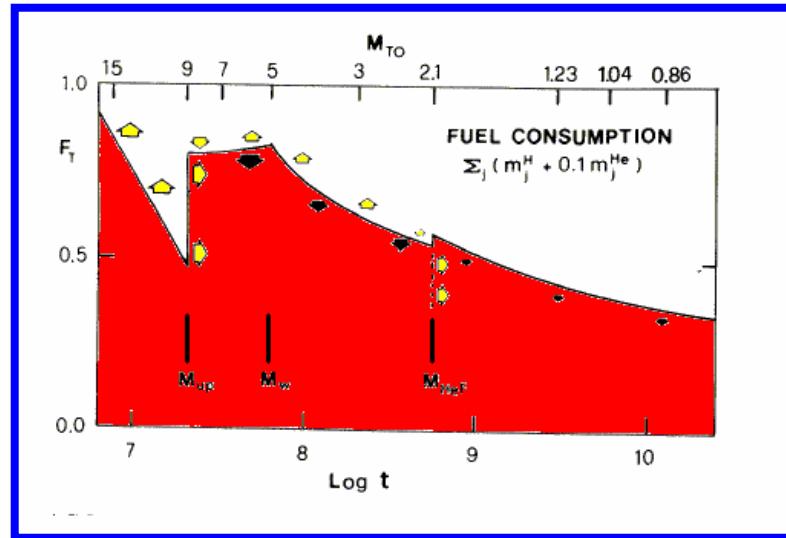
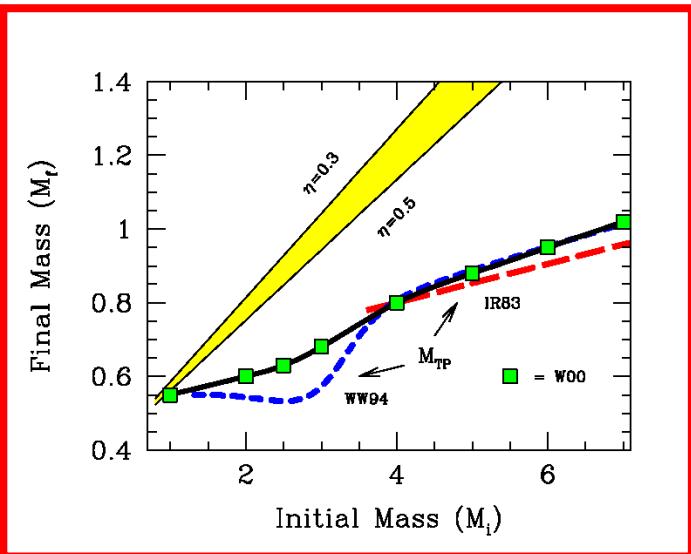
$$A \rightarrow M_{\text{tot}} \quad L_{\text{PMS}} = A M^{-s}_{\text{TO}} dM/dt \int \ell^* d\tau$$

Evolutionary flux (b) 

$$L_{\text{PMS}} / L_{\text{TOT}} = B \text{ Fuel}$$



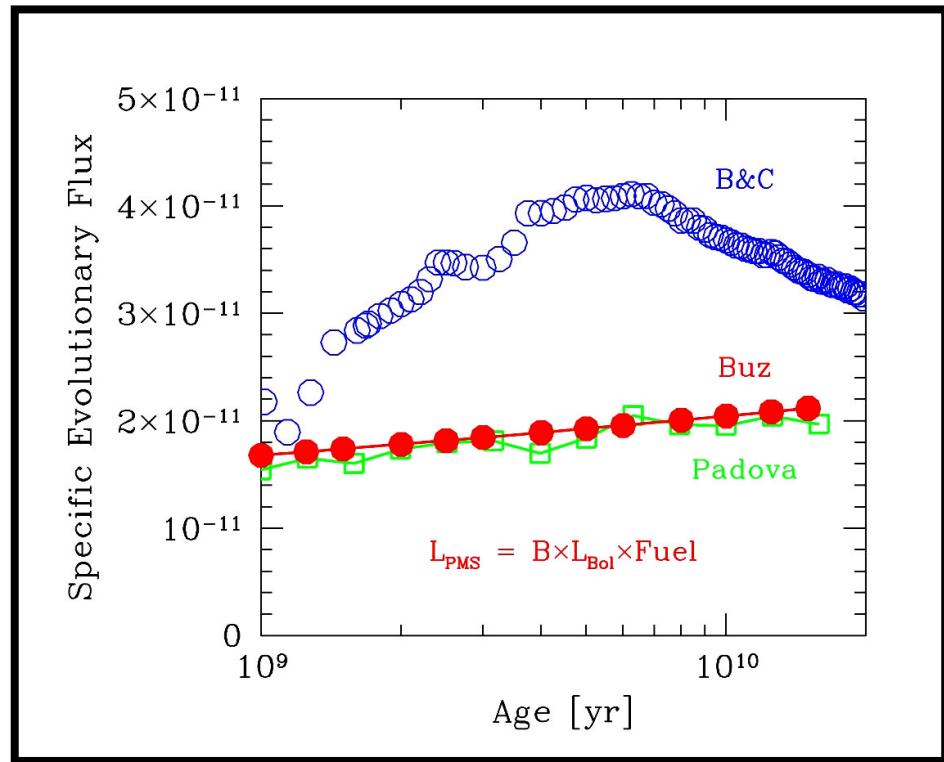
$$B = b/L_{\text{TOT}} \quad (\text{Specific evolutionary flux})$$



Fuel
B

Buzzoni, Arnaboldi & Corradi (2006)

Clock, Fuel...
& Energy
conservation!...



...a straightforward consequence on
number counts...

$$N_{\text{PMS}} = AM^{-s} dM = \left[AM_{\text{TO}}^{-s} \frac{dM_{\text{TO}}}{dt} \right] \tau = b \times \tau$$

$$N_{\text{PMS}} = \left[\frac{AM_{\text{TO}}^{-s} \frac{dM_{\text{TO}}}{dt}}{L_{\text{TOT}}} \right] L_{\text{TOT}} \tau = B \times L_{\text{TOT}} \times \tau$$

1.7 (± 0.3) 10^{-11} (Buzzoni 1989)

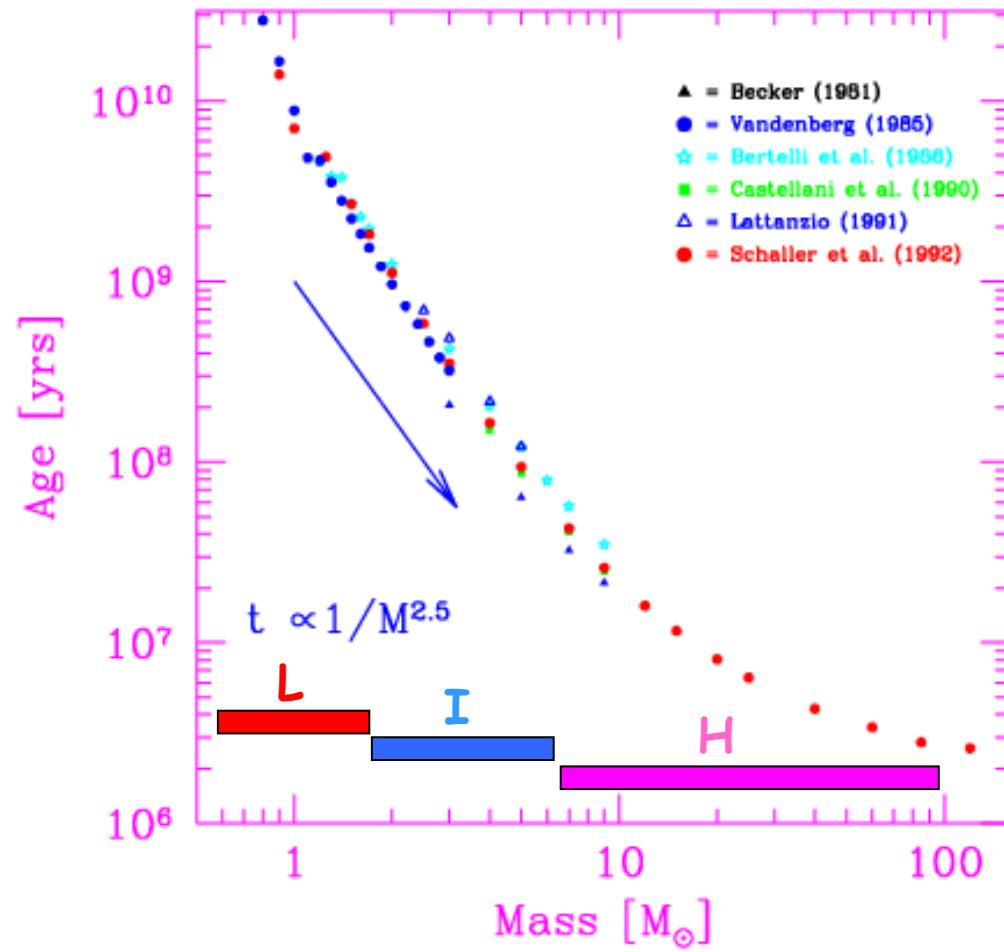
$$\frac{dt}{t} \approx -2.5 \frac{dM_{\text{TO}}}{M_{\text{TO}}}$$

S_0

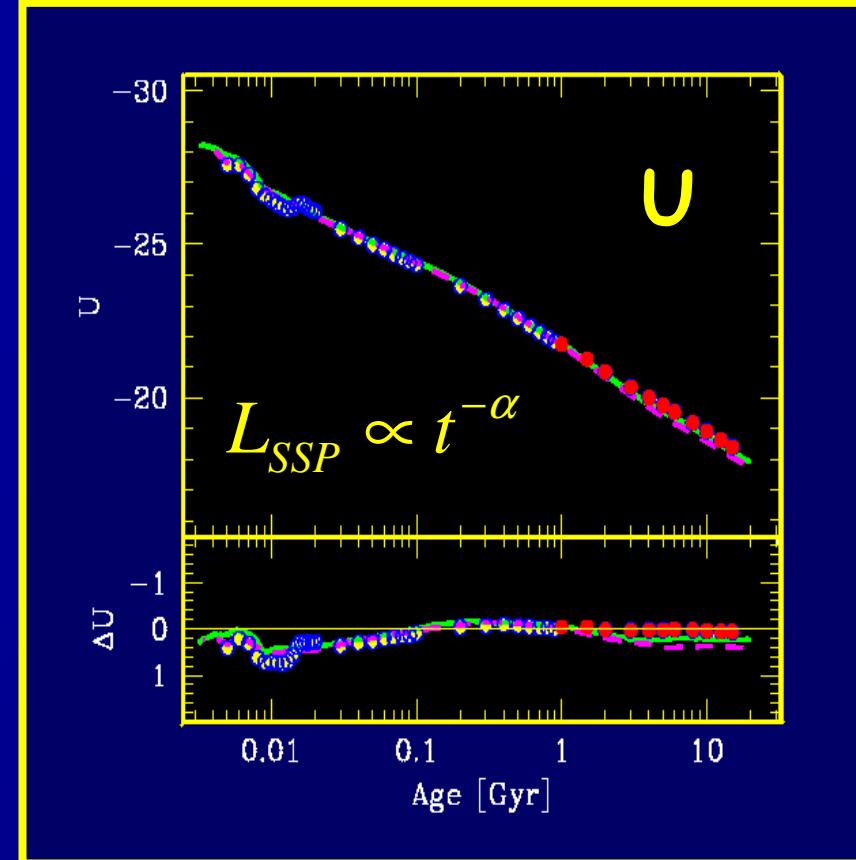
$$0.1 M_{\text{sun}} \approx \sim 3 \text{ Gyr}$$



The Clock

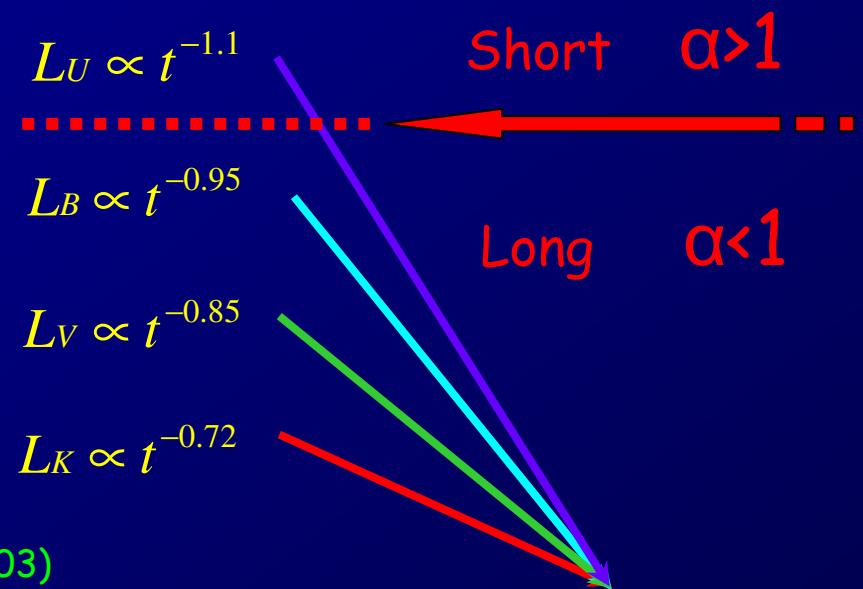
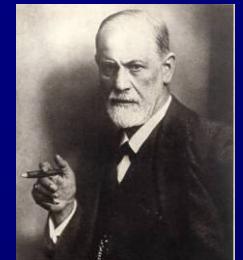


Buzzoni (2002)



- Buzzoni (2005)
- Bruzual & Charlot (2003)
- Bressan et al. (1994)
- Leitherer et al. (1999)

Short-term vs. Long-term memory



$$L_{CSP}(t) = \int_{t \min}^t L_{SSP}(\tau) SFR(\tau - t) d\tau$$

$$L_{DISK} \propto [t^{(1-\alpha)} - t_{\min}^{(1-\alpha)}]$$

The End (Part I)