

# *Planetary population synthesis*

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**UNIVERSITÄT  
BERN**



## 1) Planet formation models

Planet growth

Disk structure and evolution

Migration

## 2) First generation population synthesis models

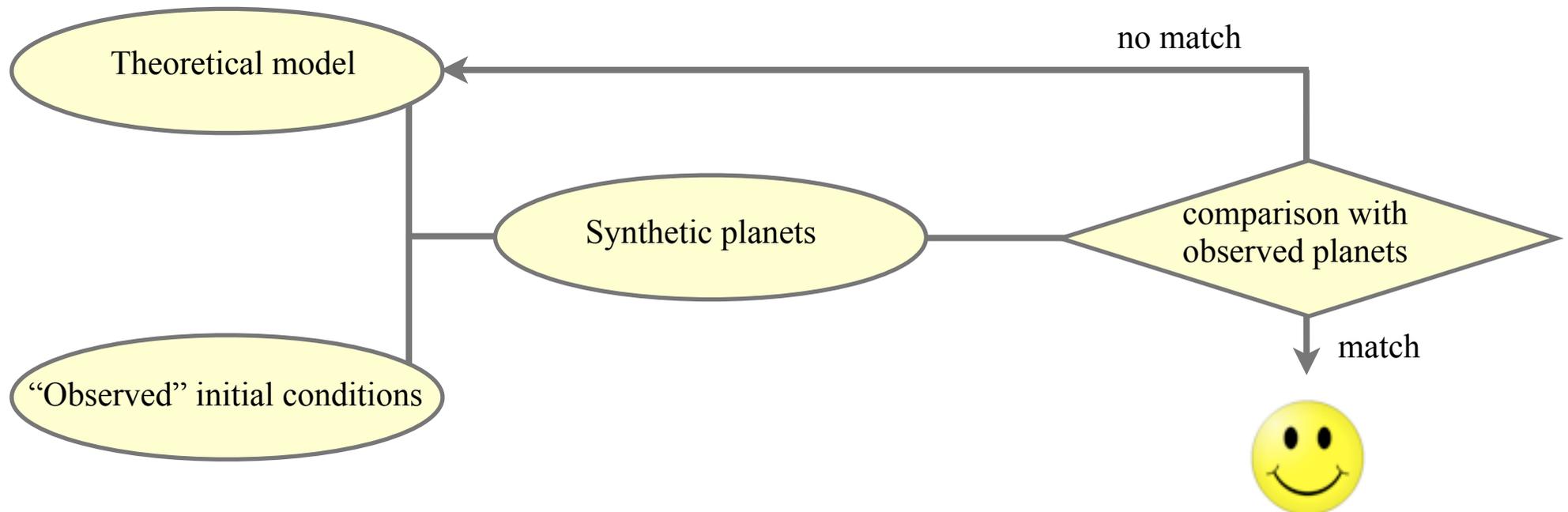
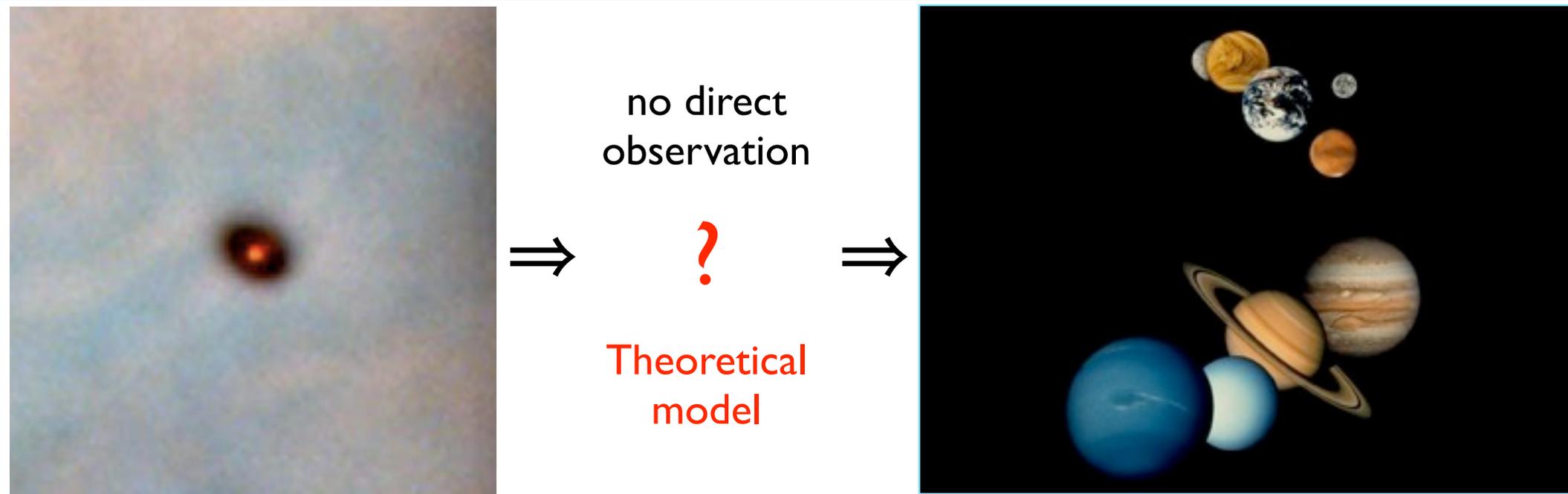
Initial conditions

Reproducing *planet* observations

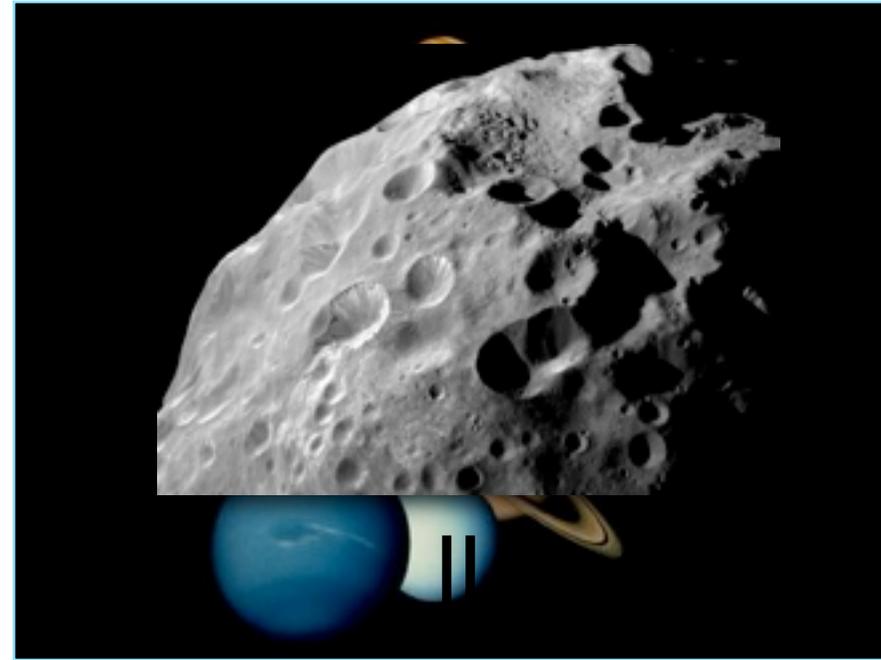
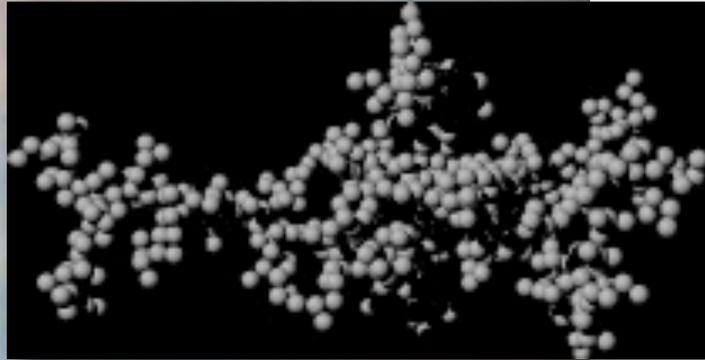
## 3) Second generation population synthesis models

Using *disk* observations

# Planet formation



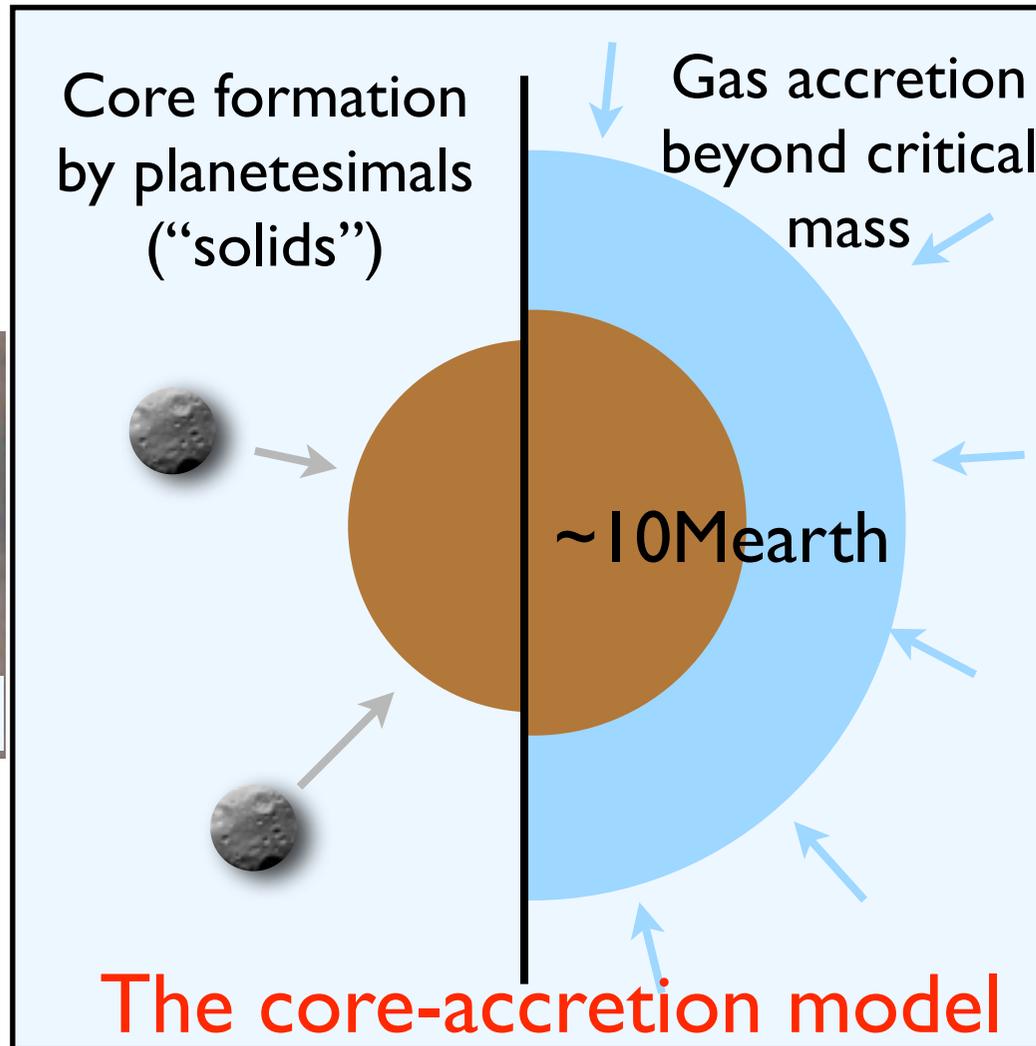
# Planet formation



Talk by Kees

This talk

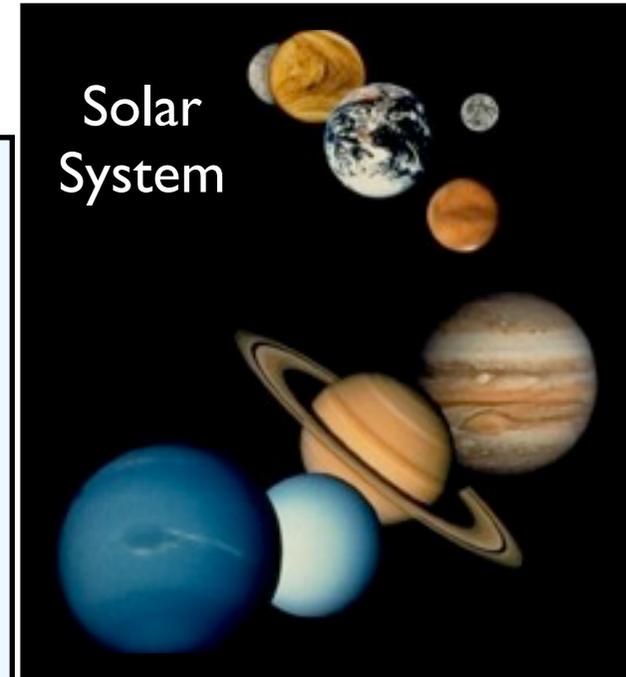
# The core accretion paradigm



Protoplanetary disk

99% gas 1% solids

Solar System

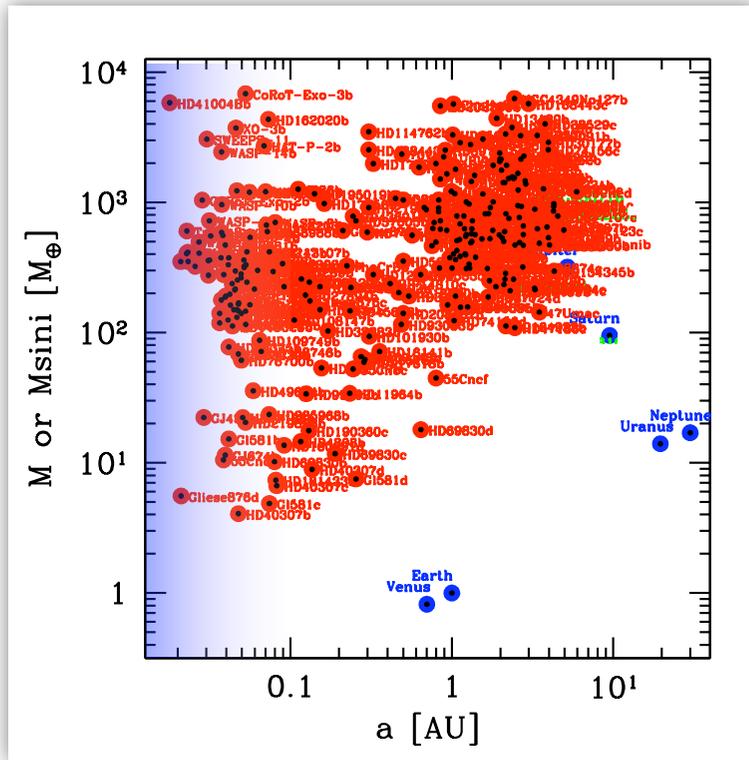


Extrasolar planets

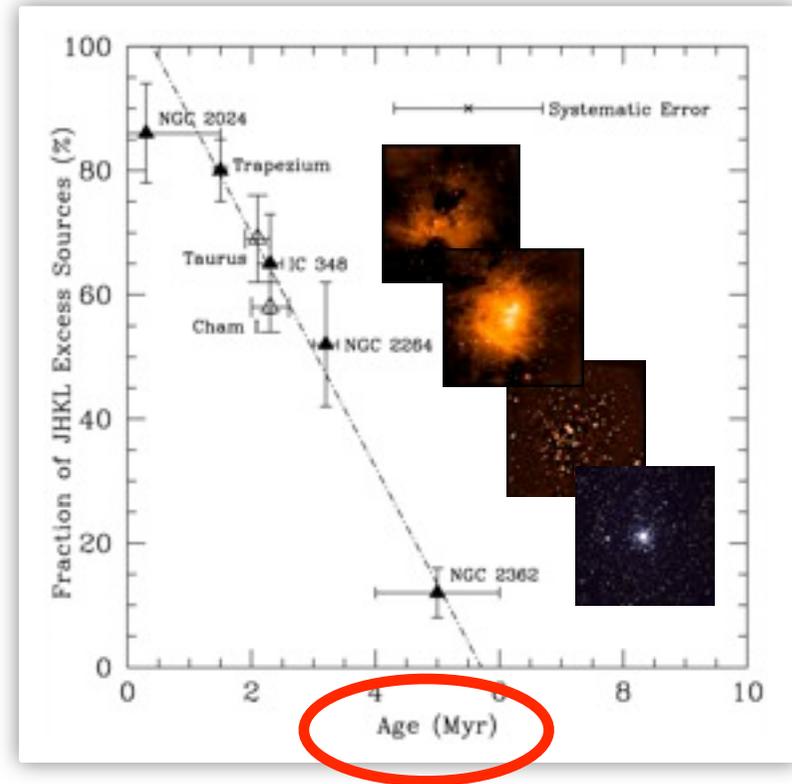


# Extended models

1) “standard” core-accretion model predict formation in few Myr



In-situ formation seems not possible  $\Rightarrow$  migration



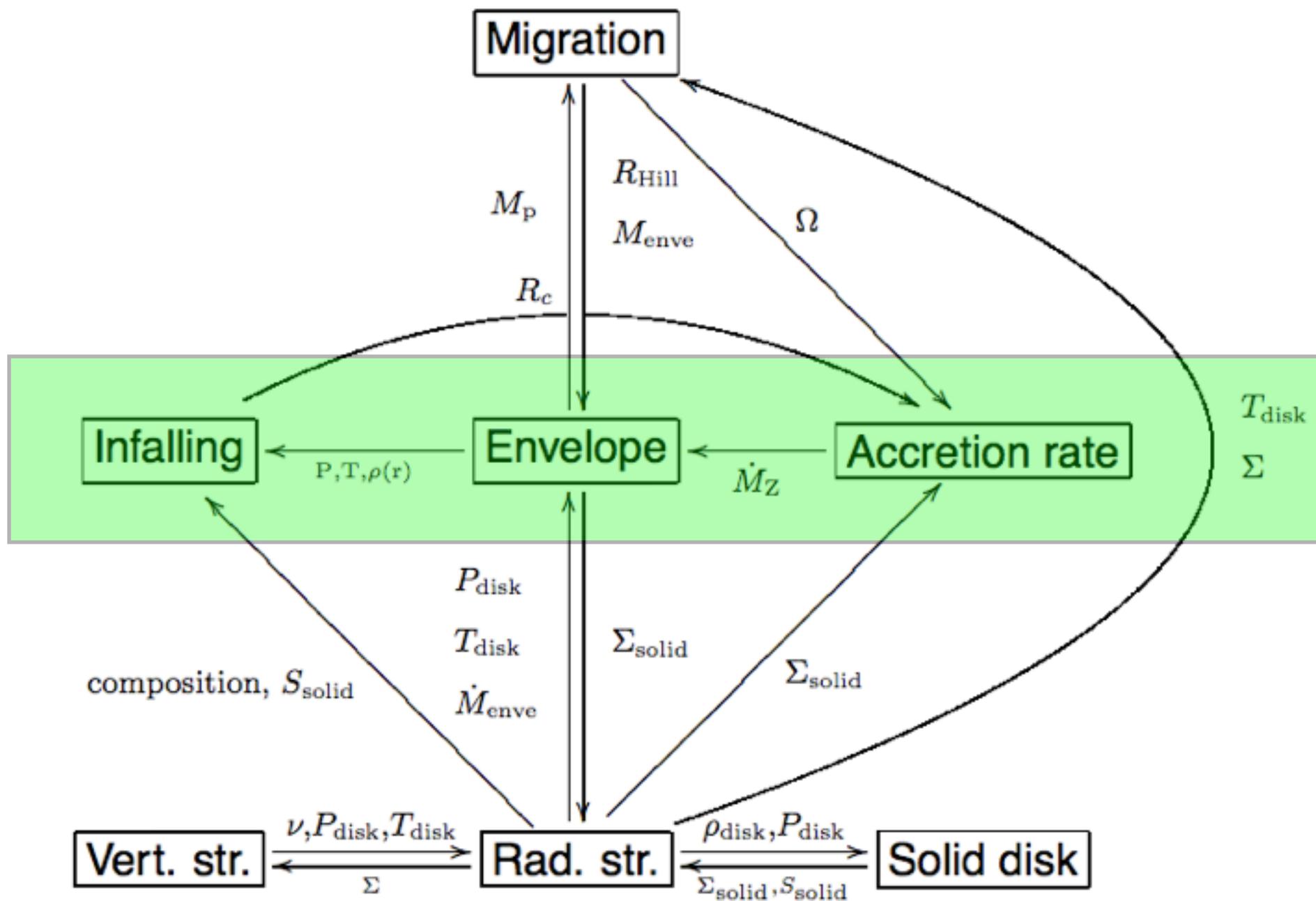
disk evolution  $\Leftarrow$  Evolution in  $\sim$ Myr

2) disk evolution

3) type I and type II migration

*The model is kept as simple as possible: No tricks, everything is “standard” but considered together...*

# Models overview



# Planet's solids accretion rate

$$\frac{dM_Z}{dt} = R_{\text{cap}}^2 \Omega \Sigma_{\text{planetesimals}} F_g(e, i, R_{\text{cap}})$$

- Trajectory of planetesimals computed with

- gas drag
- gravity

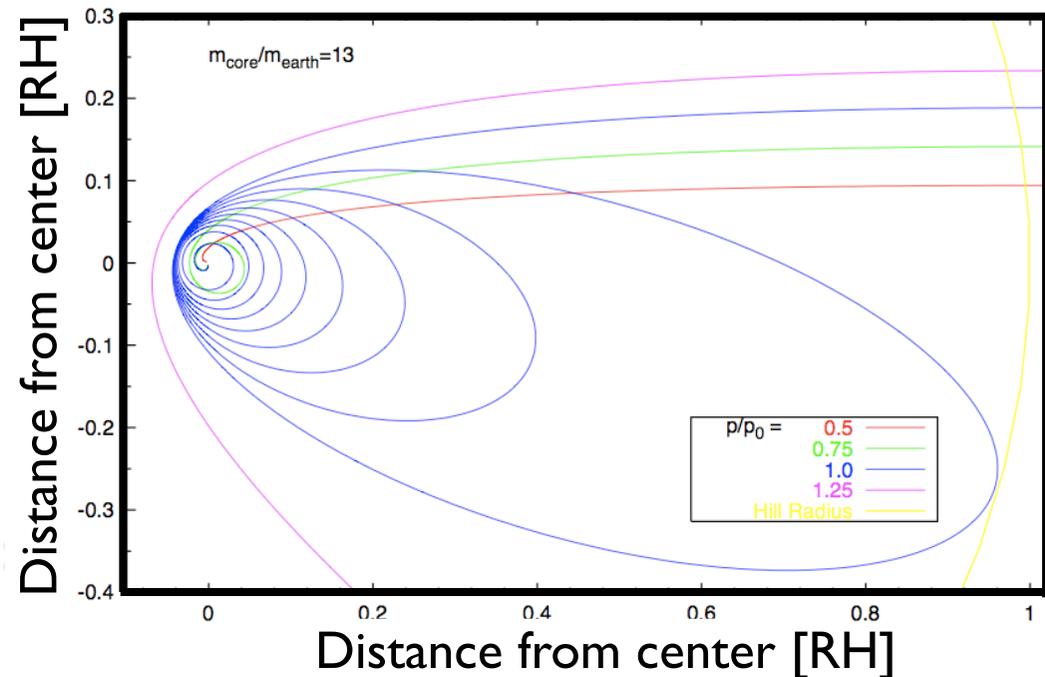
$$m(t) \frac{d^2 \vec{x}}{dt^2} = - \frac{GM(x)m(t)}{x^2} \tilde{x} - \frac{1}{2} \pi r^2 C_D(Re, Ma) \rho_g v^2 \tilde{v}$$

- Mass loss due to:

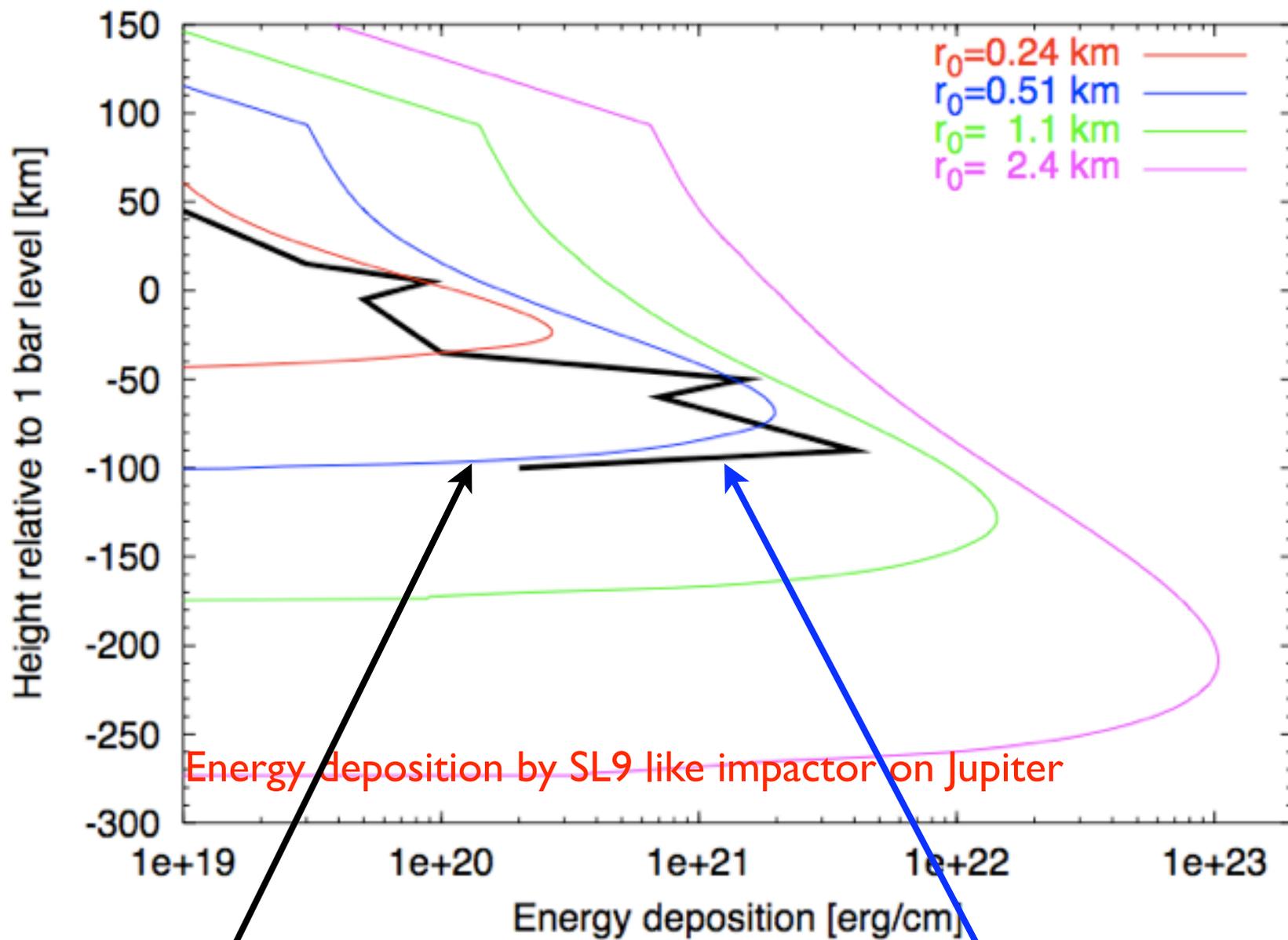
- radiation from ambient gas and shock wave:

$$\begin{cases} \frac{dm}{dt} = - \frac{F_{\text{input}} \pi r^2(t)}{Q_{\text{abl}}} \\ F_{\text{input}} = \frac{1}{2} C_H \rho_g v^3 \\ C_H = 10^{-5} \text{ to } \frac{1}{2} C_D \end{cases}$$

- mechanical effects (Zahnle 1992, MacLow 1996, Korykansky 2002)



# Planet's solids accretion rate



Full 3D models (Zahnle & MacLow 1994)

Our (1D) model (Mordasini et al., in prep)

# Planet's internal structure

## Internal structure equations

$$1) \frac{dr^3}{dm} = \frac{3}{4\pi\rho} \quad \text{mass conservation}$$

$$2) \frac{dP}{dm} = -\frac{G(m + M_{core})}{4\pi r^4} \quad \text{hydrostatic equilibrium}$$

$$3) \frac{dT}{dP} = \nabla_{ad} \text{ or } \nabla_{rad} \quad \text{energy transfer}$$

$$L = L_{\text{planetesimals}}$$

Envelope mass derives from the condition  $R_{\text{planet}} = R_{\text{Hills}}$

Gas accretion rate limited by disk properties

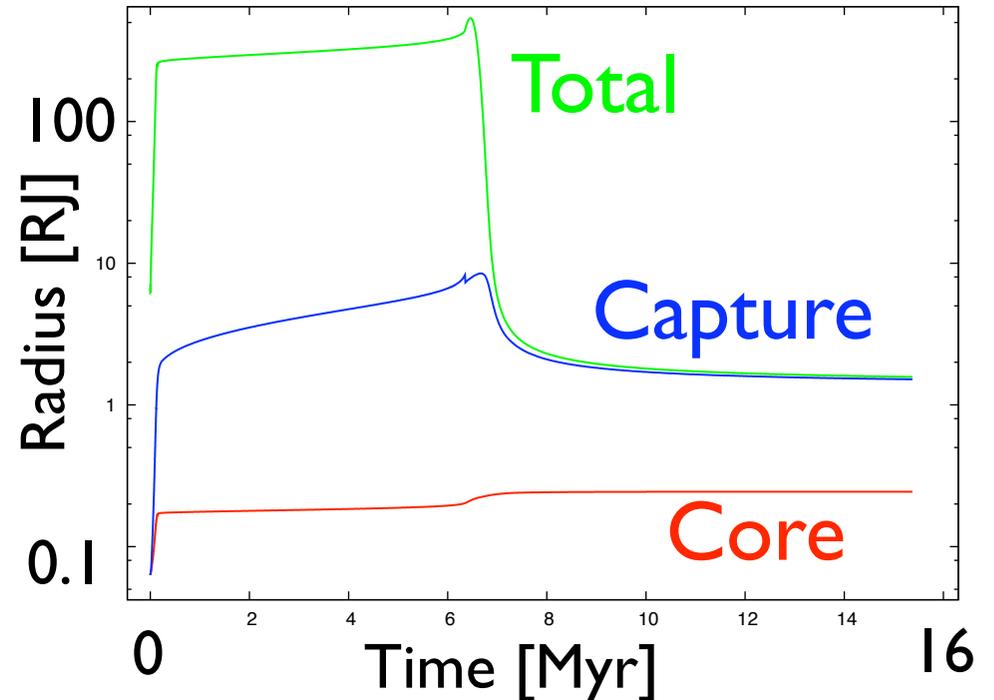
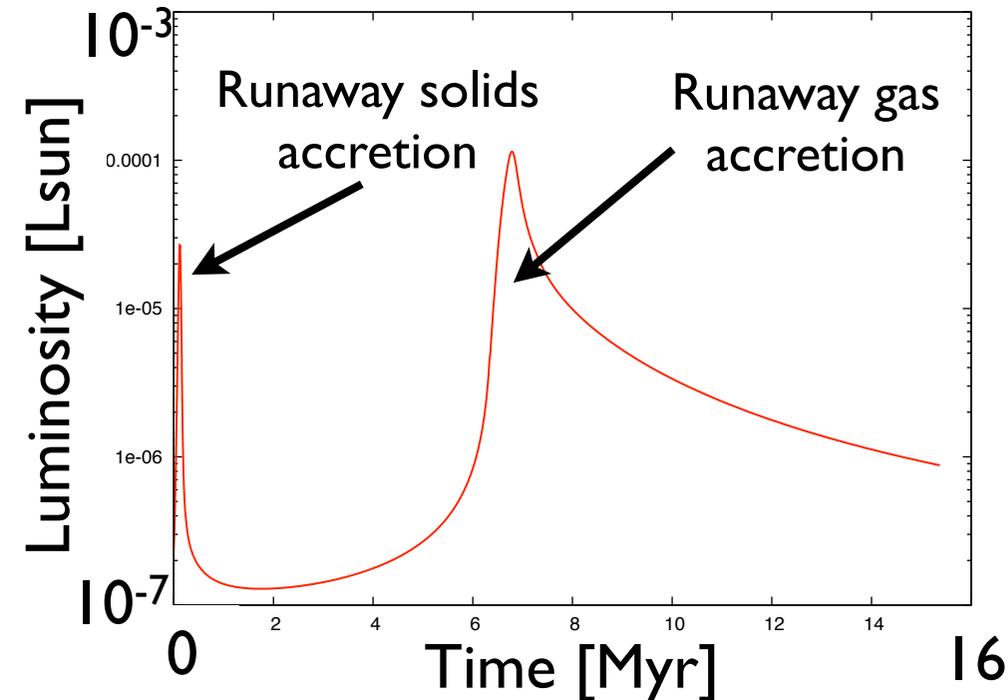
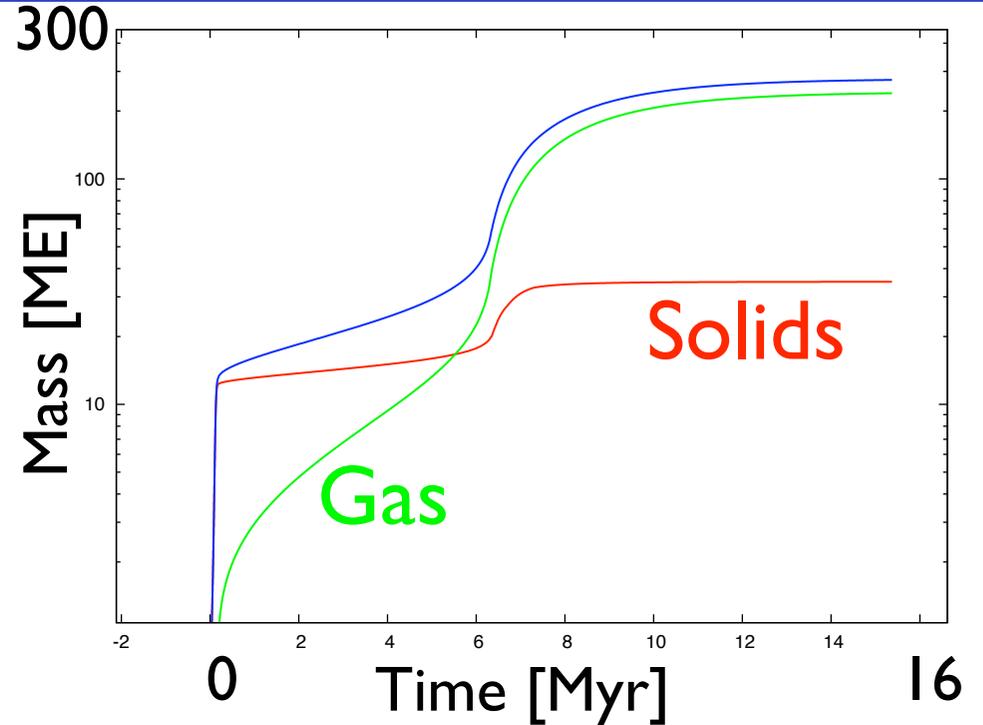
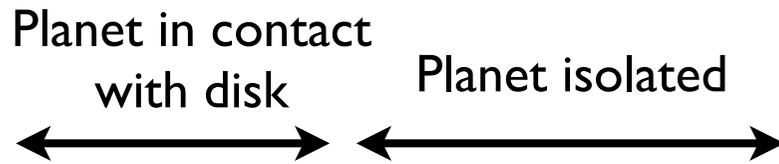
# Planet's internal structure

In situ formation of Jupiter at 5.2 AU

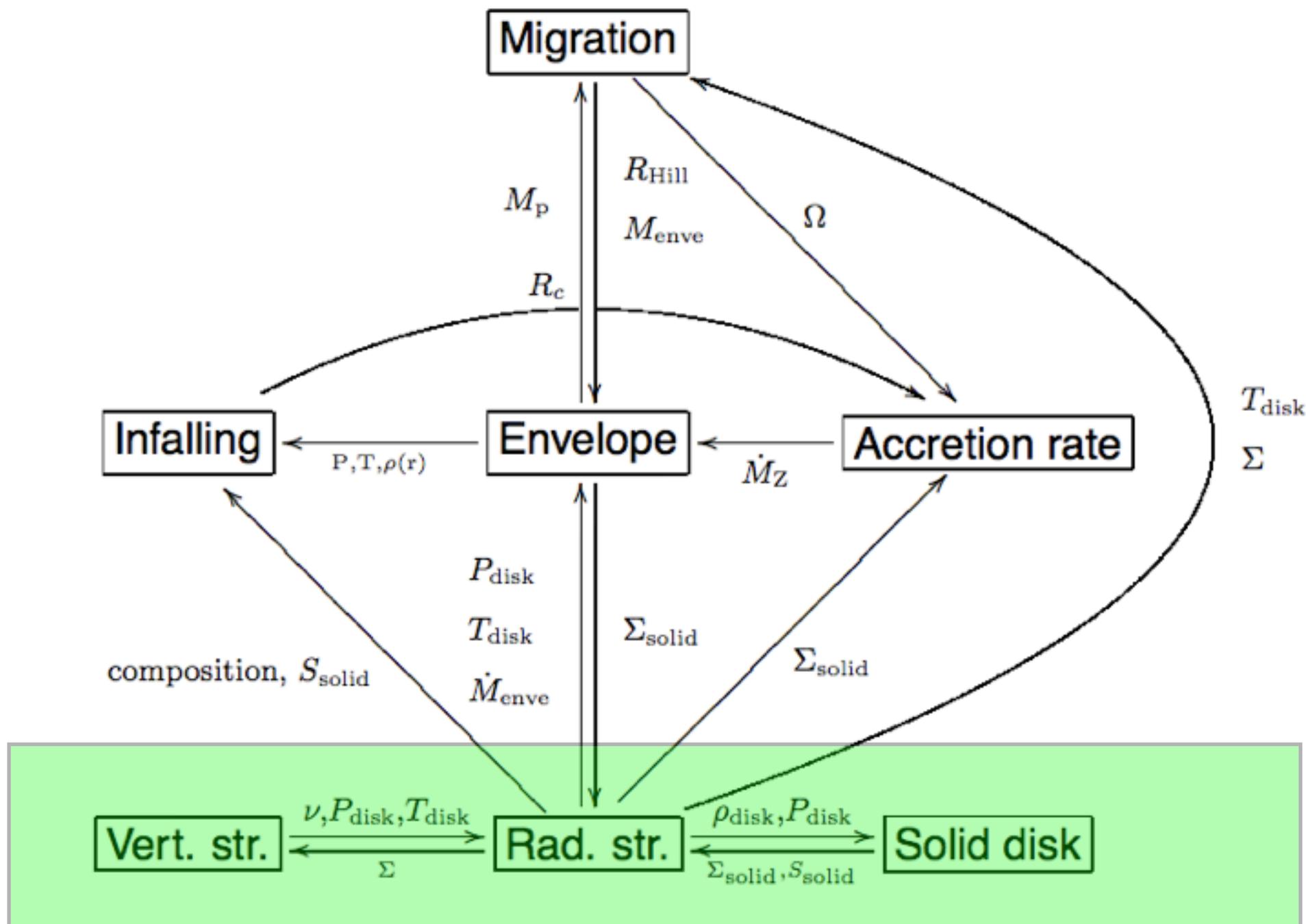
$$\Sigma_{\text{solids}} = 10 \text{g/cm}^2 @ 5.2 \text{AU}$$

$$M_{\text{disk}} \approx 0.03 M_{\odot}$$

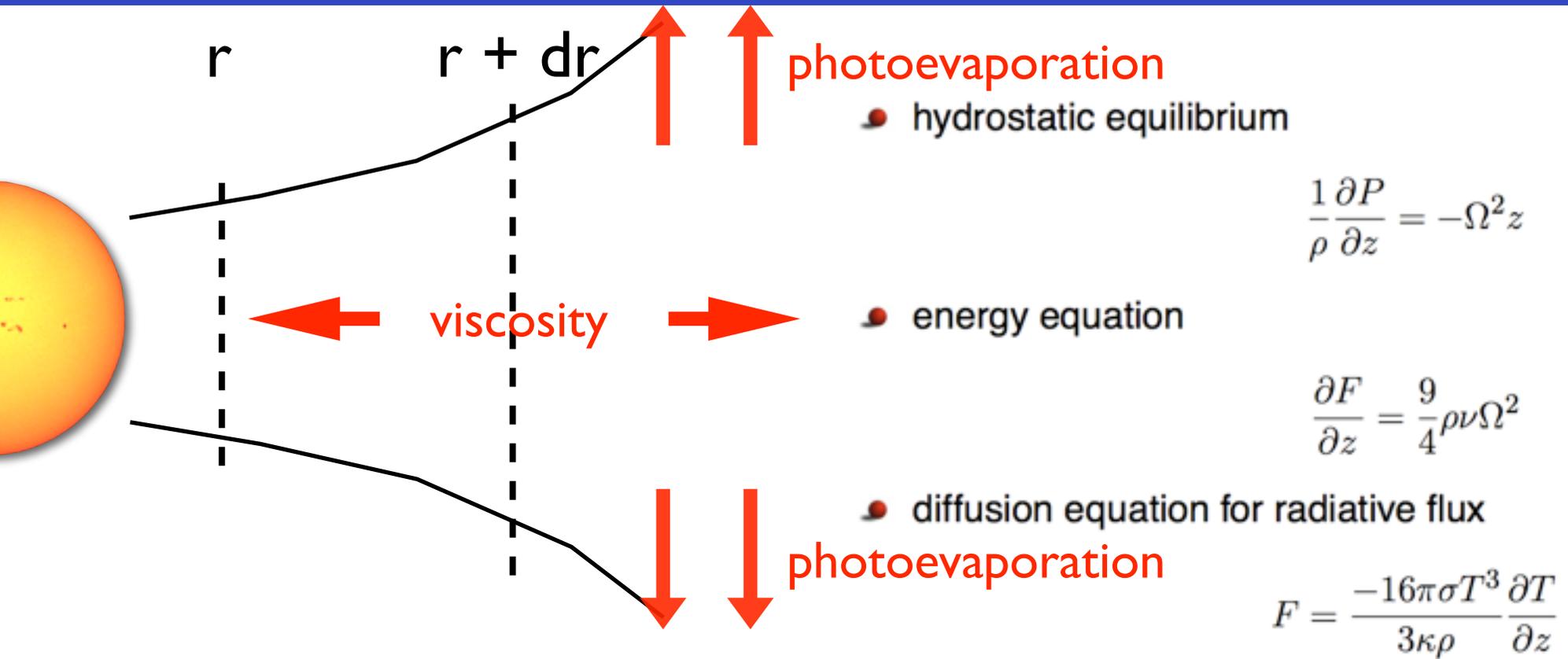
only viscosity



# Models overview



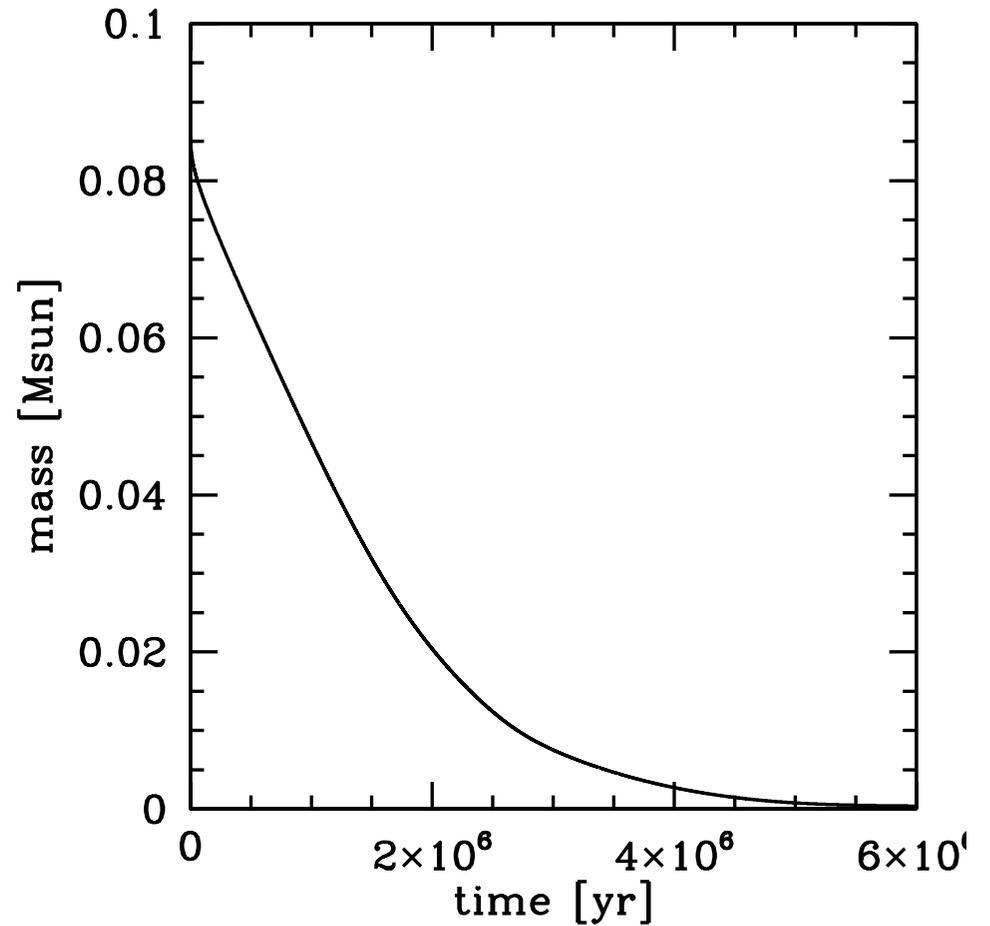
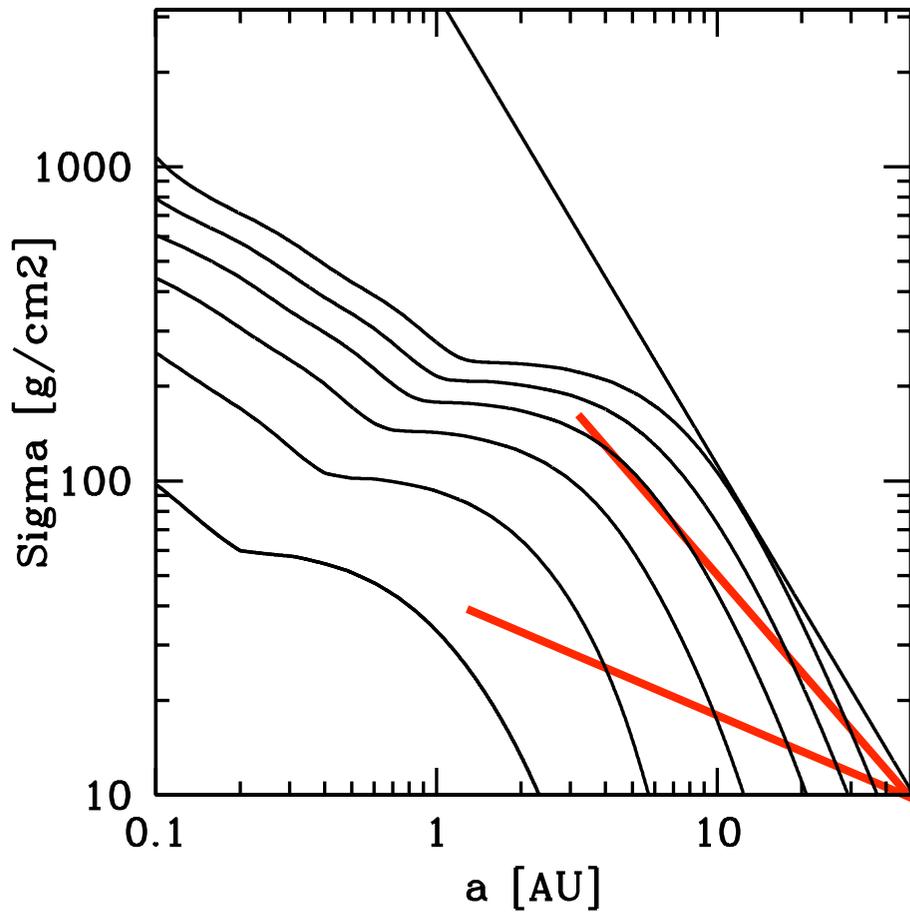
# Disk model: gas



$$\frac{d\Sigma}{dt} = \frac{3}{r} \frac{\partial}{\partial r} \left[ r^{1/2} \frac{\partial}{\partial r} \tilde{\nu} \Sigma r^{1/2} \right] + \dot{\Sigma}_w(r)$$

Photoevaporation model from Veras and Armitage 2004

# Disk model: gas



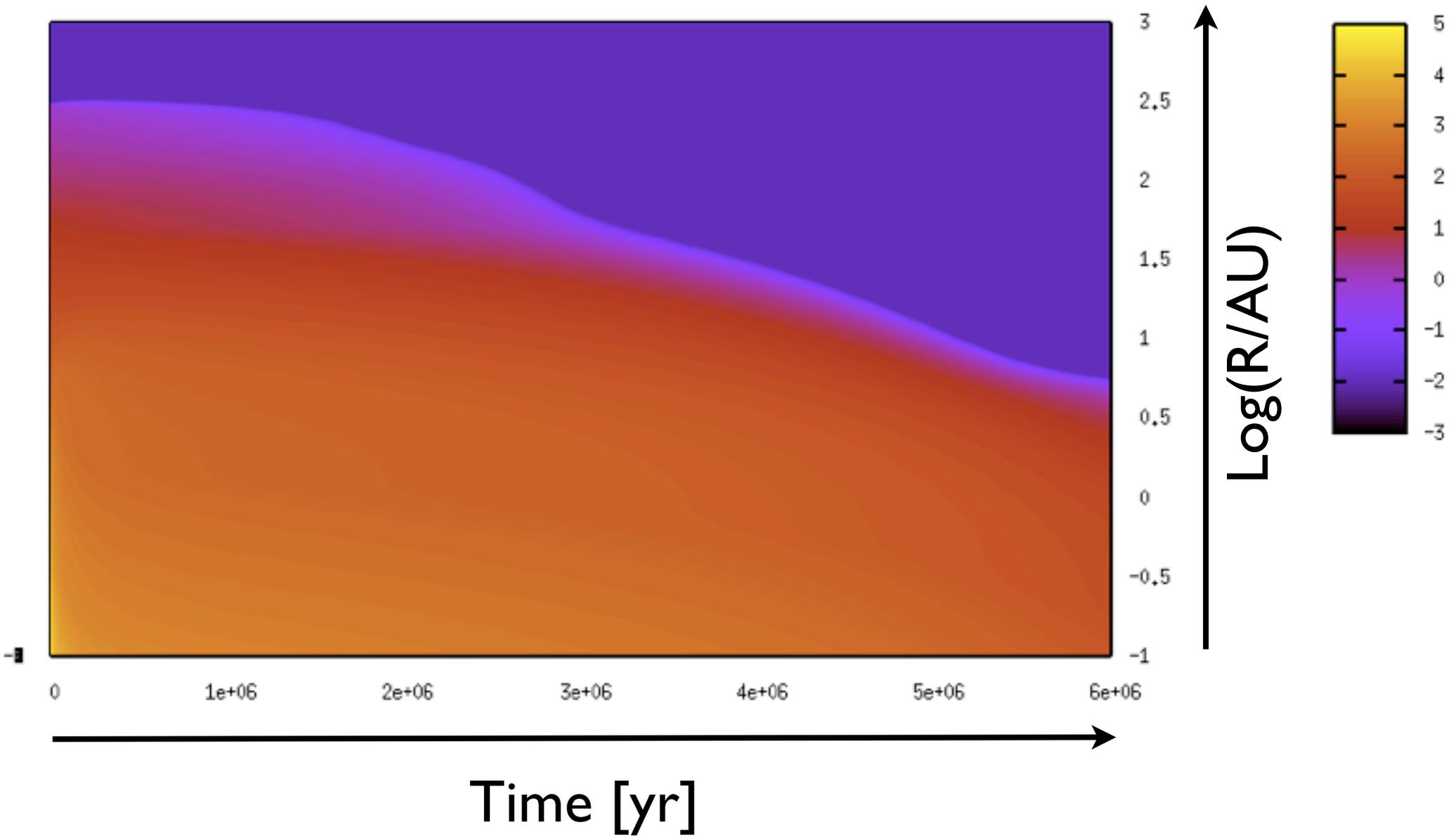
$$R_{\text{in}} = 0.1 \text{ AU}$$

$$R_{\text{out}} = 300 \text{ AU}$$

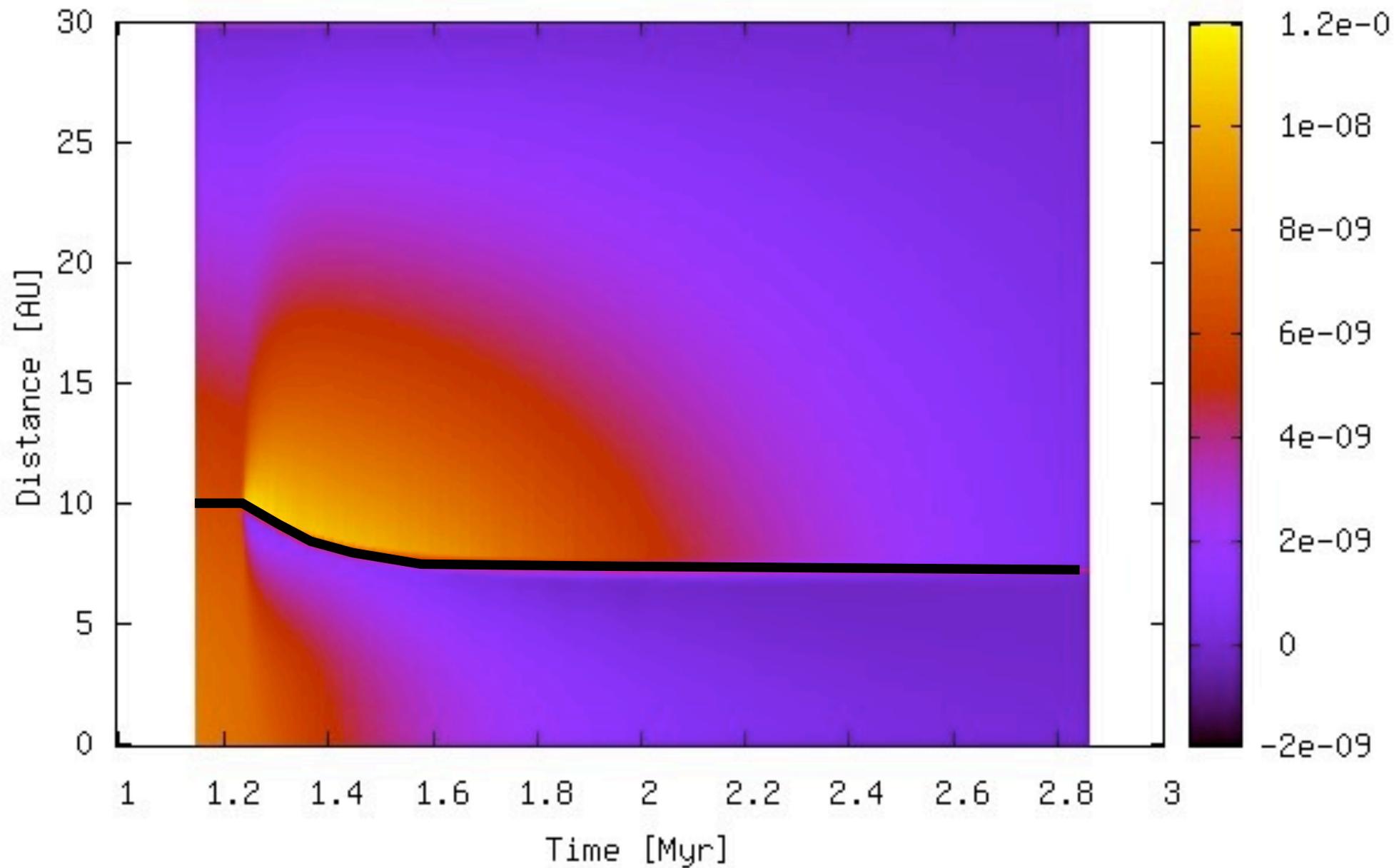
$$M_{\text{W}} = 10^{-7} M_{\odot} / \text{yr}$$

Constant viscosity parameter

# Disk model: gas

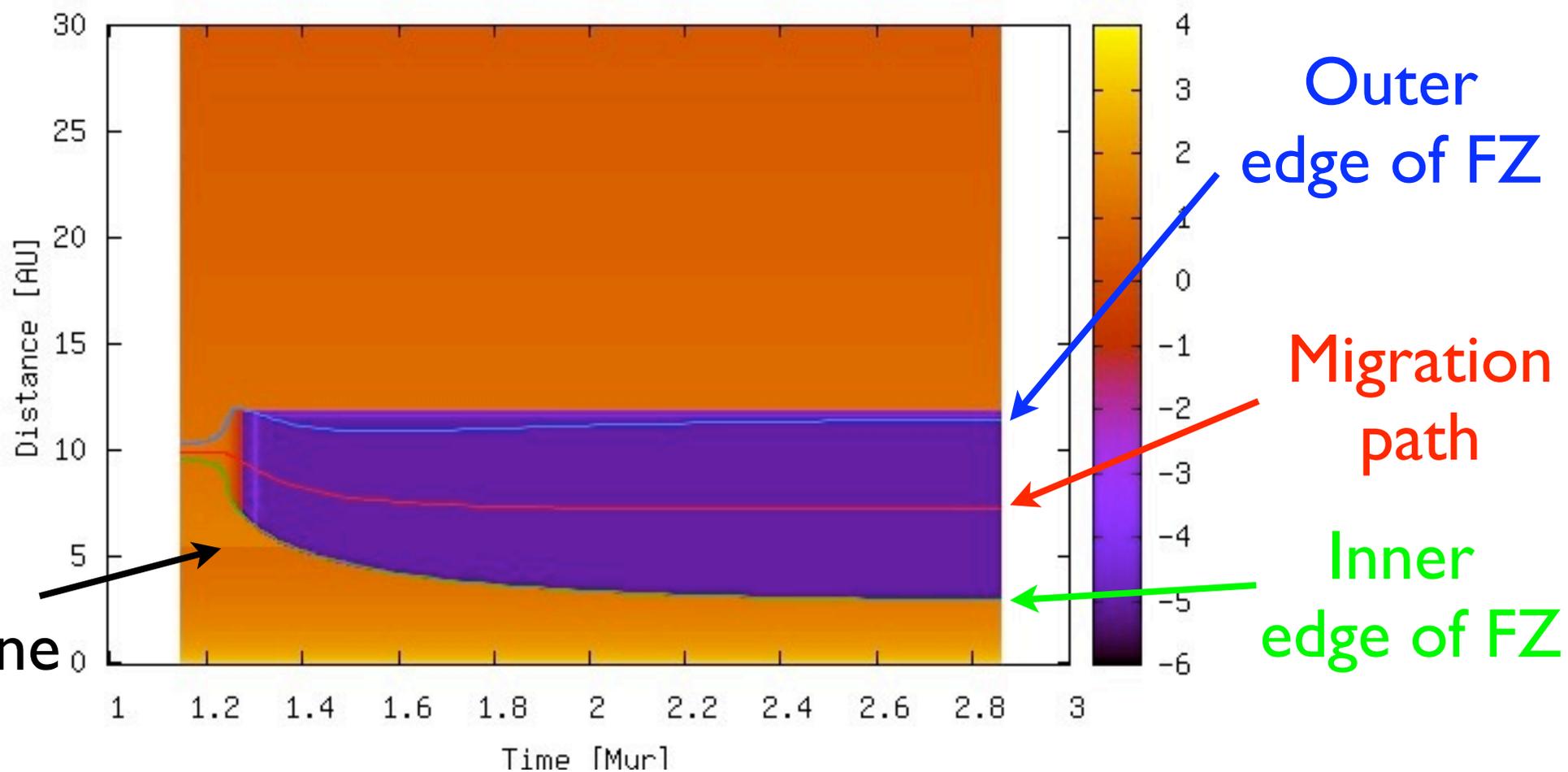
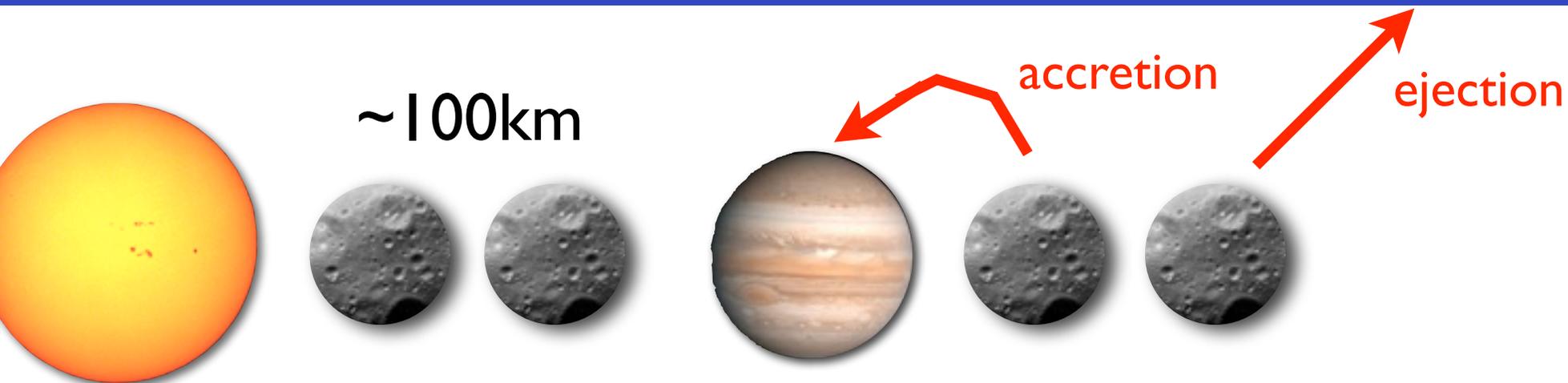


# Disk model: gas

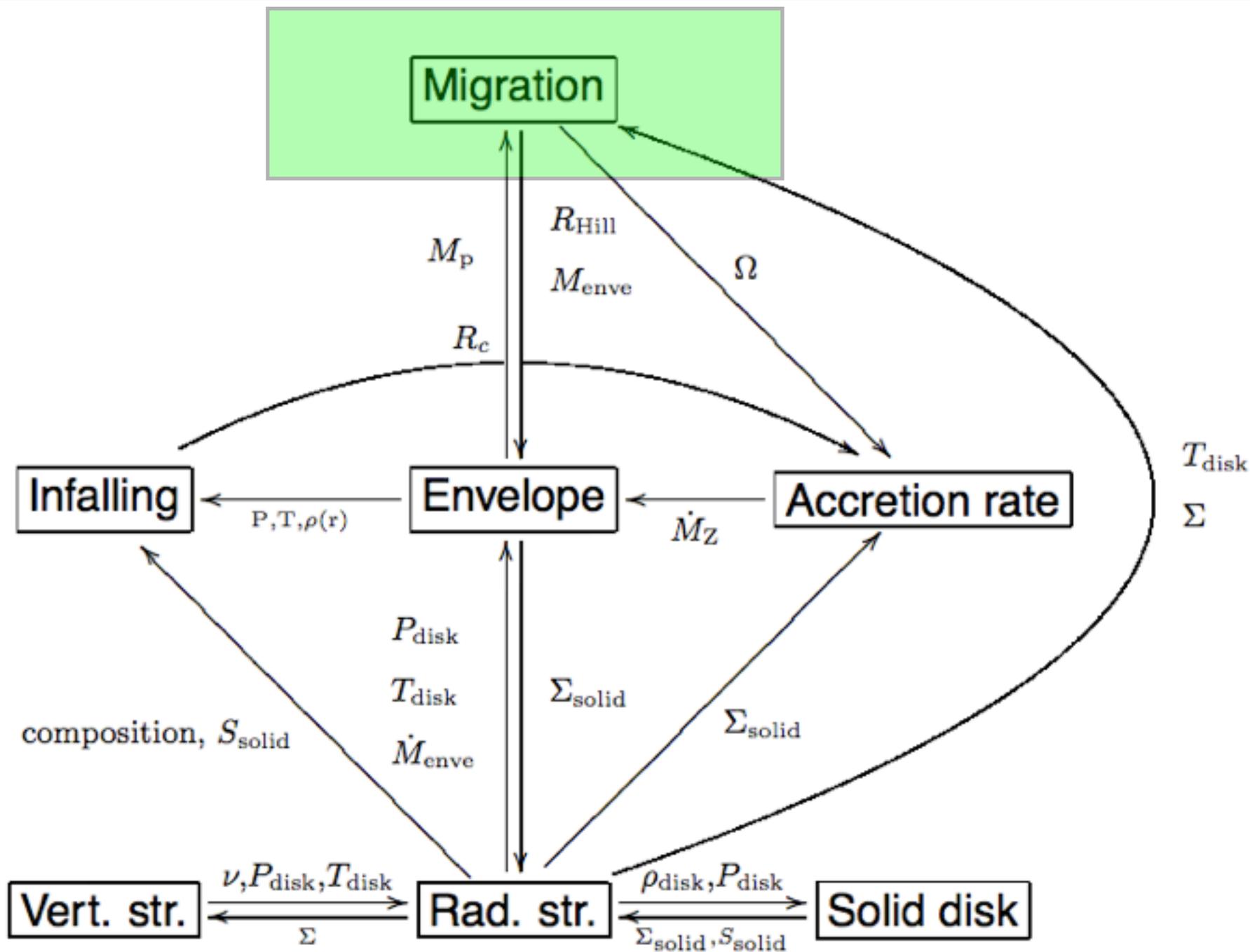


Planet migration path

# Disk model: planetesimals



# Models overview



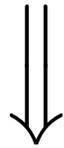
# Migration - type I

● Type I (low mass planets):  $R_{\text{Hill}} \equiv a_P \left( \frac{M_{\text{planet}}}{3M_{\text{star}}} \right)^{\frac{1}{3}} < H_{\text{disk}}$

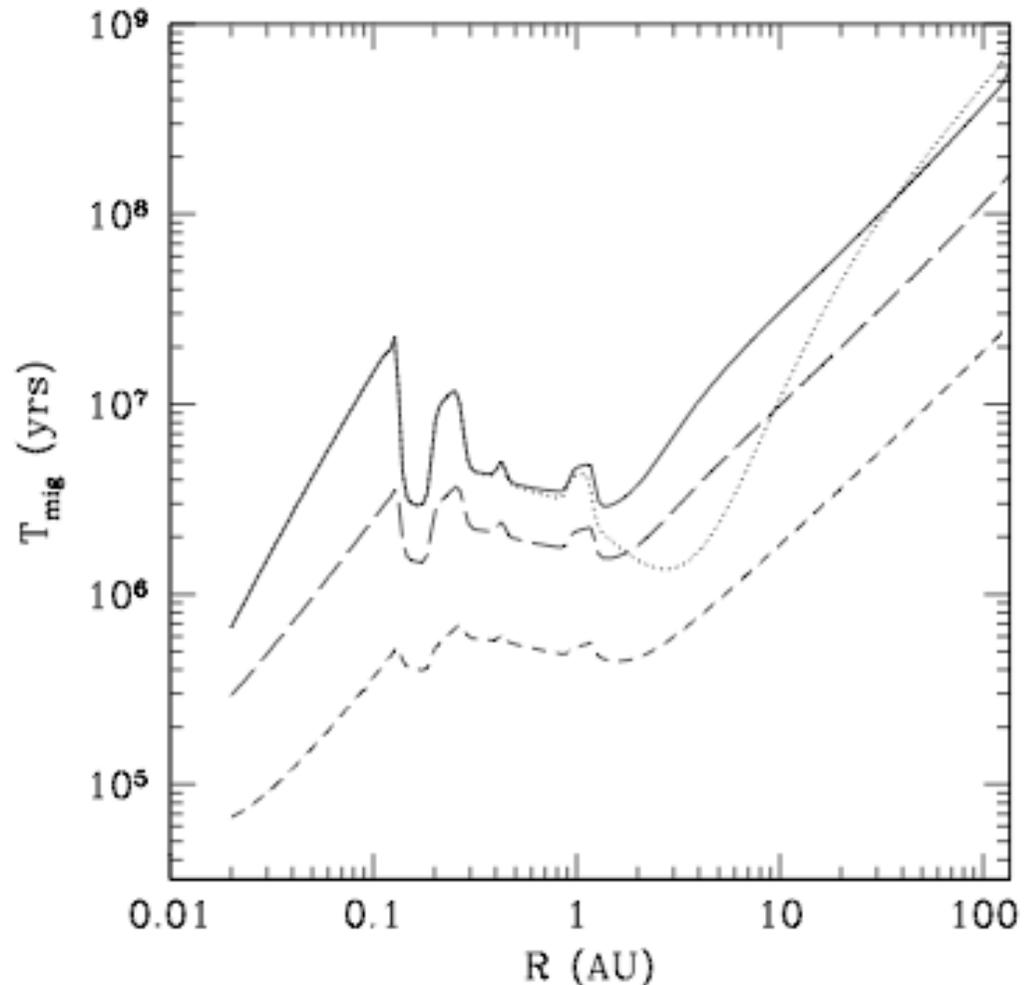
$$\frac{da_P}{dt} = f(\alpha_{\text{disk}}) \times \frac{M_{\text{planet}}}{M_{\text{star}}} \times \frac{\Sigma_P a_P^2}{M_{\text{star}}} \times \left( \frac{c_P}{a_P \Omega_P} \right)^2 \times \Omega_P^{-1} \quad \text{Tanaka, Takeuchi \& Ward 2002}$$

$$\alpha_{\text{disk}} \equiv \frac{d \ln \Sigma}{d \ln r}$$

Opacity transition regions

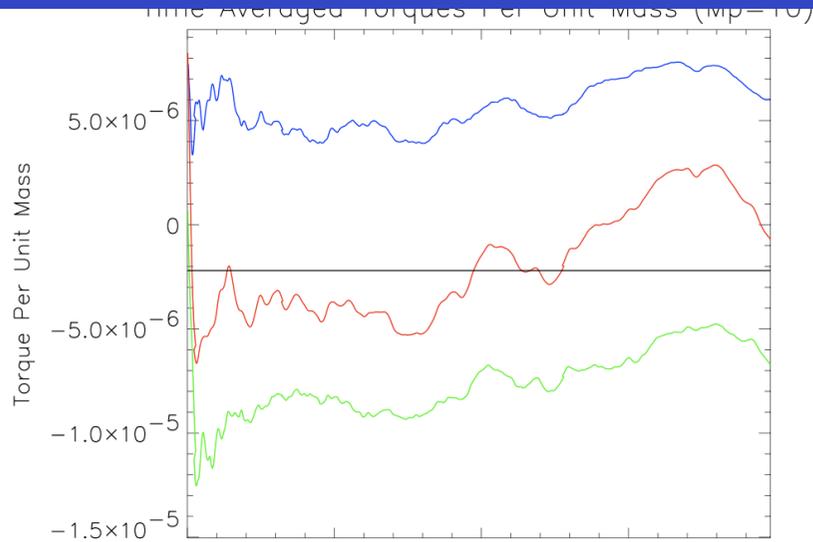


$$\alpha_{\text{disk,inside}} \neq \alpha_{\text{disk,outside}}$$

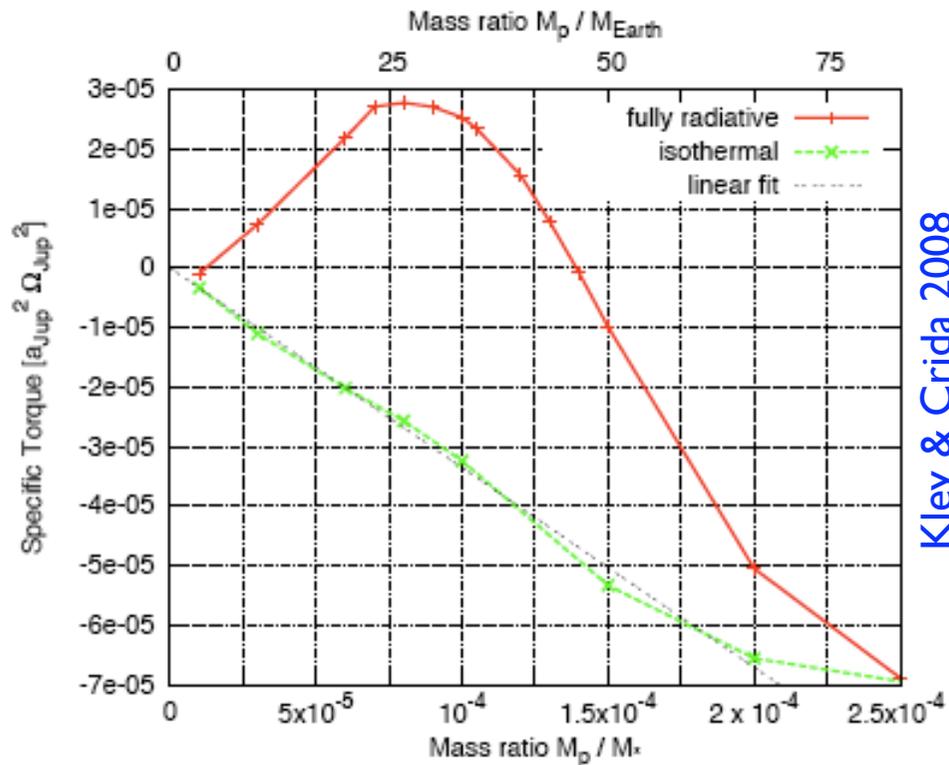


Menou & Goodman 2004

# Migration - type I

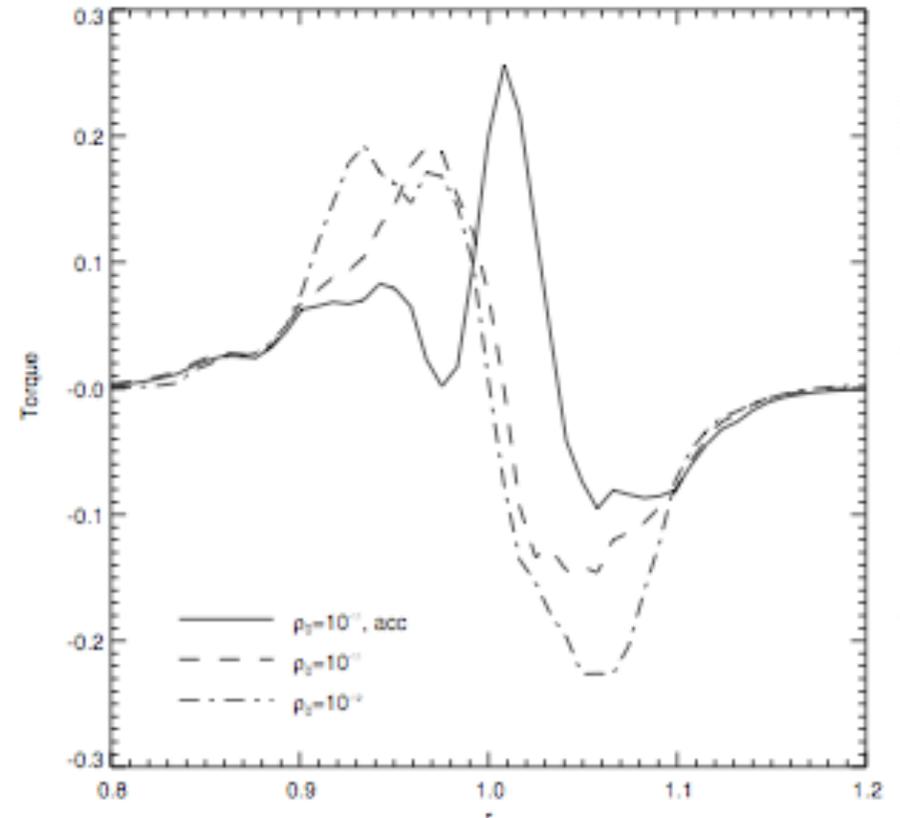


Nelson & Papaloizou 2003



Kley & Crida 2008

Density fluctuations  
 $\Downarrow$   
 "Random walk" migration



Paardekooper & Mellema 2007

Thermodynamic effects  $\implies$  Outward migration

# Migration - type I

● Type I (low mass planets):

$$\frac{da_{\text{planet}}}{dt} = f_{\text{I}} \left( \frac{da_{\text{planet}}}{dt} \right) \text{linear}$$

Tanaka, Takeuchi & Ward 2002

0 to 1



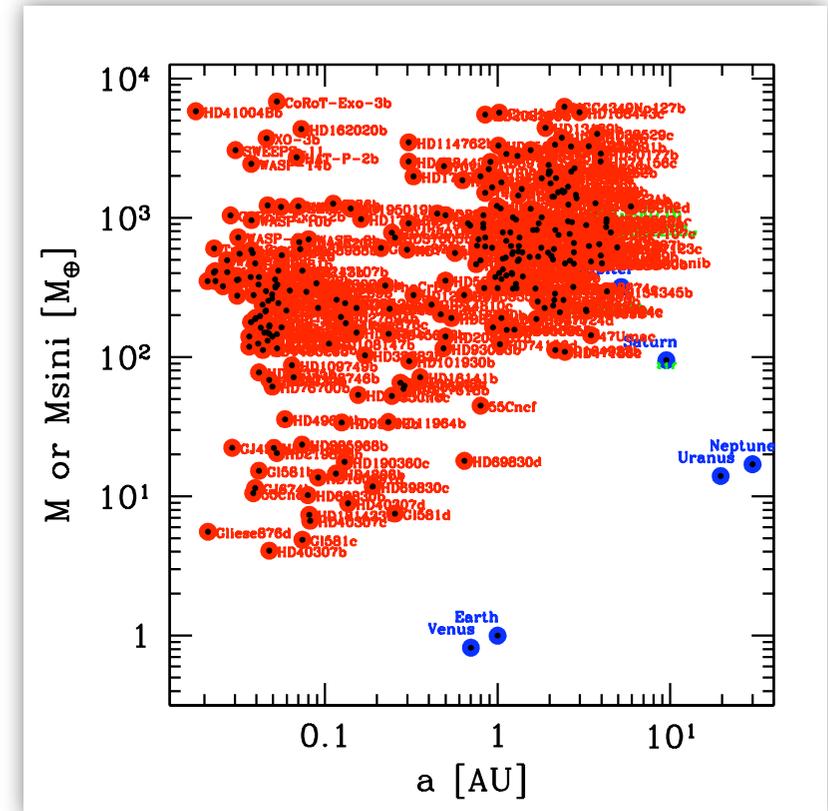
# Extrasolar planets

● Huge diversity resulting probably from different ICs:

- Protoplanetary disk
- Metallicity
- Environment

● To explain the observations, need to take into account

- 1) the ICs, with the correct probability laws
- 2) the observational biases



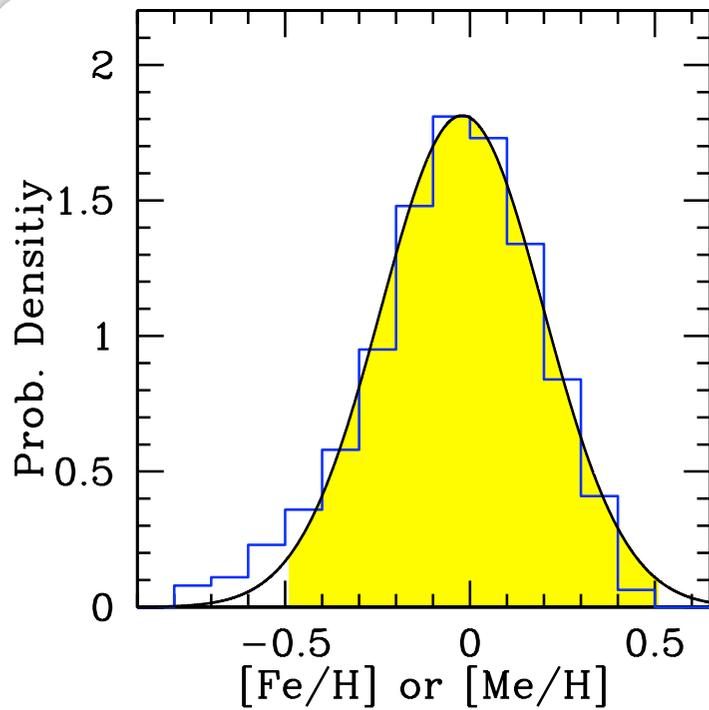
⇒ Monte-Carlo approach

# Initial conditions

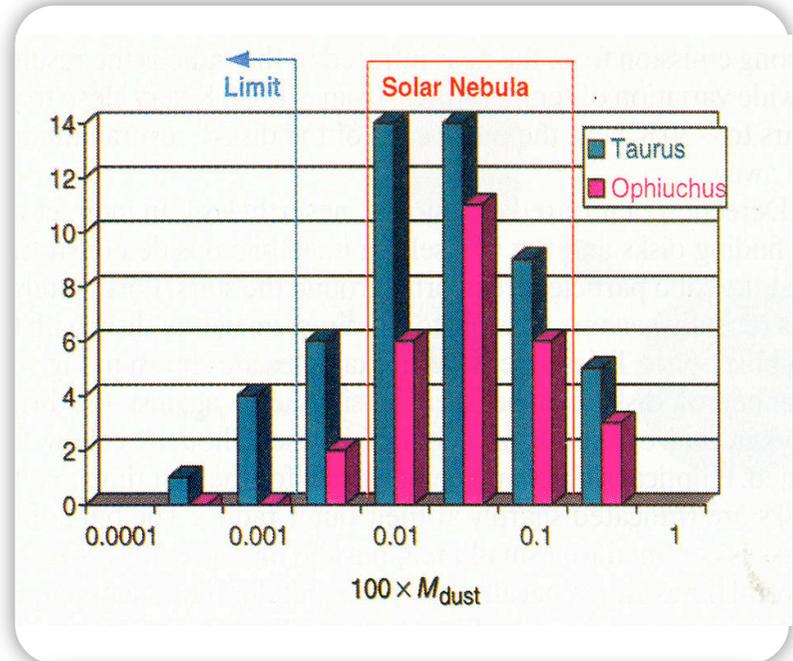
CORALIE survey



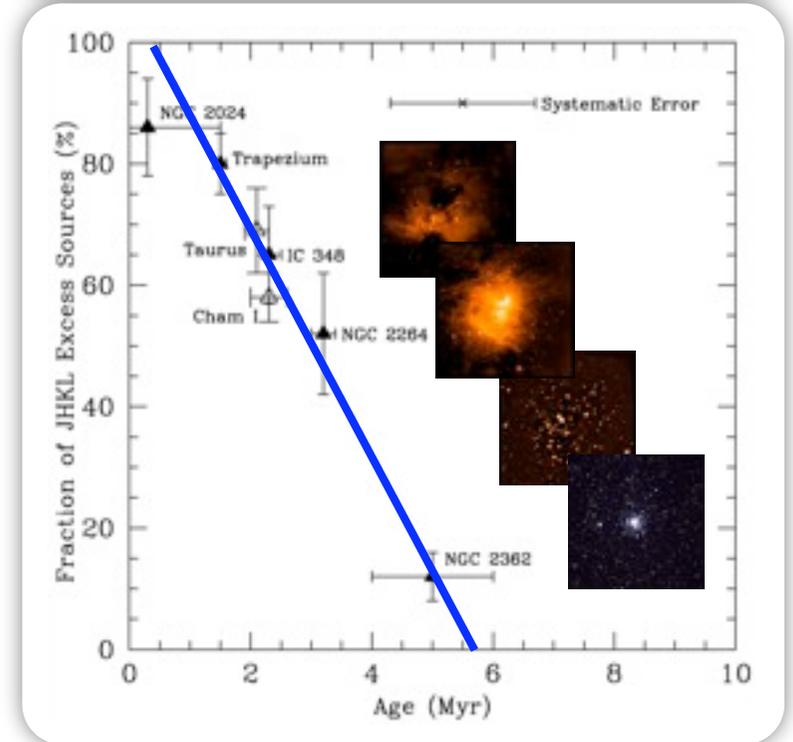
gaussian  
repartition



Santos et al. 2003

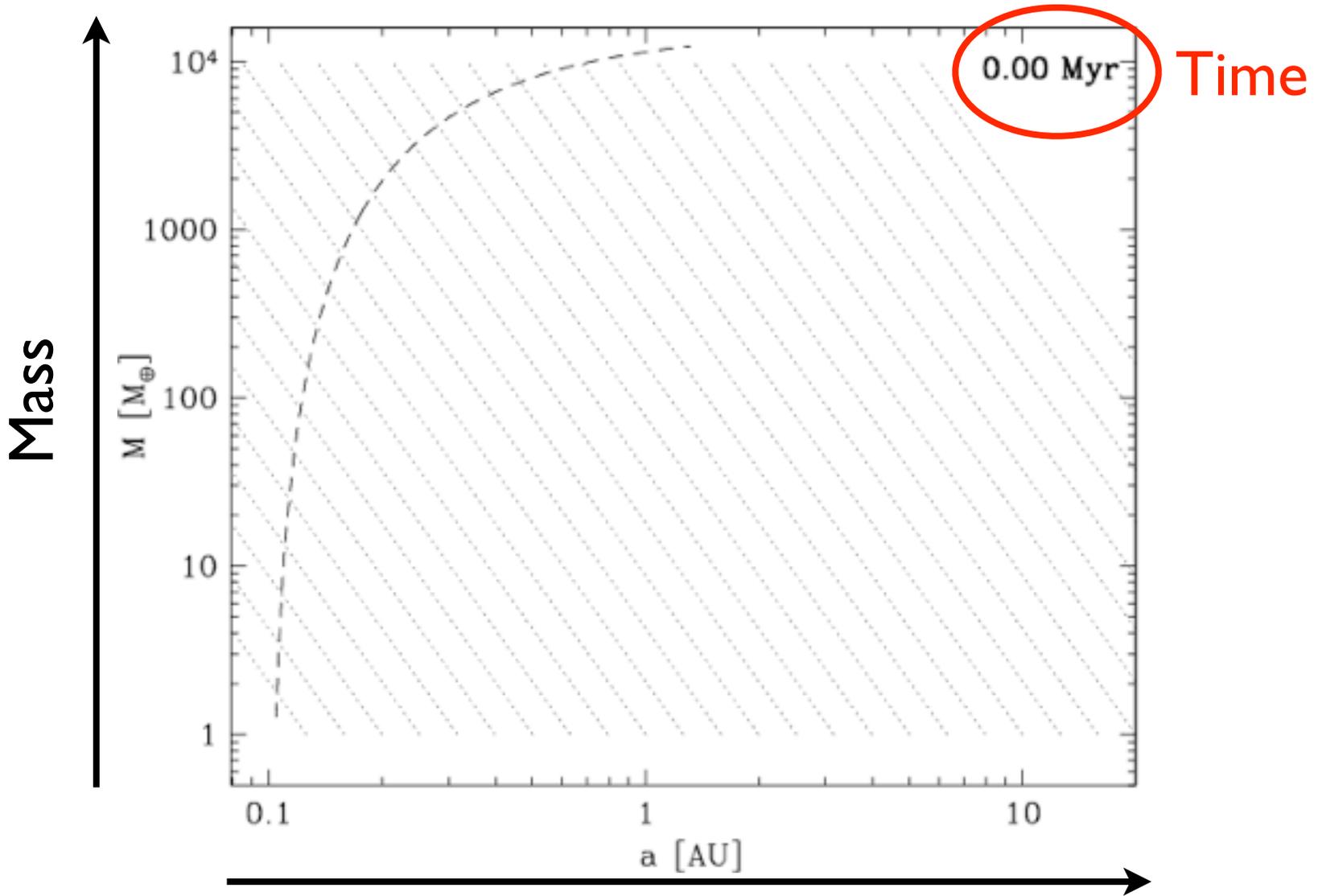


Beckwith & Sargent



Haisch et al. 2001

# Evolutionary tracks: the full population

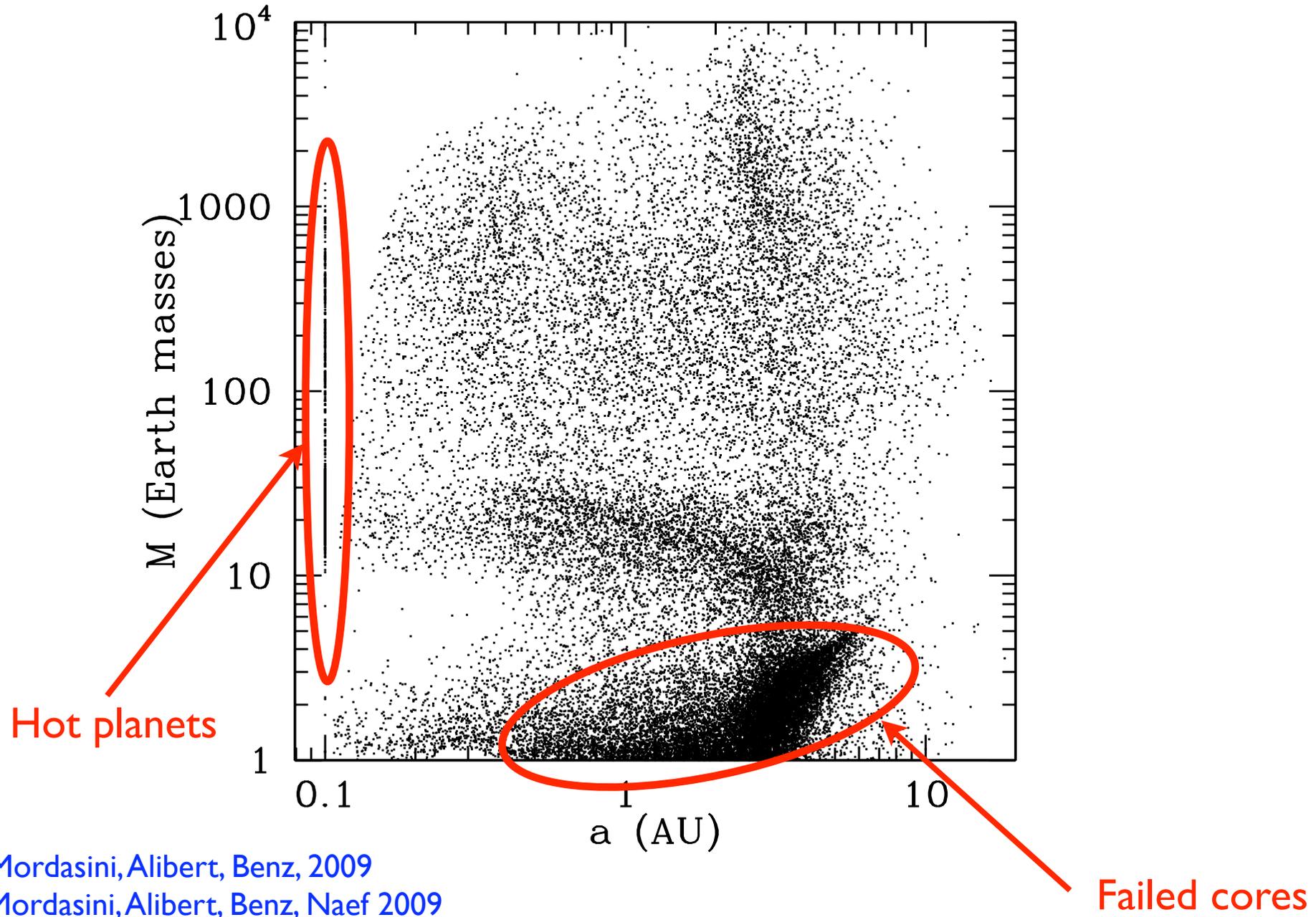


Mordasini, Alibert, Benz, 2009

Mordasini, Alibert, Benz, Naef 2009

Semi-major axis

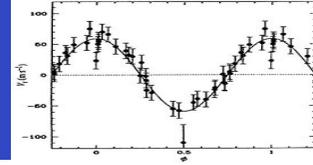
# Theoretical population



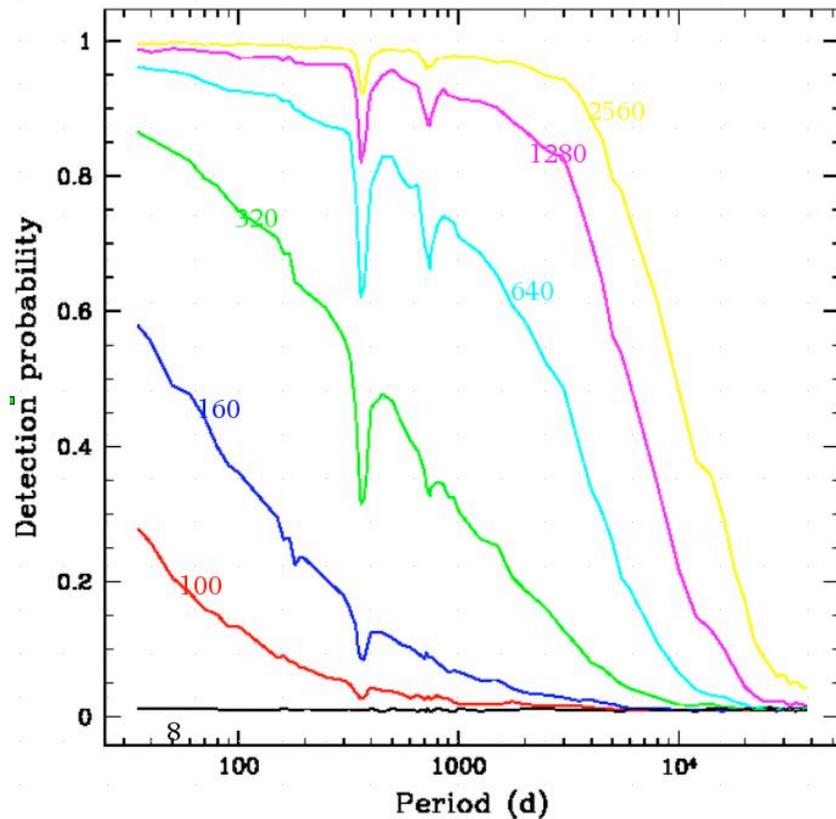
Mordasini, Alibert, Benz, 2009

Mordasini, Alibert, Benz, Naef 2009

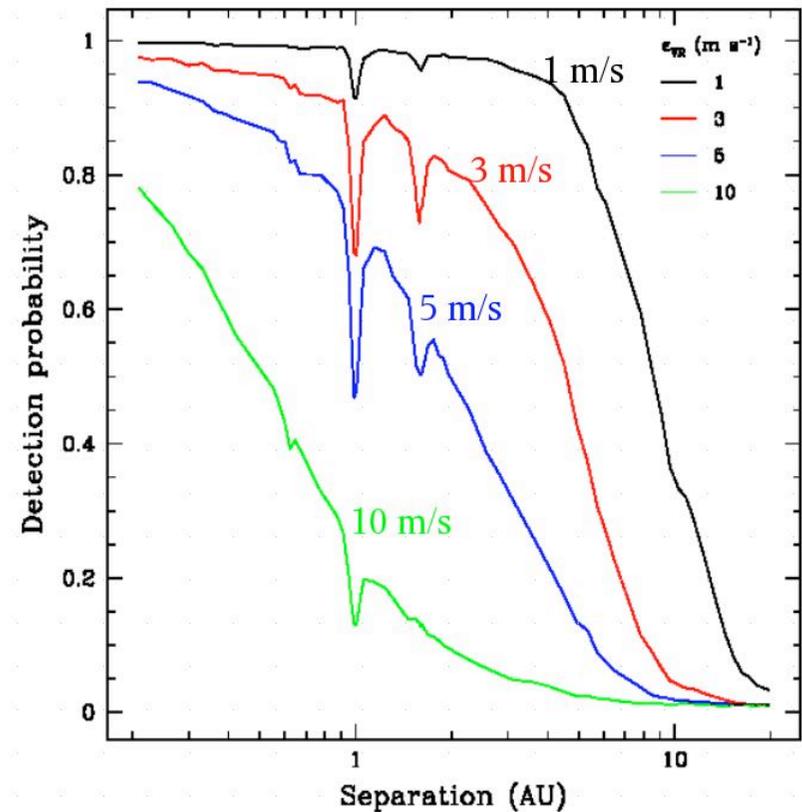
# Bias (radial velocities)



Elodie

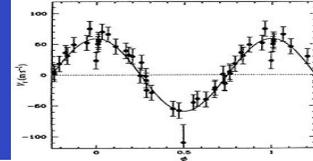


1 M<sub>J</sub>



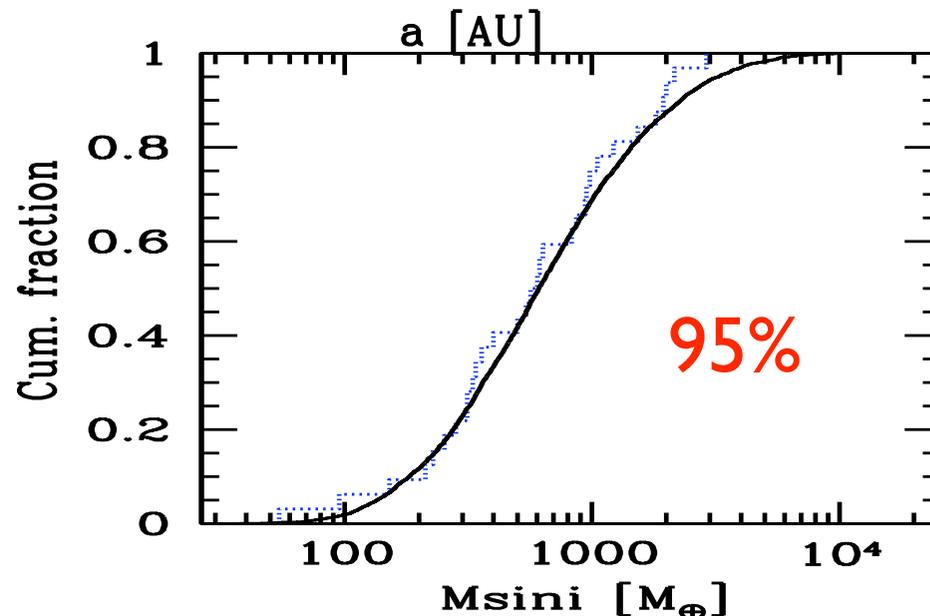
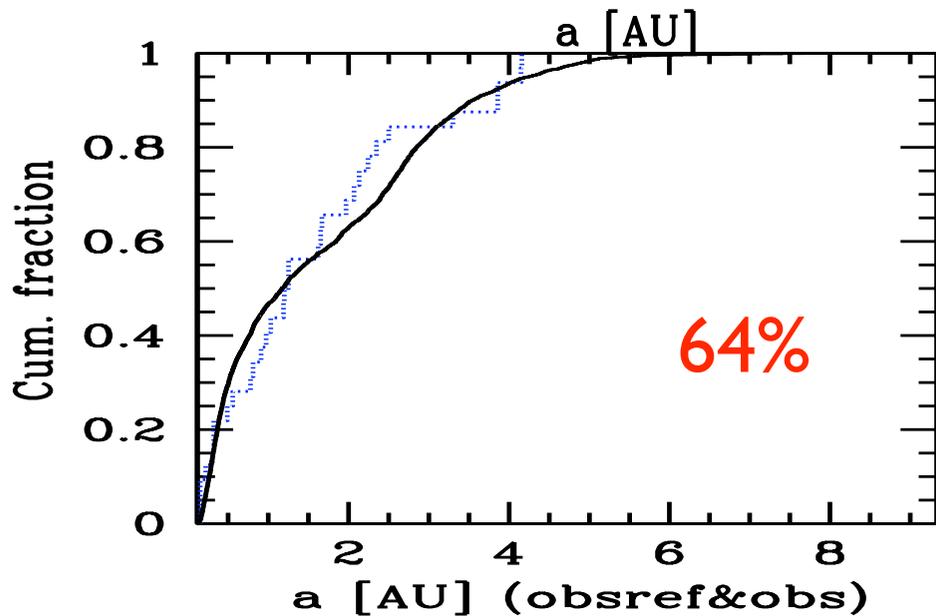
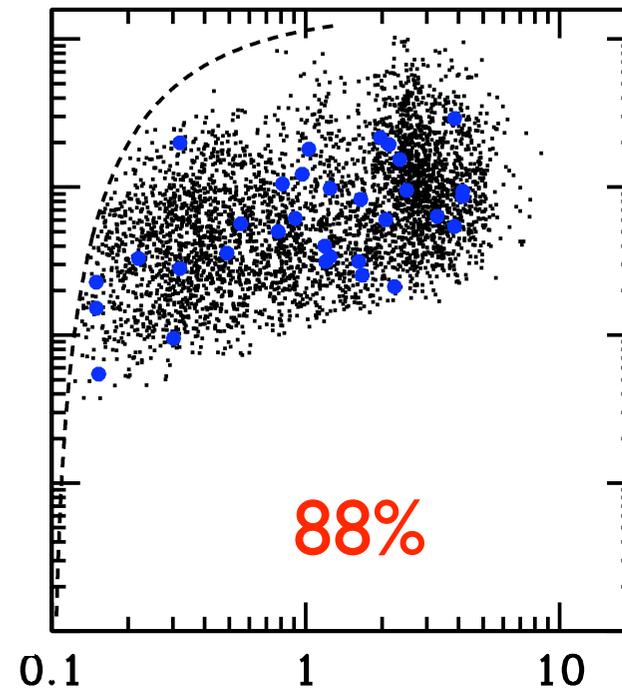
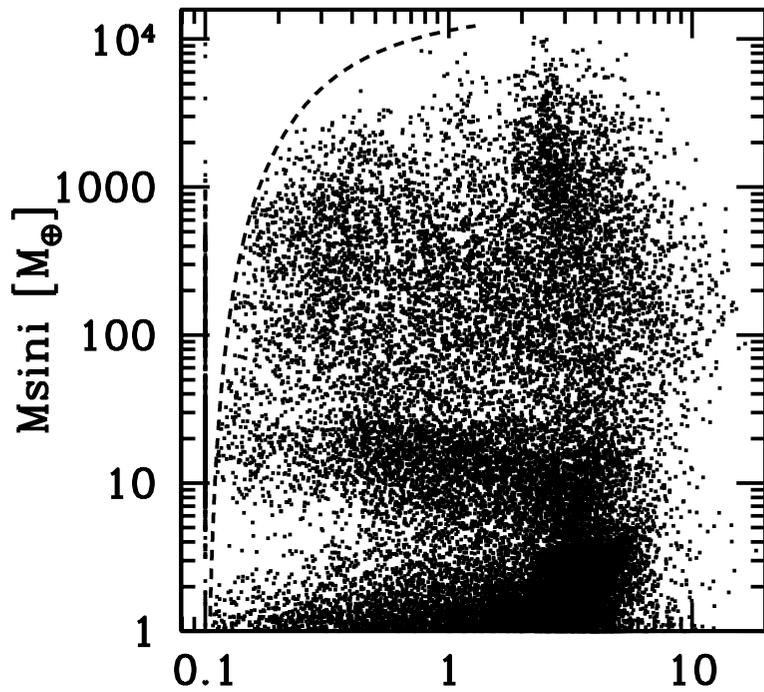
Monte-Carlo simulations by D. Naef  
eccentricity, mass, period, observation schedule...  
➡ **observational bias**

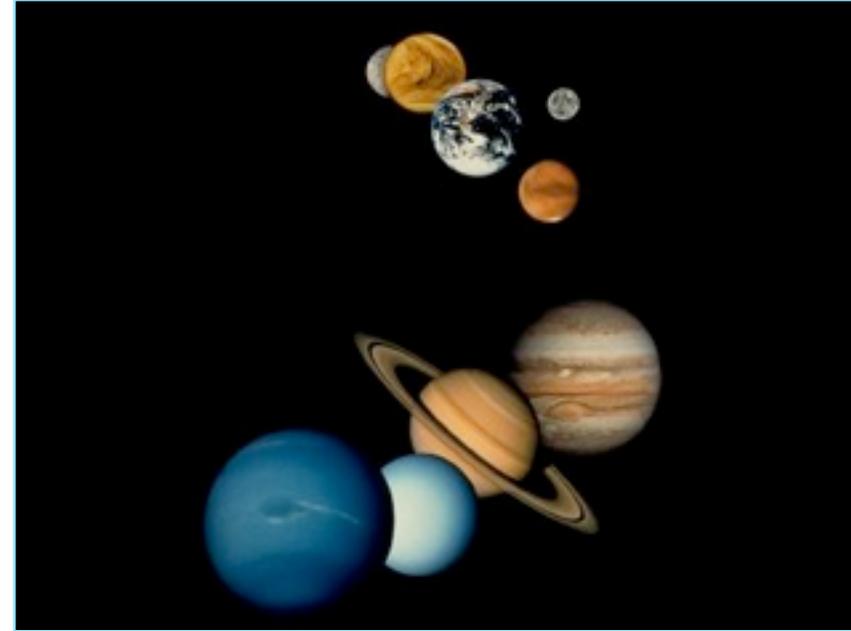
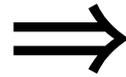
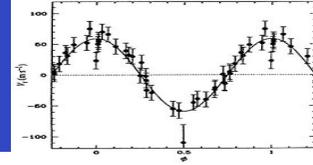
# M sin(i) vs a



all

10 m/s



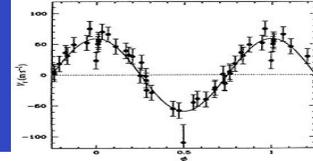


an “observed” disk...

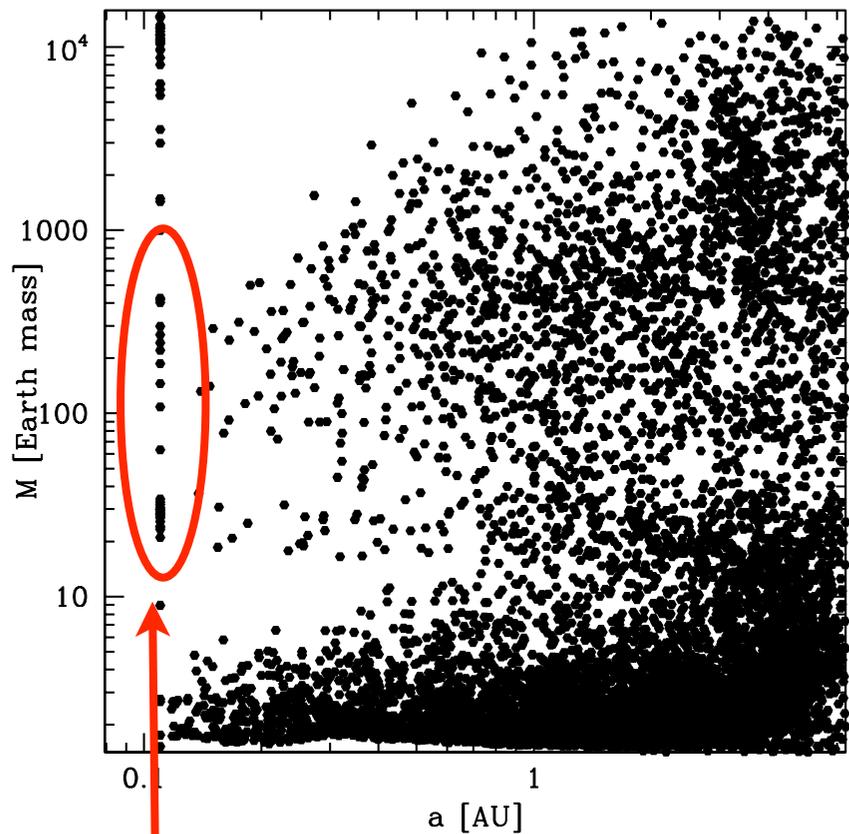
- ⇒⇒ Disk lifetime ?
- ⇒⇒ Disk mass ?
- ⇒⇒ Heating sources ?
- ⇒⇒ SED and evolution ?

Consequences on  
planetary population

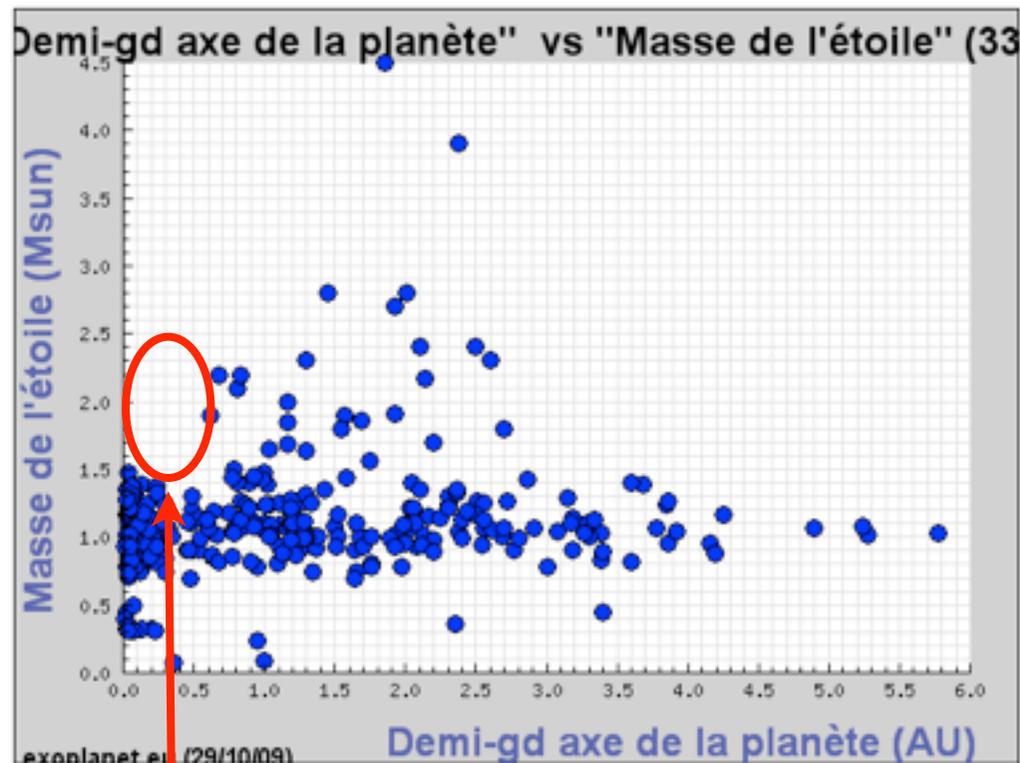
# Disk lifetime ?



2.0 Msun



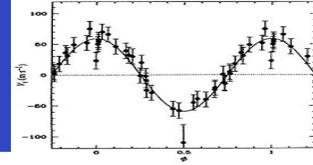
Hot Planets  
around massive stars



No observed hot planets around stars  $> 1.5 M_{\text{sun}}$   
disk lifetime effect ? (e.g. Johnson et al. 2007)

Alibert, Mordasini, Benz, in prep

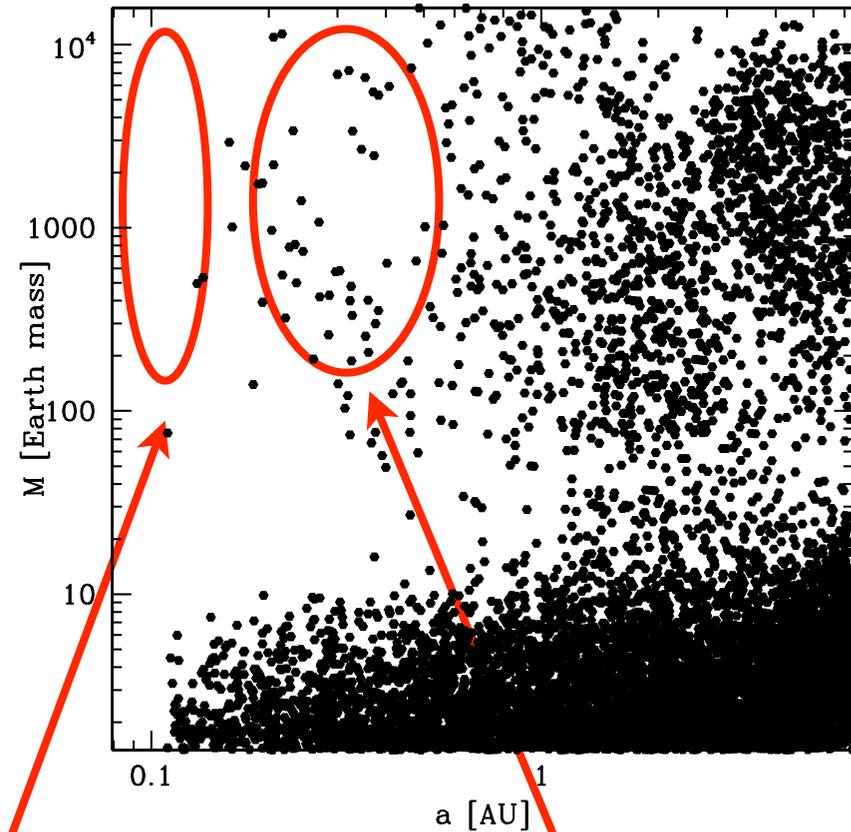
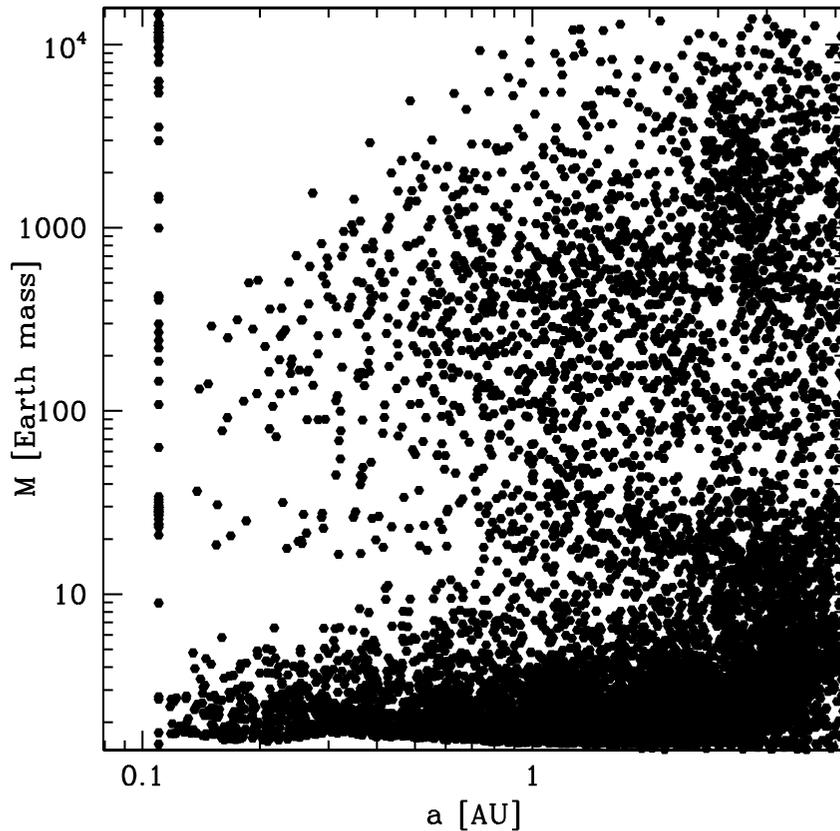
# Disk lifetime ?



$$T_{\text{disk}} \propto M_{\text{star}}^0$$

$$T_{\text{disk}} \propto M_{\text{star}}^{-1/2} \quad \text{for } M > 1.5M_{\odot}$$

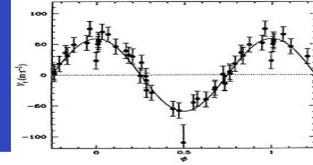
Kennedy & Kenyon (2009)



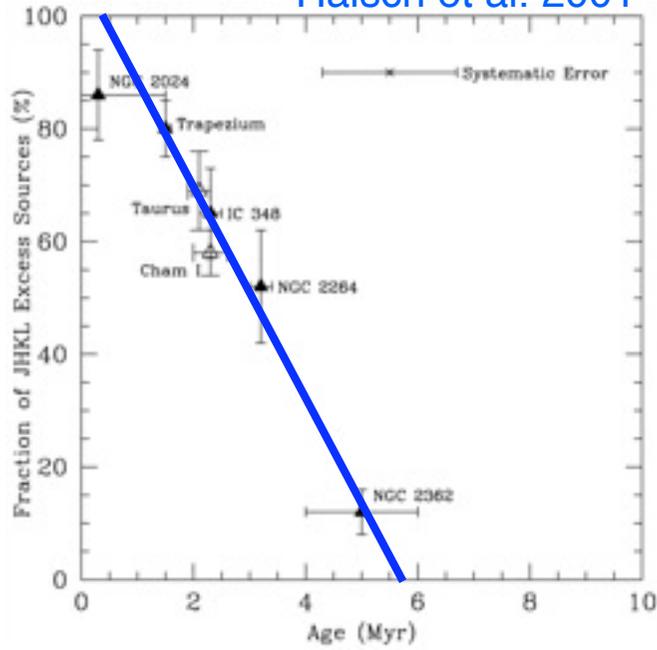
no Hot Planets

few warm planets  
statistical comparison with obs ?

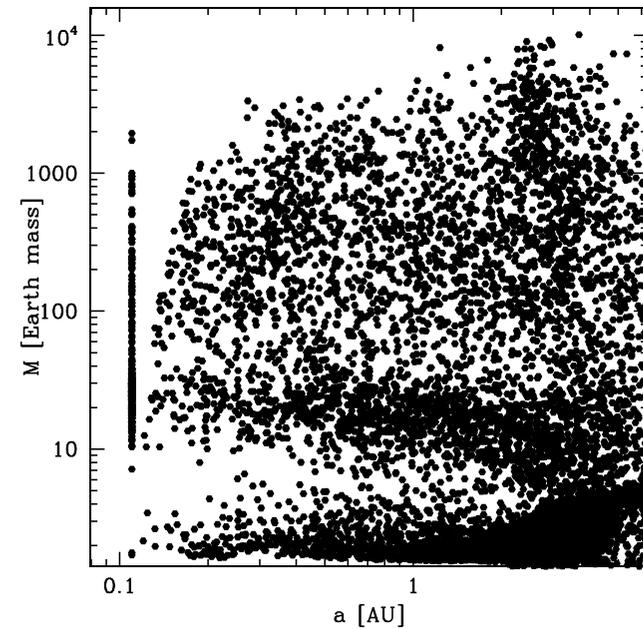
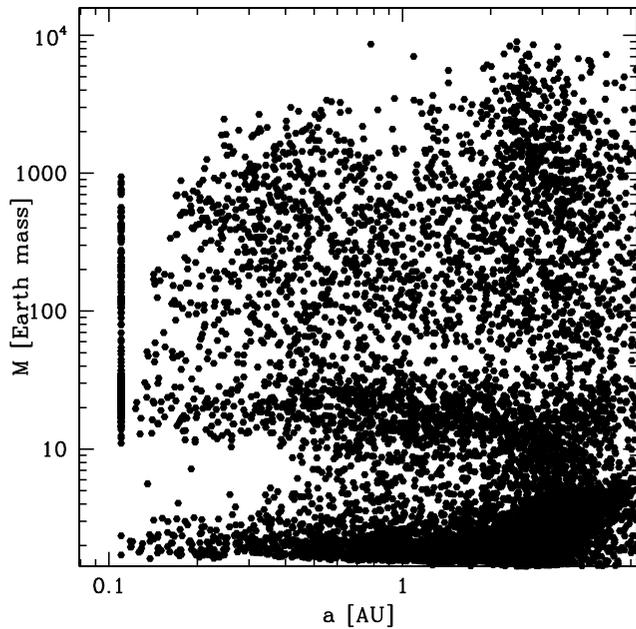
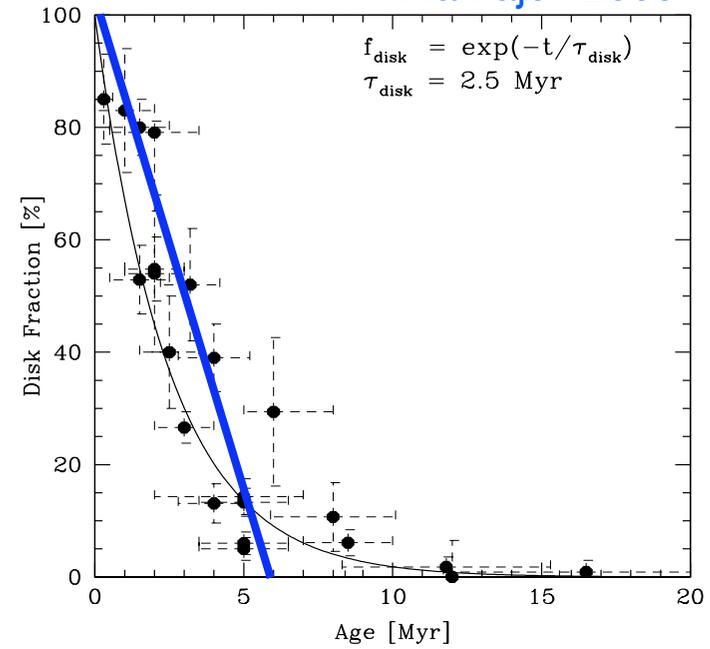
# Disk lifetime ?



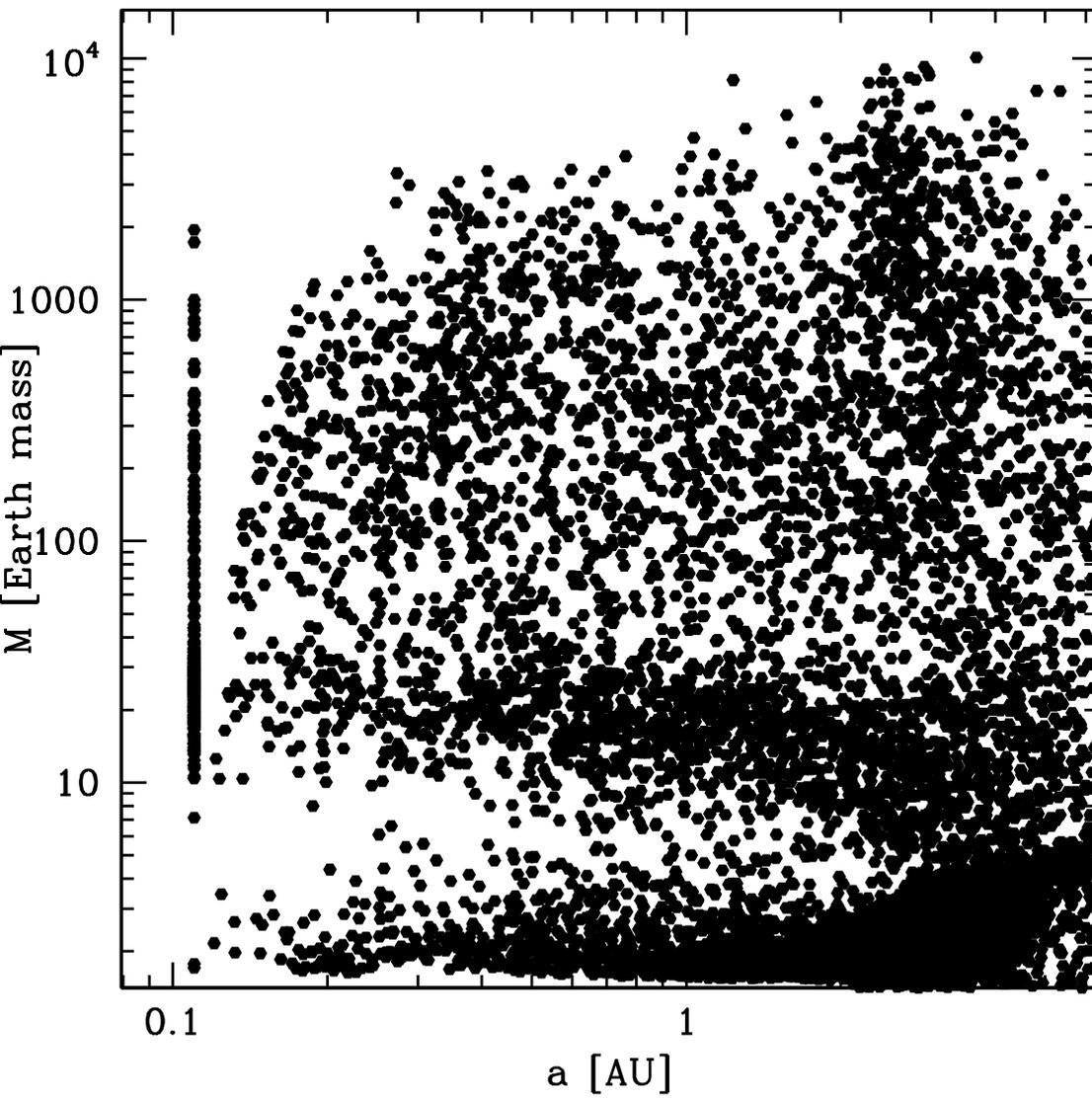
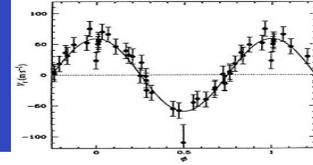
Haisch et al. 2001



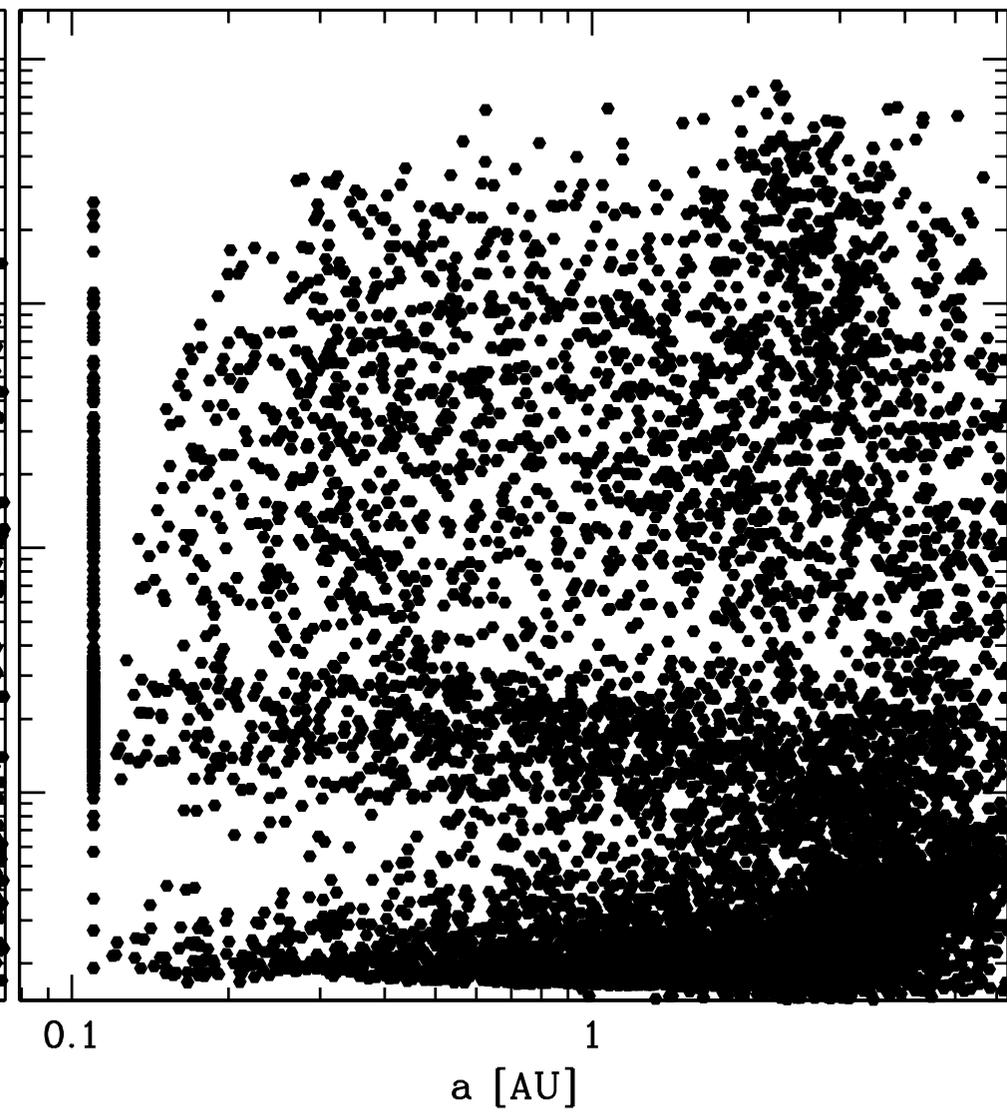
Mamajek 2009



# Disk lifetime ?

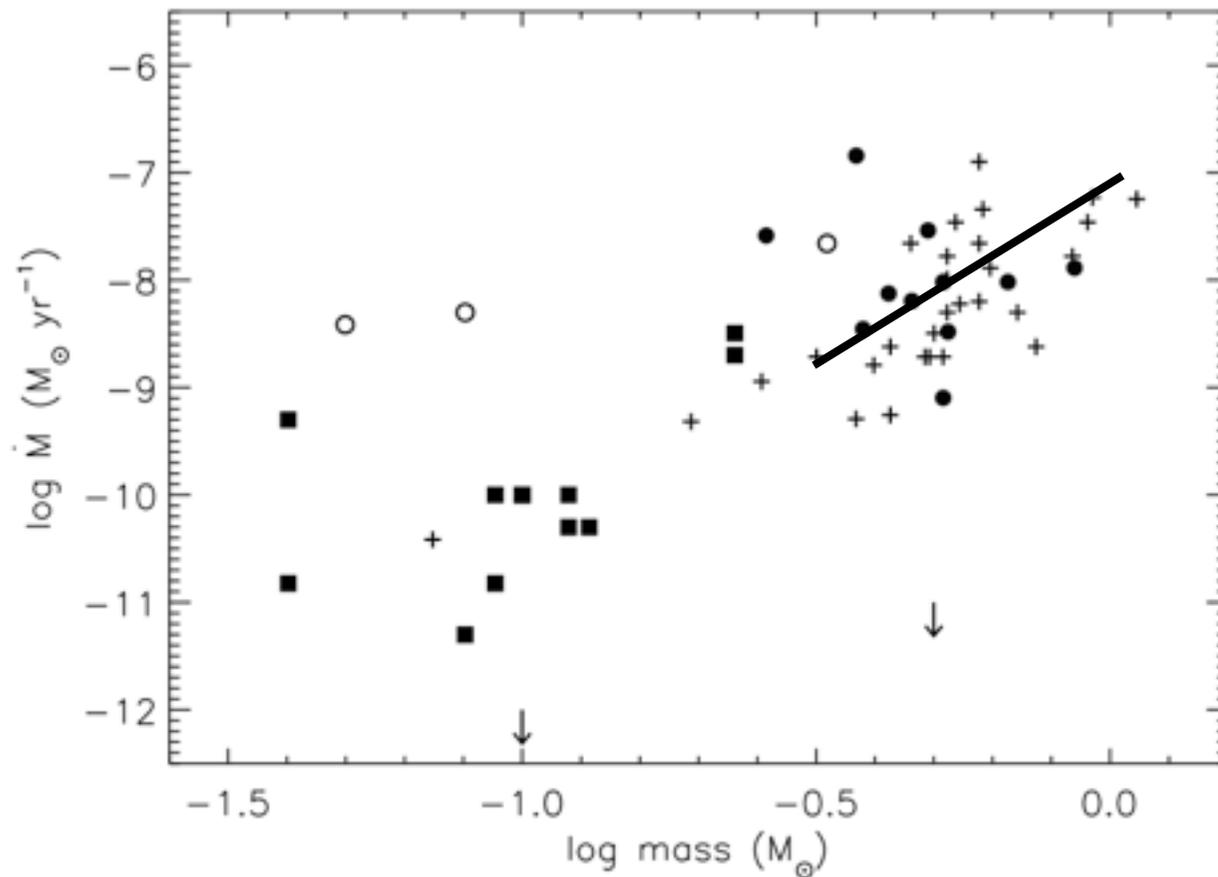
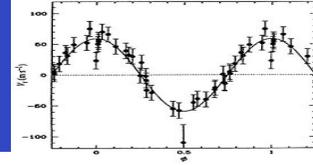


With correlation



Without correlation

# Disk mass ?



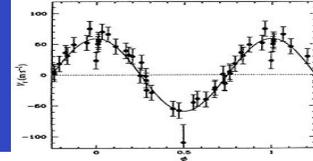
Muzerolle et al. 2003

assume  $M_{\text{disk}} \propto M_{\text{star}}^{\alpha_D}$

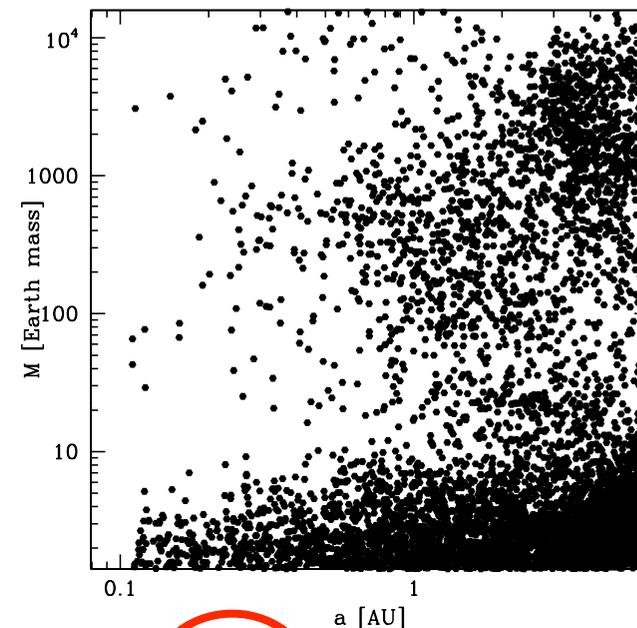
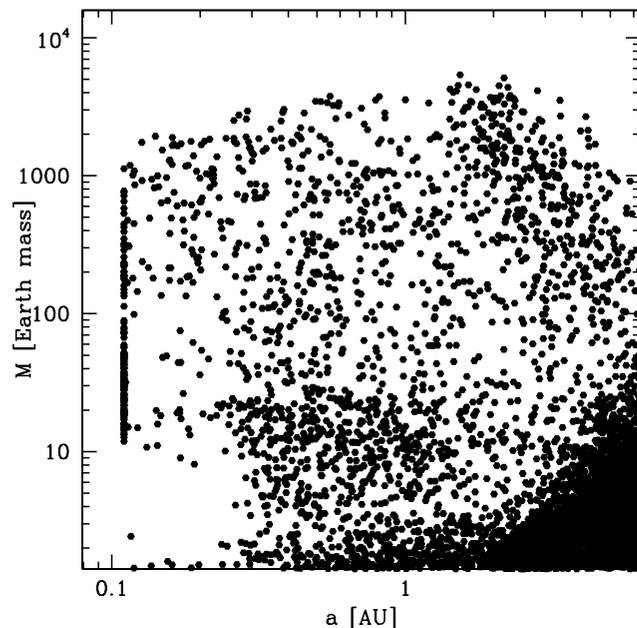
$\alpha_D$  adjusted to reproduce the  $M_{\text{disk}}$  versus  $M_{\text{star}}$  relation

**!! see also dependance of the active zone with Mstar !!**

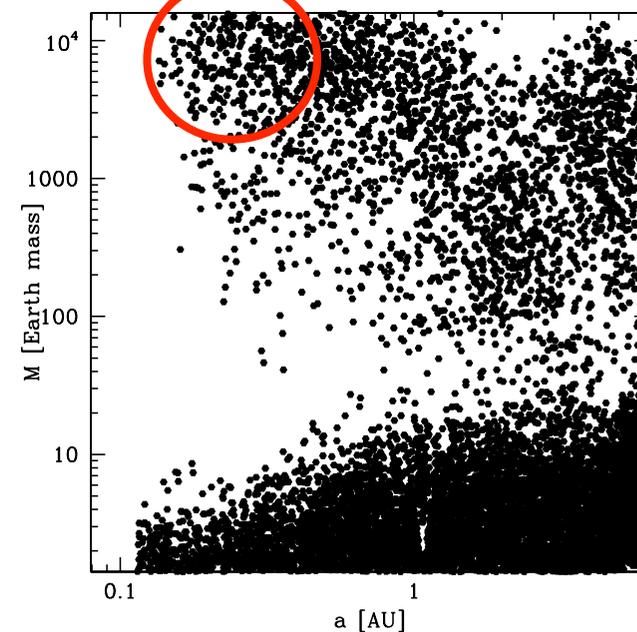
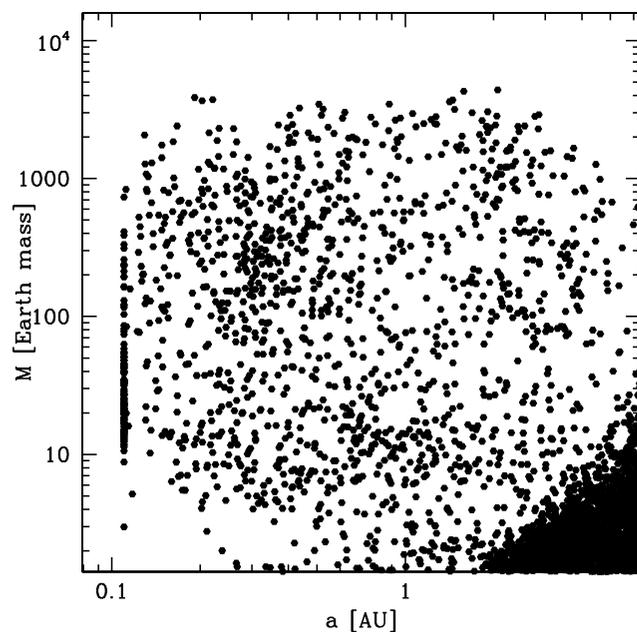
# Disk mass ?



$$M_{\text{disk}} \propto M_{\text{star}}^0$$



$$M_{\text{disk}} \propto M_{\text{star}}^2$$

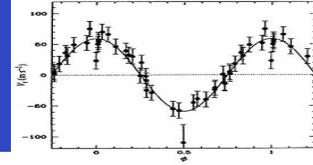


Alibert, Mordasini, Benz, in prep

0.5  $M_{\text{sun}}$

2.0  $M_{\text{sun}}$

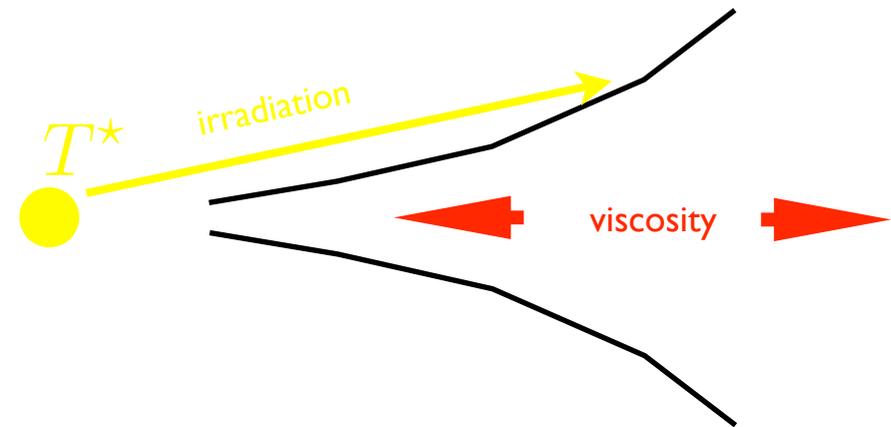
# Heating sources ?



## Heating sources

### 1) viscous heating

$$\Gamma_{\text{visc}} = \frac{9}{4} \rho \nu \Omega^2$$



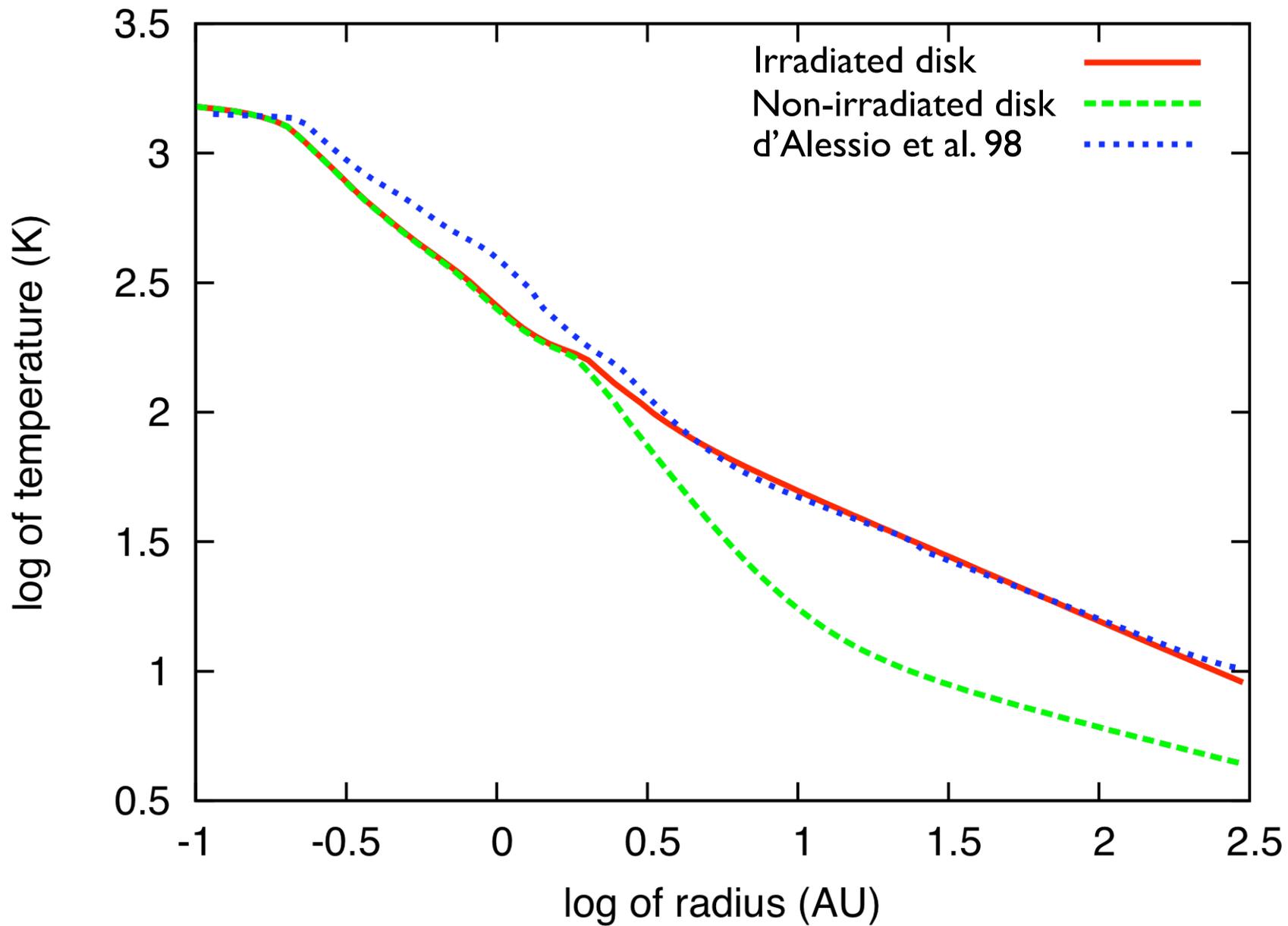
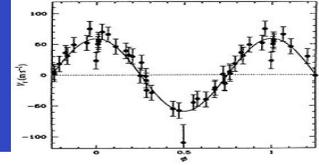
### 2) irradiation

$$T_{\text{irr}} = T_{\star} \left[ \frac{2}{3\pi} \left( \frac{R_{\star}}{r} \right)^3 + \frac{1}{2} \left( \frac{R_{\star}}{r} \right)^2 \left( \frac{H}{r} \right) \left( \frac{d \ln H}{d \ln r} - 1 \right) \right]^{1/4}$$

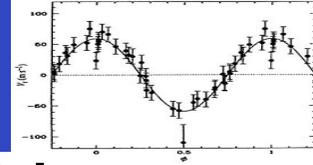
eq. value: 9/7

irradiation flux added to the surface flux (due to mass accretion)

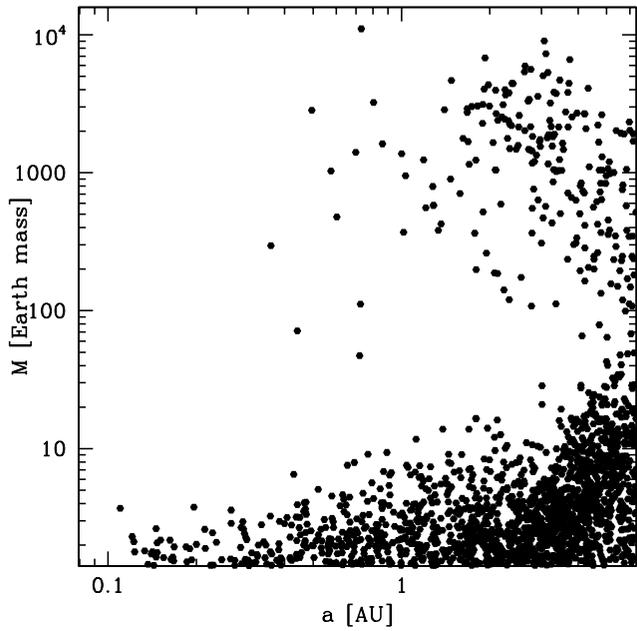
# Heating sources ?



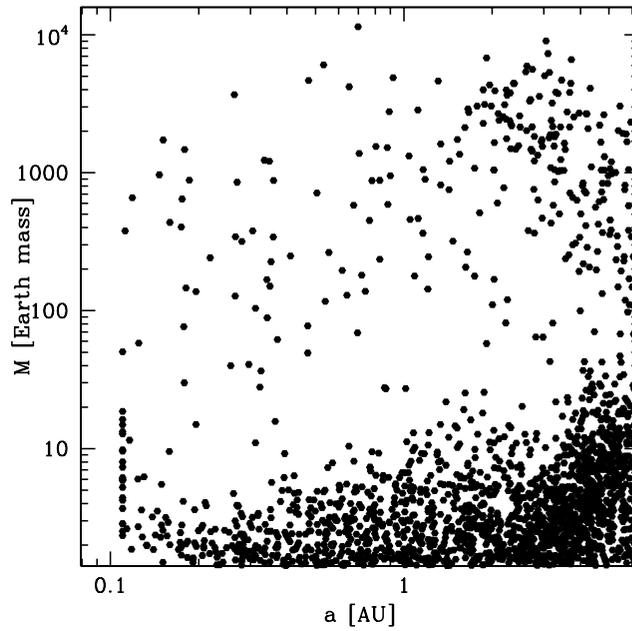
# Heating sources ?



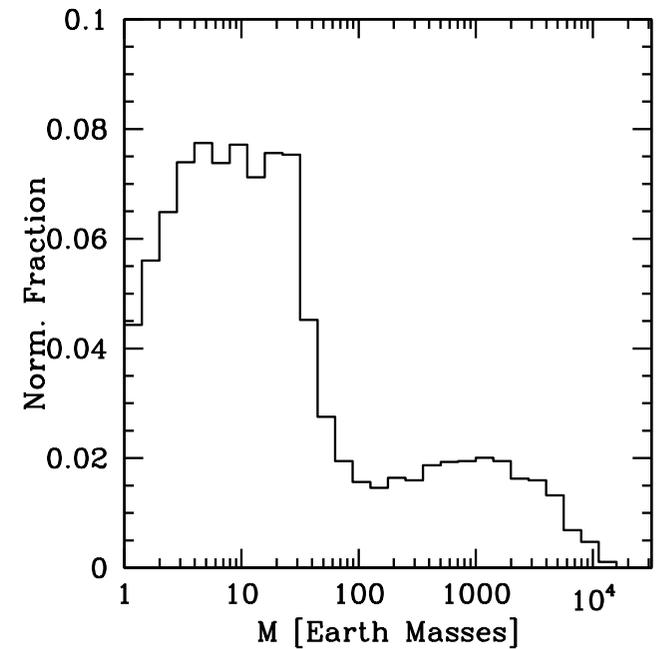
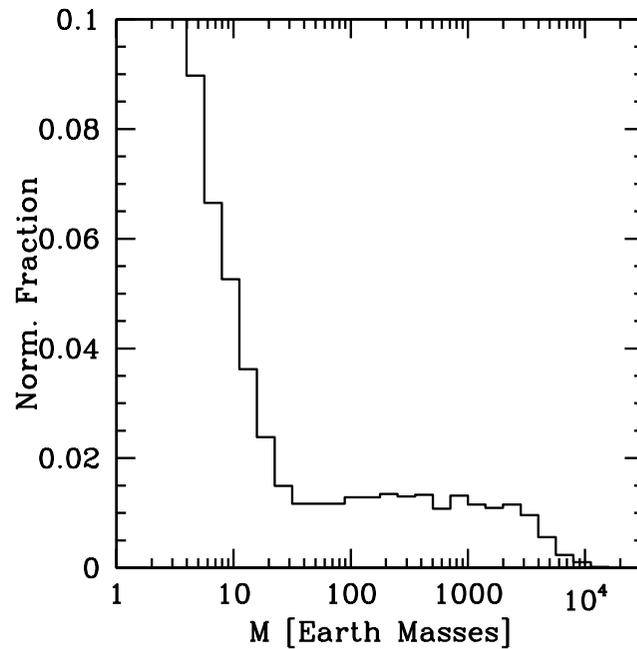
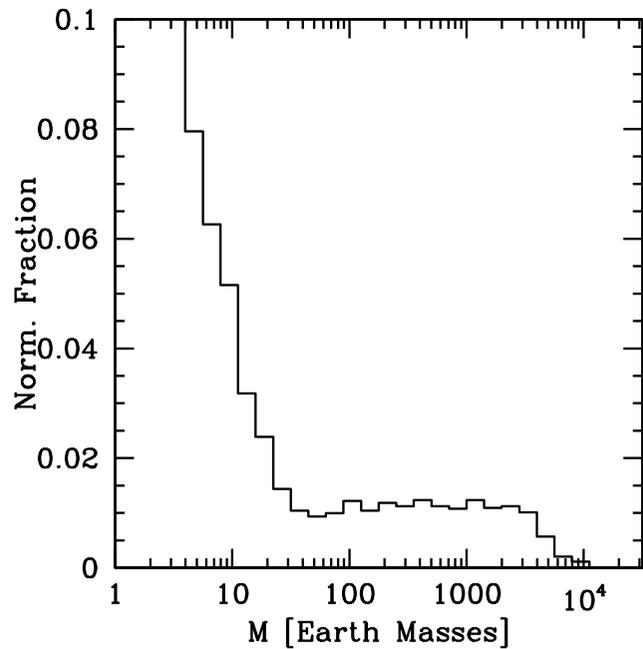
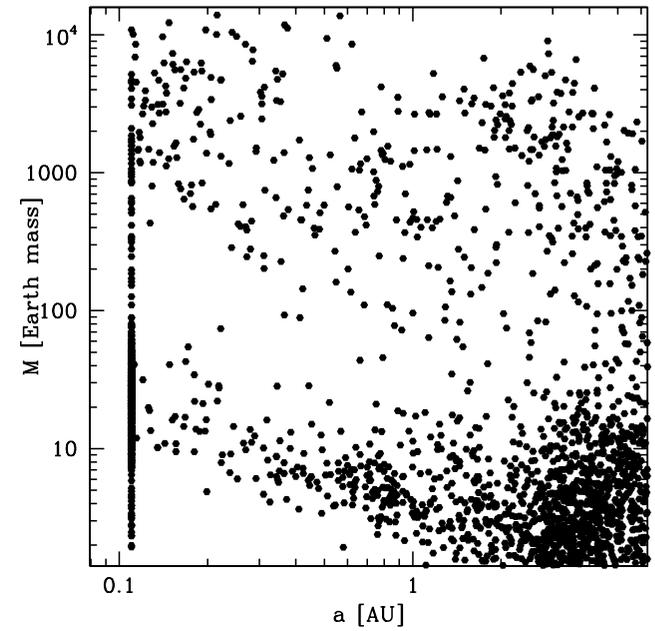
$f_l = 0.001$



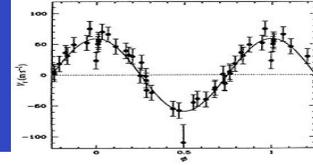
$f_l = 0.01$



$f_l = 0.1$

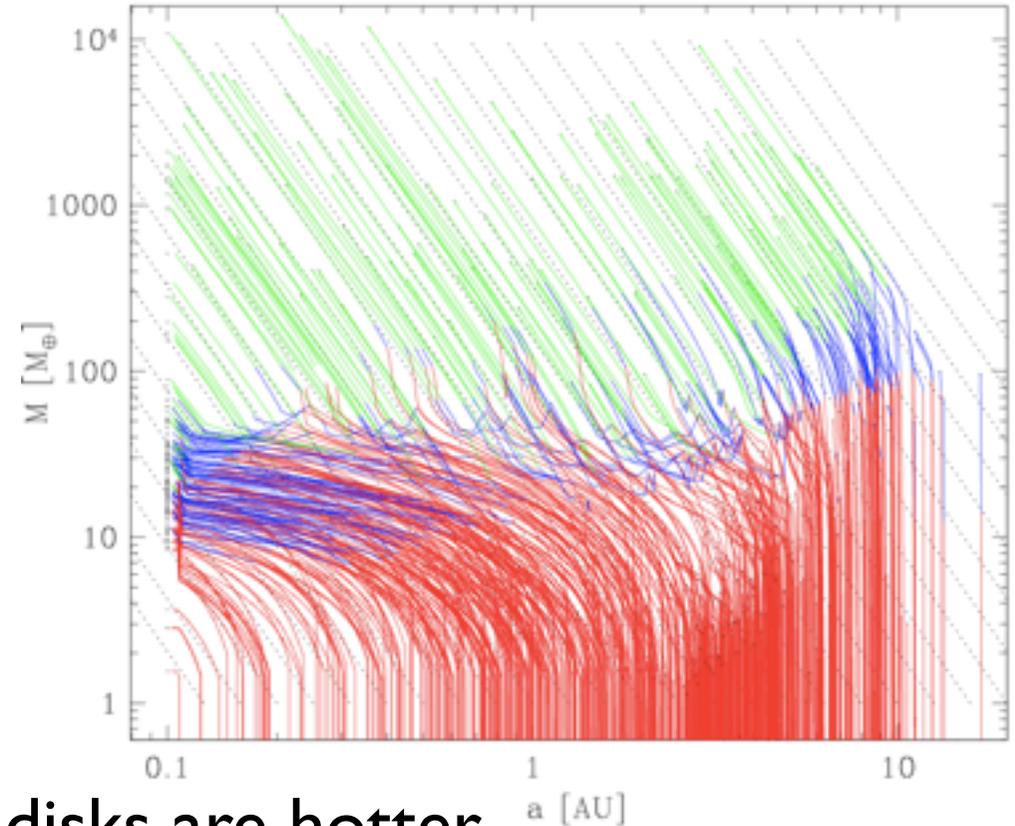
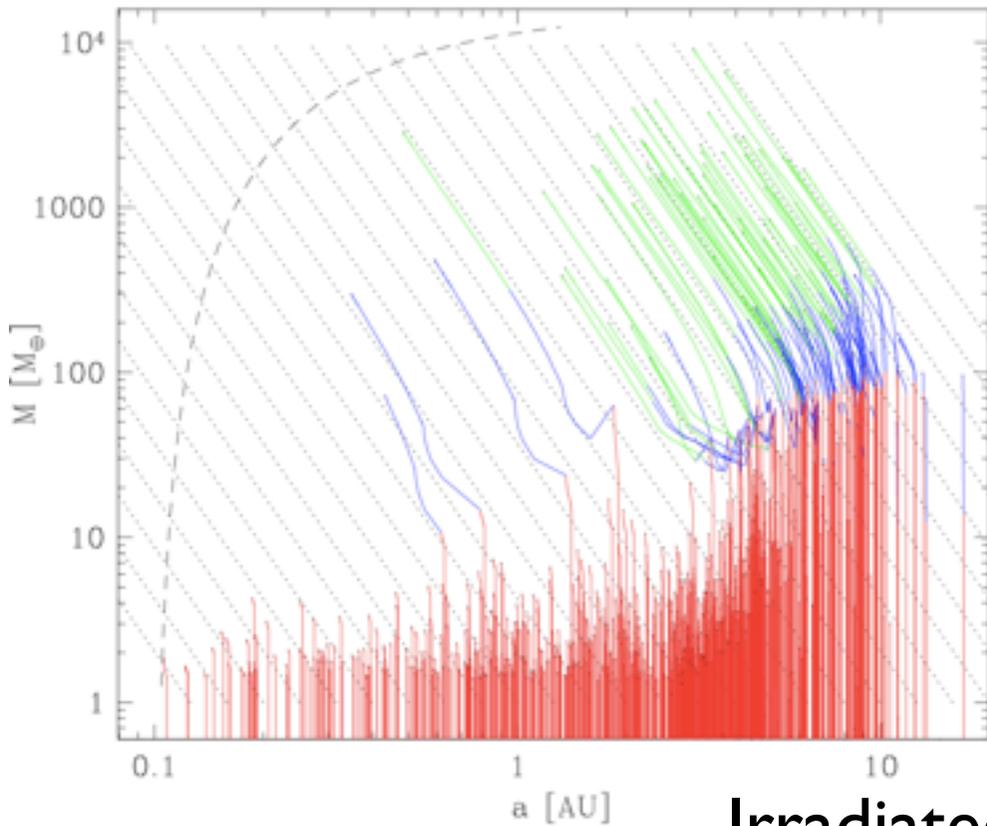


# Heating sources ?



$fI=0.001$

$fI=0.1$



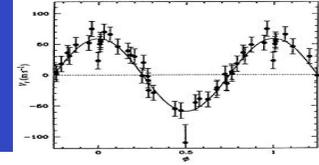
Irradiated disks are hotter

H/R larger than non irradiated

type II for larger masses

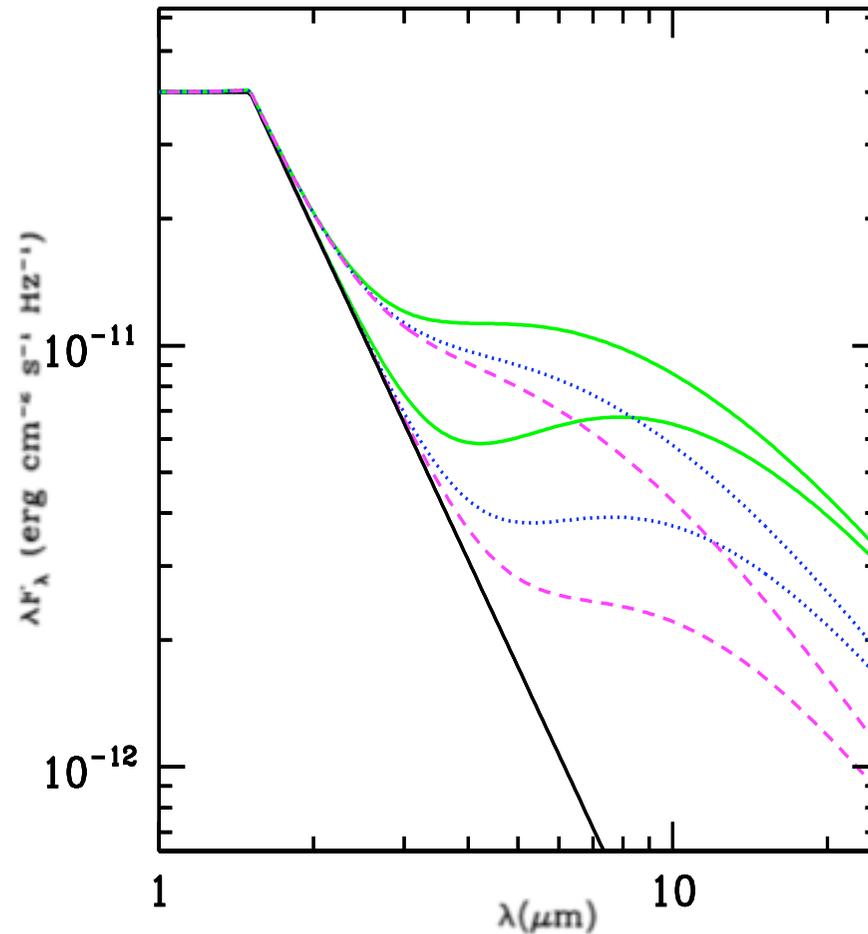
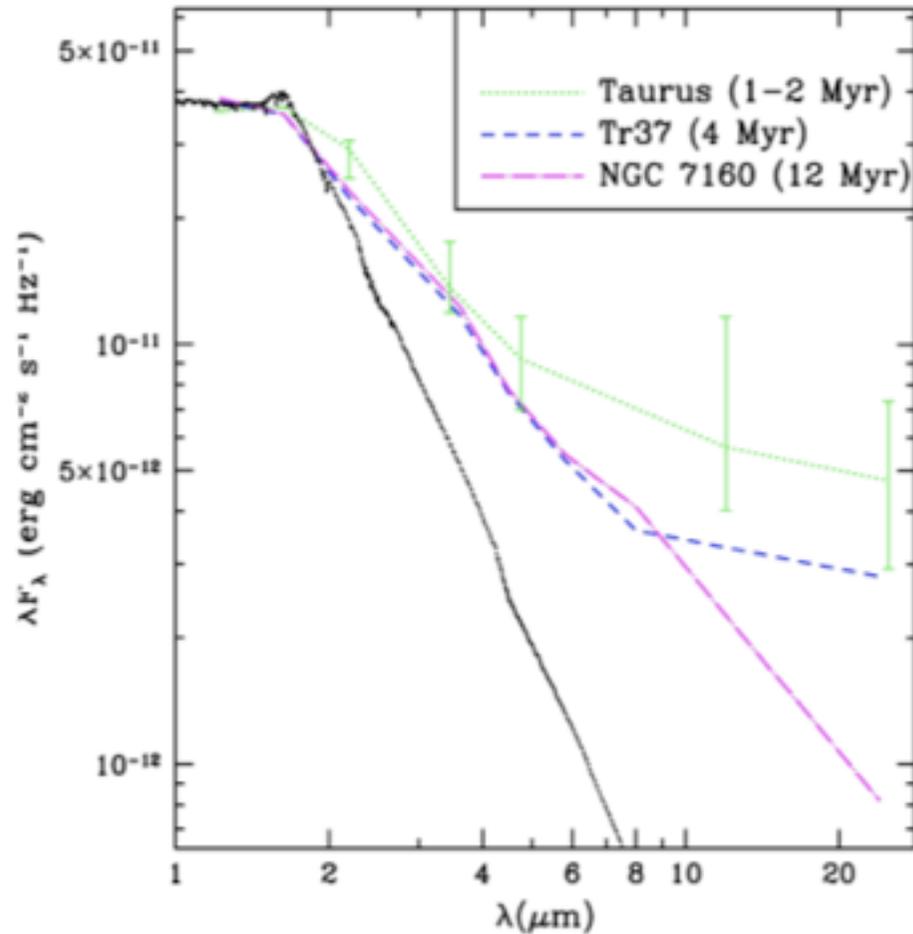
need larger type I migration to collect mass

# SED and evolution ?



No inclination, gas and dust in equilibrium, etc...

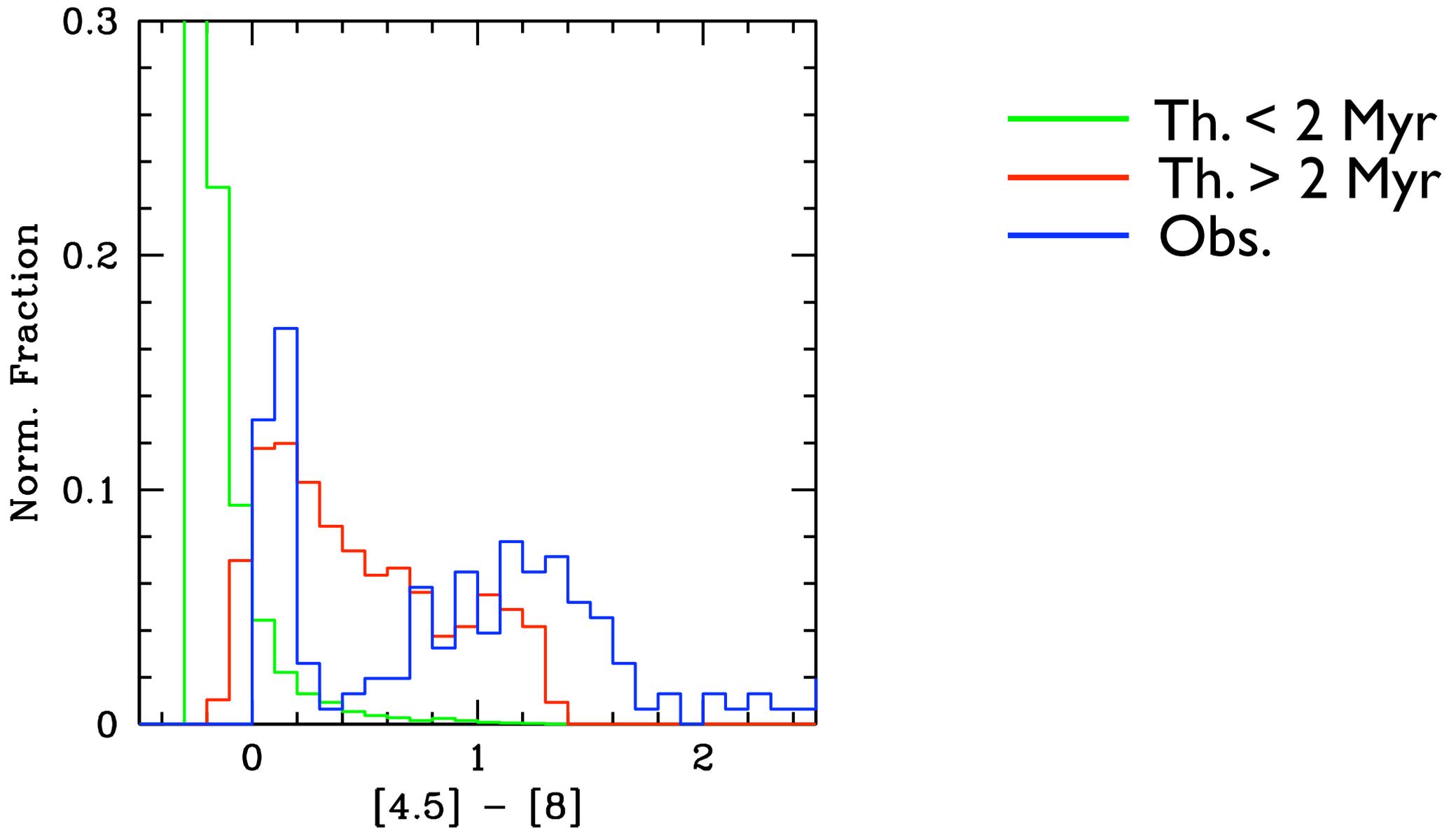
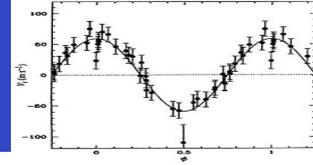
Sicilia-Aguilar et al. 2006



$R_{\text{disk}} = 0.05 \text{ AU} \rightarrow 3000 \text{ AU}$   
 $\Sigma_{\text{disk}} = 900 \text{ g/cm}^2$

homologous depletion of disks (Thayne's talk)

# SED and evolution ?



Many thanks to Luisa Rebull and collaborators for providing the unpublished Spitzer photometry

# Conclusions

- **first generation extended models allow quantitative predictions and can:**
  - reproduce the diversity of the exoplanets
  - fit RV data for G stars, with high KS values
- disk structure and evolution is a key ingredient for these models
- **second generation of models will focus on comparison with disks:**
  - disk properties for different stellar type
  - disk evolution / SED

